

# Low-Power System Design

227-0781-00L

Fall Semester 2019

Jan Beutel

# Plan for Today

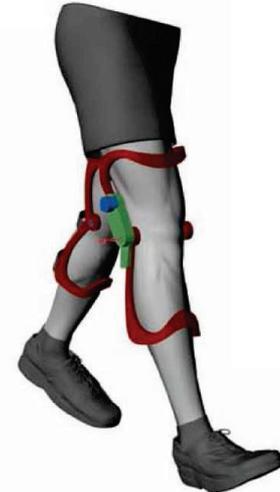
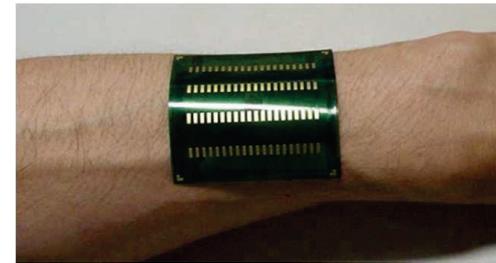
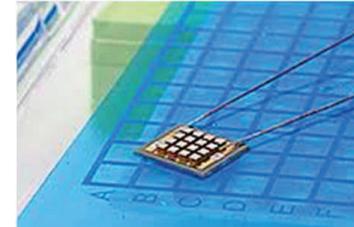
- Renewable Energy Sources – Harvesting Systems
- Energy Harvesting Systems Integration
  - Maximum Power Point Tracking
- System Design
  - TEG- based Energy Scavenging
- Modeling
  - Harvesting Control
  - Battery State-of-Charge Approximation
  - Long-term Energy Neutral Operation
- Slides contain material from J. Rabaey, D. Brunelli, D. Bernath, C. Moser and B. Buchli

Low-Power System Design

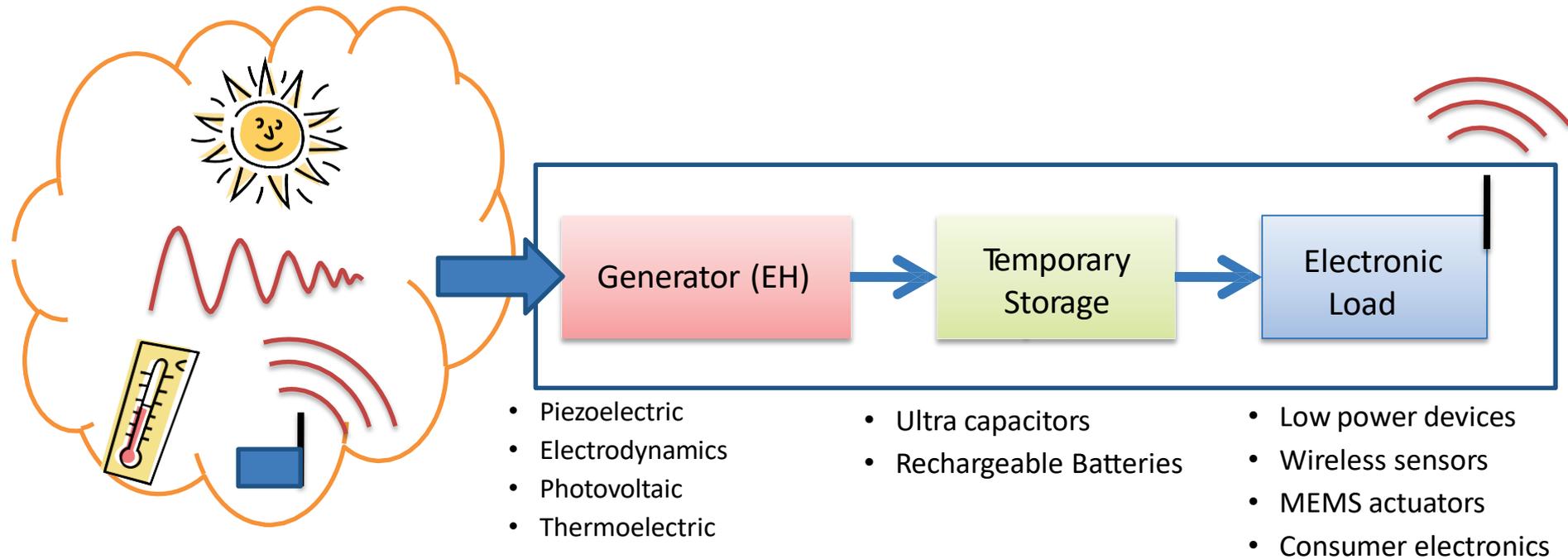
# **RENEWABLE ENERGY SOURCES – HARVESTING SYSTEMS**

# Energy Harvesting Basics

- **Energy harvesting** is the process by which energy is **captured** and **stored**
- This term often refers to small, autonomous devices: **micro energy harvesting**
  - Energy harvesting shrinks or replaces batteries or extends recharge periods
  - Power output of energy harvesting transducers is linked to their size (area, volume) and thus to their price
  - Power addresses matching of loads and supplies aiming at the maximum energy output



# Energy Harvesting Principle

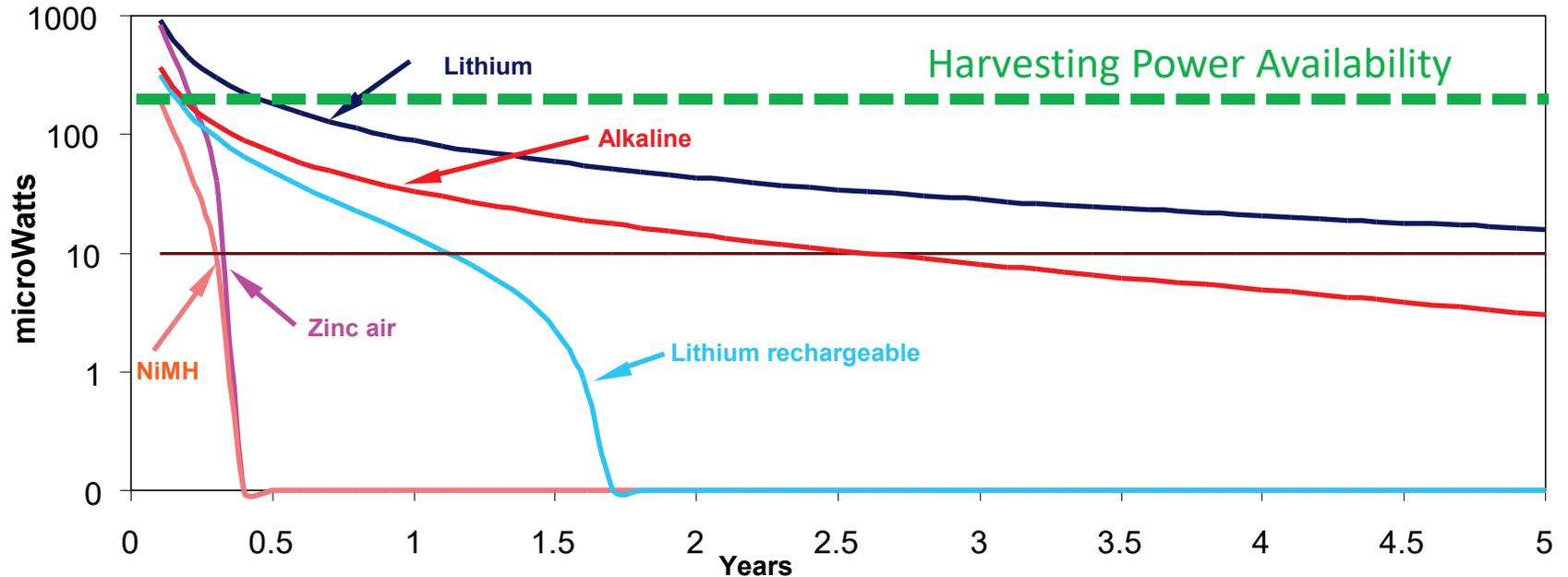


## • Benefits

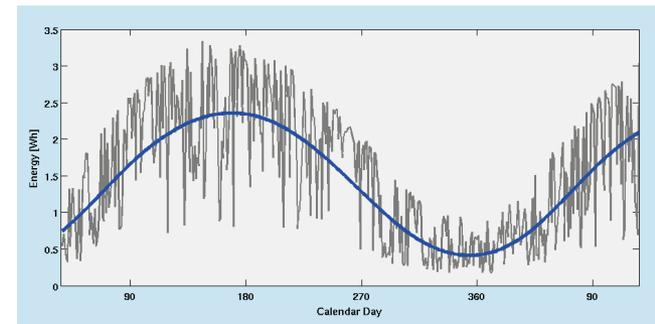
- Long lasting operability
- No chemical disposal
- Cost saving
- Safety
- Maintenance free
- No charging points
- Inaccessible sites operability
- Flexibility
- Applications otherwise impossible

# Extending the Lifetime

Continuous Power / cm<sup>3</sup> vs. Life Several Energy Sources



- Of course life is not quite so easy: The energy harvesting (input) exhibits fluctuations



# Available Energy is All Around

Light



EM waves



Motion and vibration

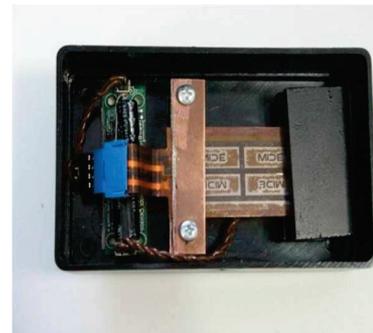
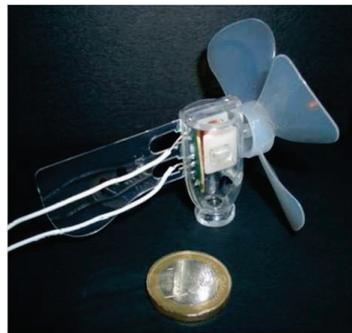
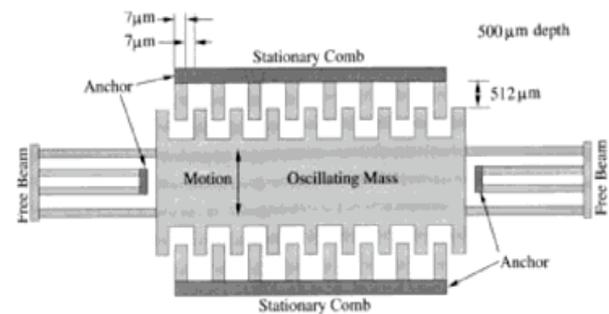
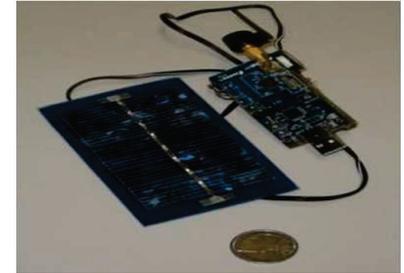


Heat



# Ambient Energy Sources

- Light
  - Photovoltaic cells 10  $\mu\text{W}/\text{cm}^2$  to 15  $\text{mW}/\text{cm}^2$
- Temperature gradients
  - 80  $\mu\text{W}/\text{cm}^2$  @ 1V from 5K difference
- Mechanical sources
  - Vibrations 0.1 to 10000  $\mu\text{W}/\text{cm}^2$
  - Pressure variation
  - Acceleration
  - Air/liquid flow
- Radiation
  - RF sources
  - Nuclear radiation



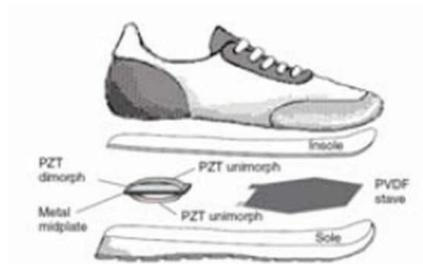
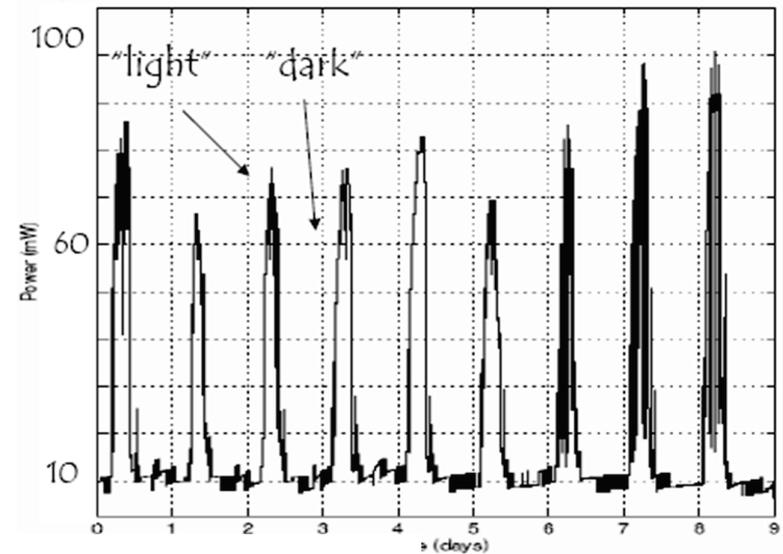
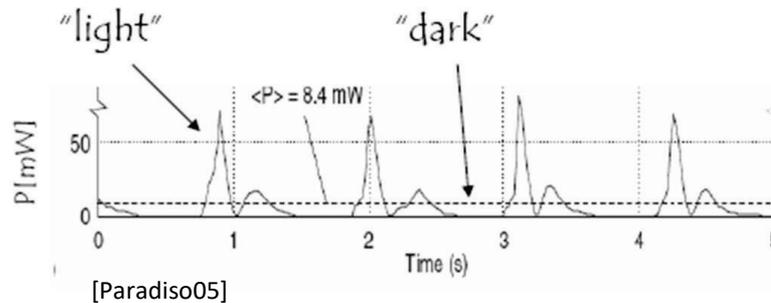
# Energy Harvesting Sources

Energy Source	Source Polarity	Efficiency	Harvested Power	Characteristics
Light	DC	10-24%	100 mW/cm <sup>2</sup> (Outdoor)	Operating conditions vary widely with environment light level. MPPT algorithms needed to achieve maximum power transfer
			100 μW/cm <sup>2</sup> (illuminated office)	
Thermal	DC	~0.1%	60 μW/cm <sup>2</sup> (Human)	Low output voltage. Step-up circuit needed. Impedance matching to achieve maximum power transfer
		~3%	~1-10 mW/cm <sup>2</sup> (Industrial)	
Vibration	AC	25-50%	~4 μW/cm <sup>3</sup> (Human motion - Hz)	High AC output voltage with positive and negative fluctuations (spikes). Rectifier & Step-down circuits are needed.
			~800 μW/cm <sup>3</sup> (Machines - KHz)	
Ambient Air flow	AC	~39% (Dynamic)	35 μW/cm <sup>2</sup> (@ <1 m/s)	Dual or 3-phase output. Rectifier is needed. MPP varies slightly with wind speed. Impedance matching is sufficient to achieve maximum power transfer in many applications
		~41% (Generator)	3.5 mW/cm <sup>2</sup> (@ 8.4 m/s)	
RF	AC	~50%	0.1 μW/cm <sup>2</sup> (GSM 900 MHz) 0.001 mW/cm <sup>2</sup> (WiFi)	Impedance matching to achieve maximum power transfer

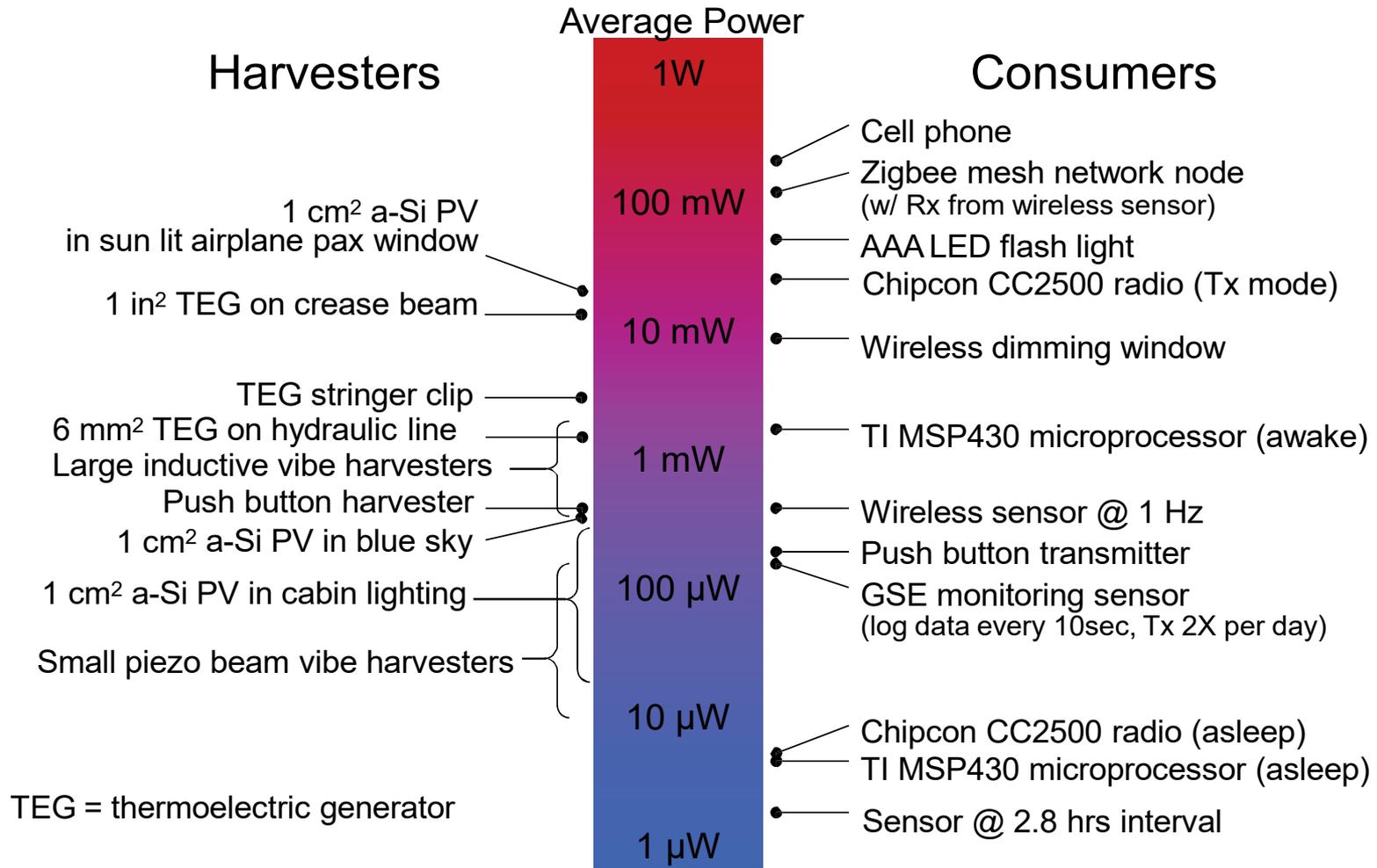
# Ambient Energy

## Non-monotone, Unpredictable

- Example: Solar power (PV-cells)
- Example: Power waveform from human walk (piezo-scavengers)



# Power Generation & Utilization



# Technology: Solar Power

- Max. power density for outdoor solar is  $1000 \text{ W/m}^2$  or  $100 \text{ mW/cm}^2$ 
  - At midday, summer, no clouds, right angle reception
  - A night with full moon yields only  $1 \text{ mW/m}^2$
  - Winter solar energy (in Europe) is about  $1/10^{\text{th}}$  of summer
  - Indoors  $500\text{-}1000 \text{ mW/m}^2$
  - Attenuation over distance is very strong

Distance	20cm	30cm	45 cm	Office Light
$\mu\text{W/cm}^2$	503	236	111	7.2

Power densities measured indoors from a 60 Watt incandescent light bulb

- Typical solar cell efficiencies: 10-20%
  - 2-5% for very cheap/small cells

# Technology: Solar Panel Characteristics

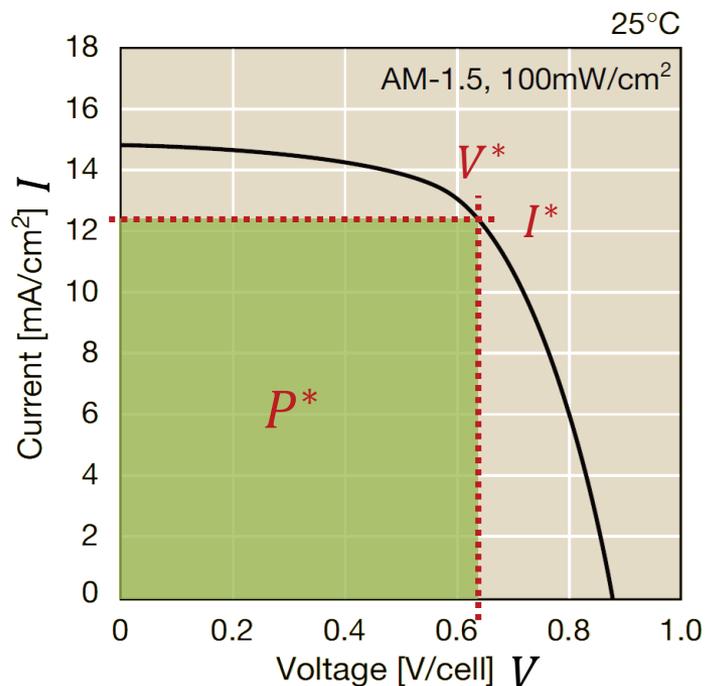
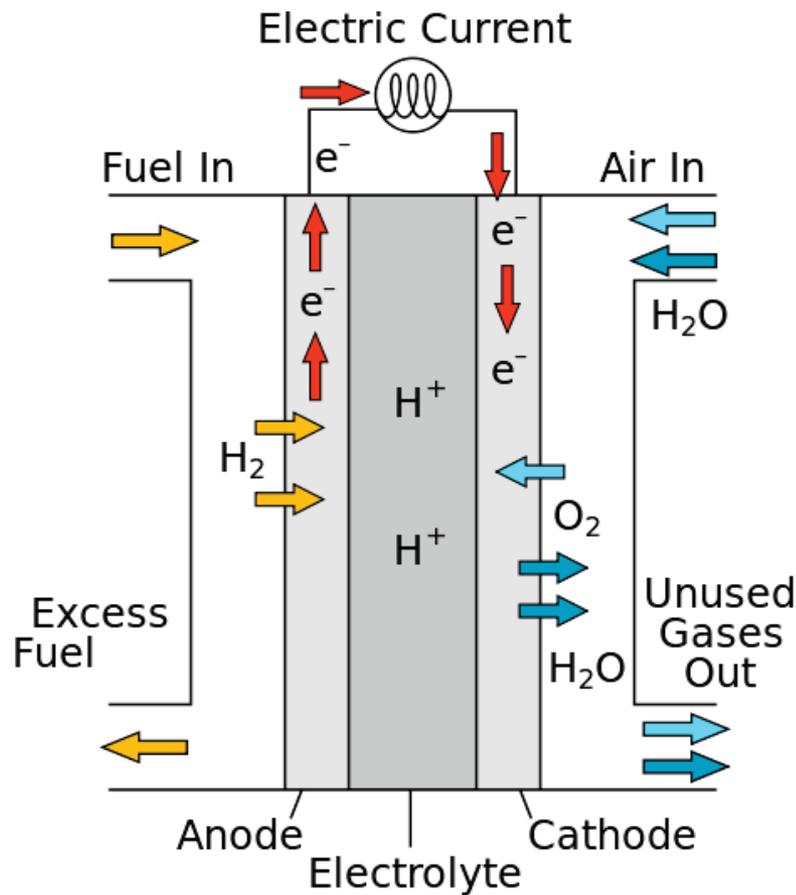


Diagram: Amorton Amorphous Silicon Solar Cells Datasheet, © Panasonic

- Variable output power
  - Illuminance level
  - Electrical operation point
  - (Temperature, age, ...)
- I-V-Characteristics
  - Non-linear
- Efficient Use
  - Dynamic algorithms to find  $P^*$

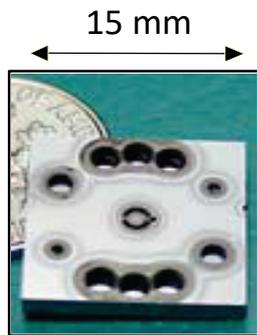
# Technology: Micro-Fuel Cells



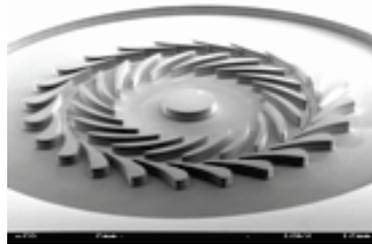
- Max current is a limiting factor due to surface area constraints (as with micro-batteries).
- Methanol energy density is 17.6 kJ/cm<sup>3</sup>. (6 X lithium and 15 X rechargeable lithium).
- Efficiencies of large fuel cells is about 45% (up to almost 90% if cogeneration is employed.)
- Efficiencies of demonstrated micro-fuel cells are on the order of 1% (Holladay et al. 2002).
- Products are not really micro

# Technology: Micro-Heat Engines

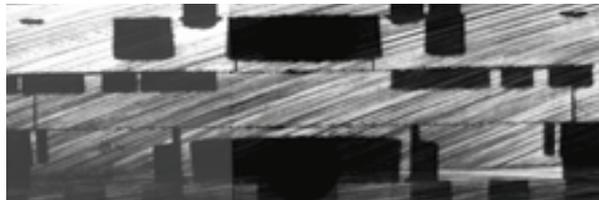
4 mm Turbine – top view



ROTOR



Microturbine bearing rig



4 mm dia

- Research started by Epstein et al. 1997. Many types of engines are now being developed
- Petrol (gasoline) energy density is  $30 \text{ kJ/cm}^3$ 
  - 10 X lithium and 25 X rechargeable lithium
- Expected efficiencies range from 5% to 20%
- 0.1 to 10 W output
- Size  $\sim 1 \text{ cm}^3$

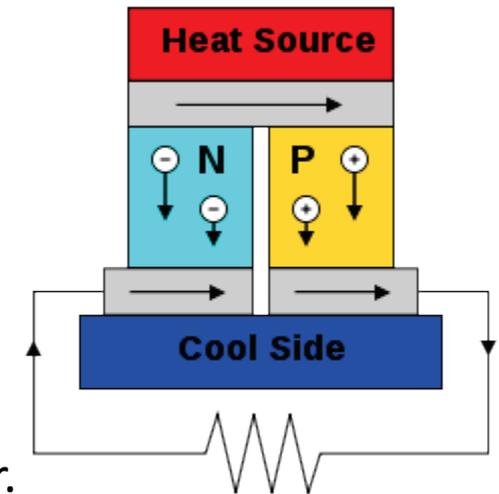
# Technology: Thermal Gradients

- **Seebeck effect** is the conversion of temperature differences (heat flux) directly into electricity

- Efficiency is given by:

$$\eta = \frac{\Delta T}{T}$$

- At  $T = 20^\circ\text{C}$  and  $\Delta T = 5^\circ\text{C}$ ,  $\eta = 1.6\%$
- However, demonstrated efficiencies are far lower.

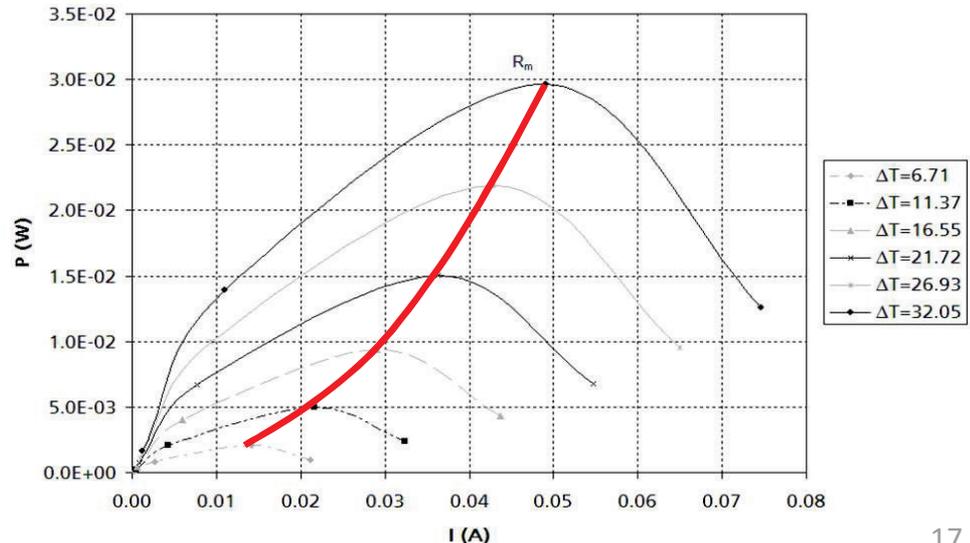
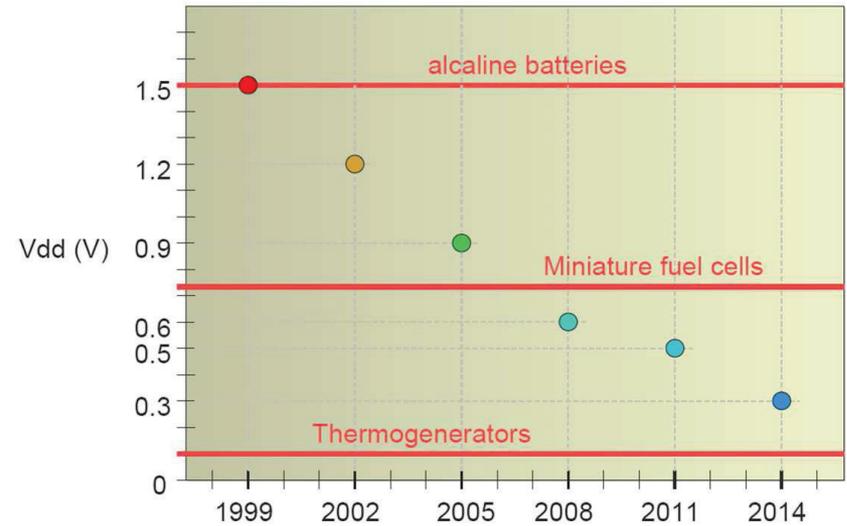


- Power is proportional to  $\Delta T^2$

$$P_{out} \propto \frac{\Delta T^2}{T}$$

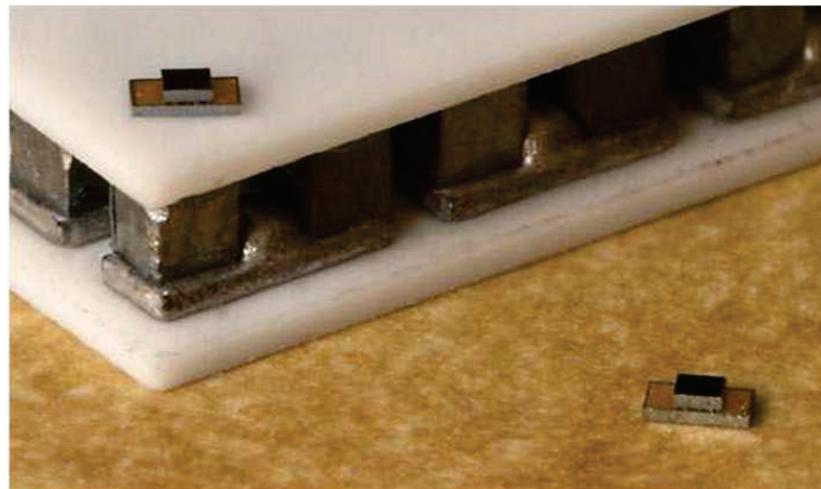
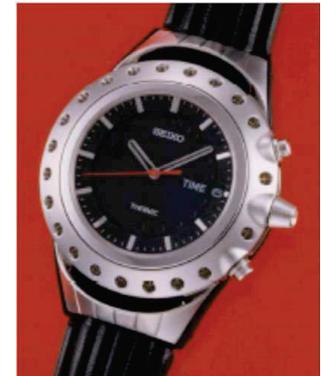
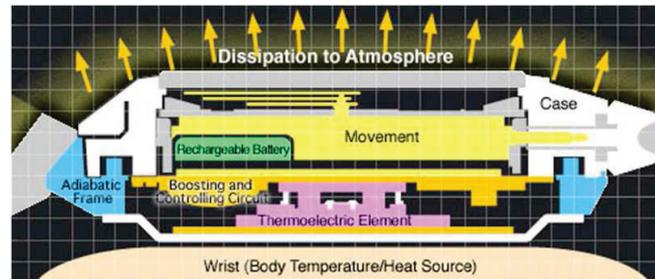
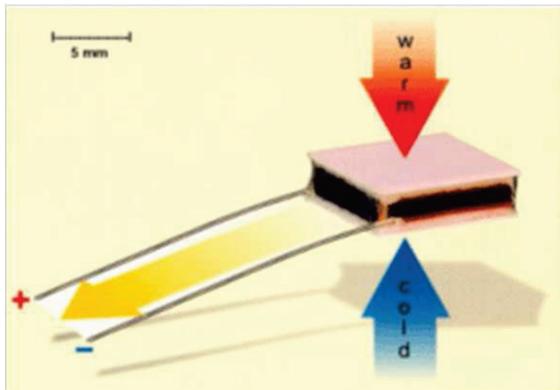
# TEG Characteristics

- TEGs output voltage is very low
- TEGs have a maximum power point (MPP) which changes with  $\Delta T$
- MPP is usually the half of the open circuit voltage ( $V_{\text{teg}} - V_{\text{oc}}$ )
- Problem
  - Internal resistance of TEG depends on temperature and aging



# Example: Thermo Electric Generator

Seiko Thermic wristwatch, convert heat from the wrist (body heat) into electricity.



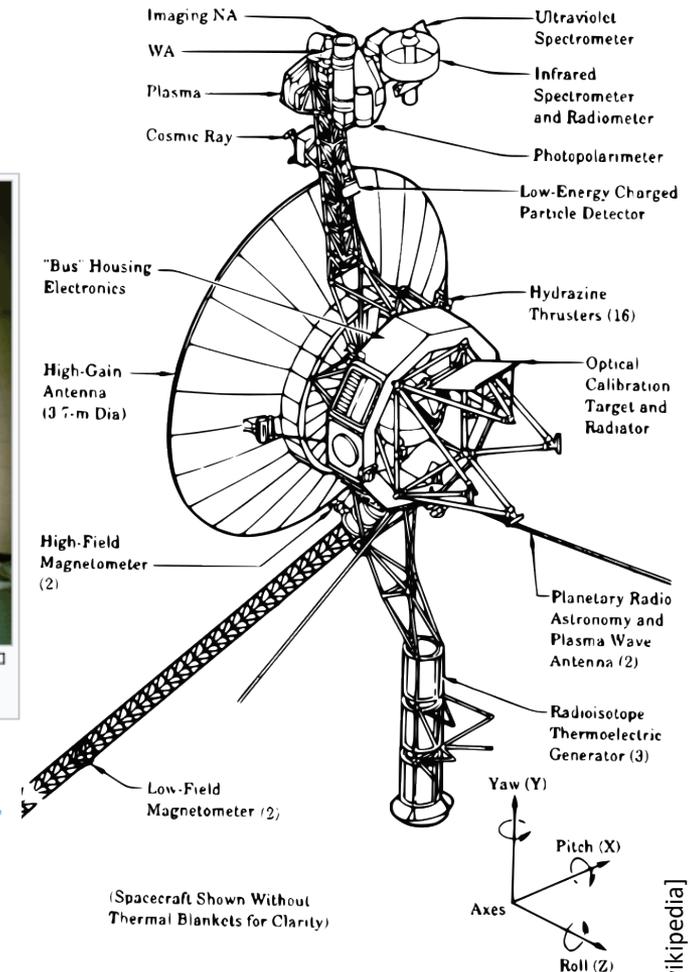
# Powering the Voyager Spacecraft

## Power [edit]

Electrical power is supplied by three MHW-RTG radioisotope thermoelectric generators (RTGs). They are powered by plutonium-238 (distinct from the Pu-239 isotope used in nuclear weapons) and provided approximately 470 W at 30 volts DC when the spacecraft was launched. Plutonium-238 decays with a half-life of 87.74 years,<sup>[28]</sup> so RTGs using Pu-238 will lose a factor of  $1 - 0.5^{(1/87.74)} = 0.79\%$  of their power output per year.

In 2011, 34 years after launch, such an RTG would inherently produce  $470 \text{ W} \times 2^{-(34/87.74)} \approx 359 \text{ W}$ , about 76% of its initial power. Additionally, the thermocouples that convert heat into electricity also degrade, reducing available power below this calculated level.

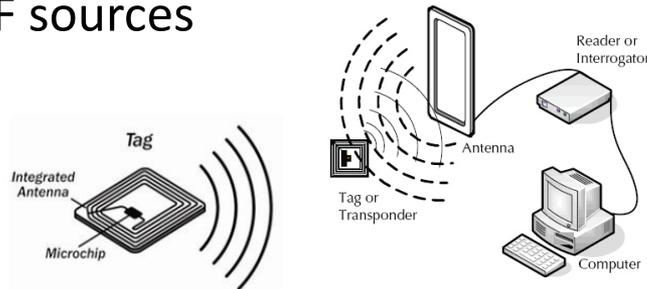
By 7 October 2011 the power generated by Voyager 1 and Voyager 2 had dropped to 267.9 W and 269.2 W respectively, about 57% of the power at launch. The level of power output was better than pre-launch predictions based on a conservative thermocouple degradation model. As the electrical power decreases, spacecraft loads must be turned off, eliminating some capabilities. There may be insufficient power for communications by 2032.<sup>[29]</sup>



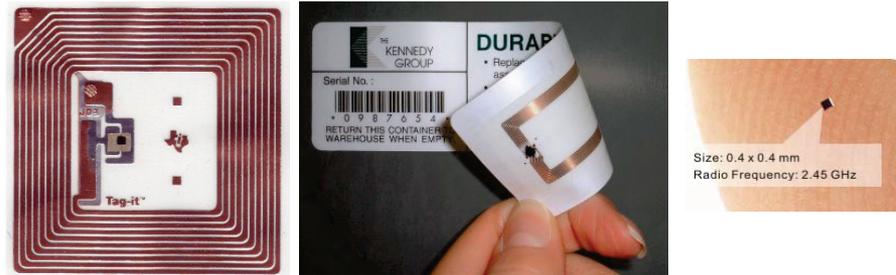
[wikipedia]

# Technology: RF Radiation Sources

- Remote powering of systems from RF sources



- Inductive coupling using a large excitation coil and a small pickup coil
  - Medical Implants
  - RFID Tags
  - Smart Cards
  - Wristwatches
  - Badges
- Experimental systems with higher power capabilities are explored



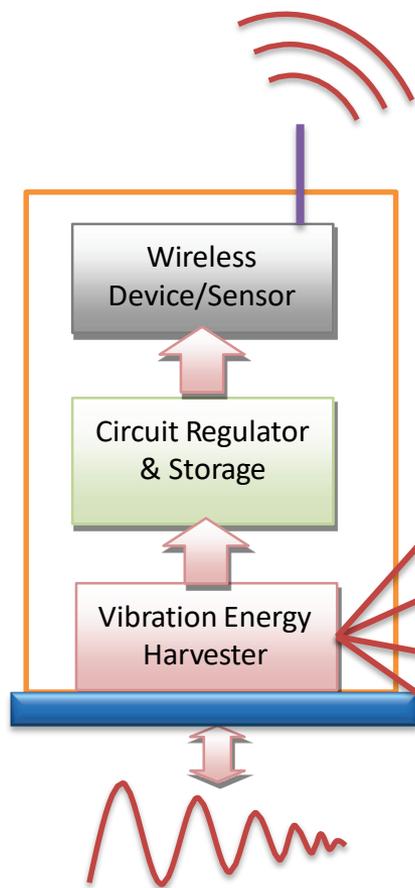
- Issue: Attenuation

$$P_r = \frac{P_o \lambda^2}{4\pi R^2}$$

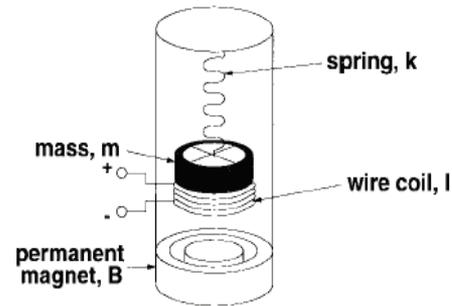
$P_o$  = transmit power  
 $P_r$  = power received  
 $\lambda$  = wavelength  
 $R$  = transmit distance

- Example  
2.4 GHz, 5 meters,  $P_o = 1$  watt,  $P_r = 50$  uW
- Probably not useful for a dense sensor networks, but useful in many applications

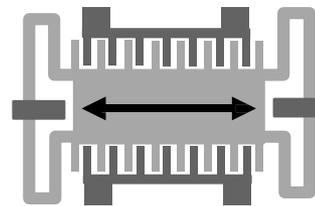
# Technology: Vibration Energy Harvesting



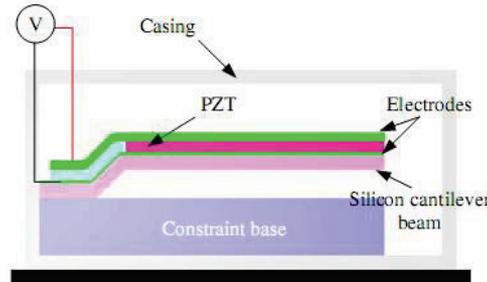
- Ambient vibrations
- Human motion
- Wind, Hydro



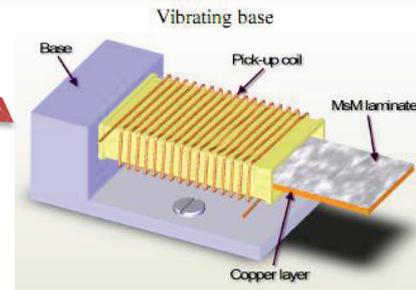
Electromagnetic



Electrostatic/Capacitive



Piezoelectric



Magnetostrictive

# Vibrations – Electrostatic Conversion

- Generic vibration power conversion model (adapted from William et al. 1995)

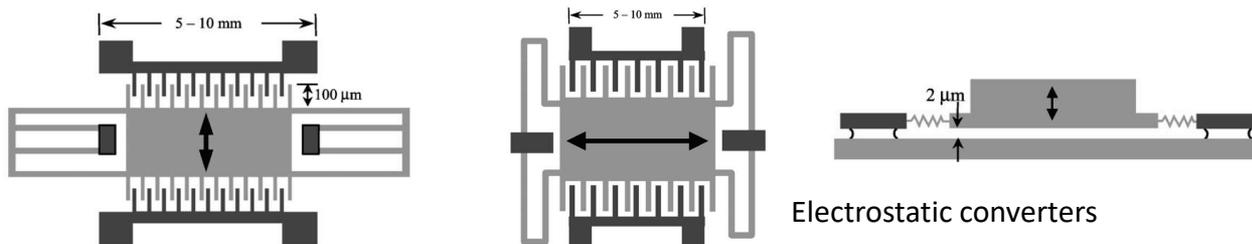
$$P = \frac{m \zeta_e^2 A^2}{4\omega(\zeta_e + \zeta_m)^2}$$

$m$  is the proof mass  
 $\zeta_e$  is the electrically induced damping ratio  
 $\zeta_m$  is the mechanical damping ratio  
 $A$  is the acc. amplitude of the vibrations  
 $\omega$  is the resonant freq. and input freq.

Vibration Source	Peak Acc. (m/s <sup>2</sup> )	Freq. (Hz)
Base of 3-axis machine tool	10	70
Kitchen blender casing	6.4	121
Clothes dryer	3.5	121
Door frame just as door closes	3	125
Small microwave oven HVAC vents in office building	2.25	121
Wooden deck with foot traffic	0.2 – 1.5	60
Breadmaker	1.3	385
External windows next to street	1.03	121
Notebook computer w/ CD.	0.7	100
Washing machine	0.6	75
Second story floor of a wood frame office building	0.5	109
Refrigerator	0.2	100
	0.1	240

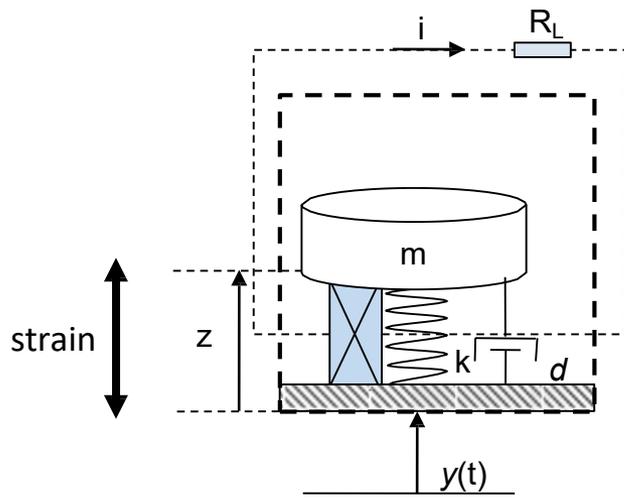
Acceleration magnitudes range from 0.1 to 10 m/s<sup>2</sup>.  
 Frequencies range from 60 to 200 Hz.

- Three things to notice from the model:
  - Power output is proportional to the mass of the device
  - Power is proportional to the square of the acceleration amplitude
  - Power output is inversely proportional to frequency

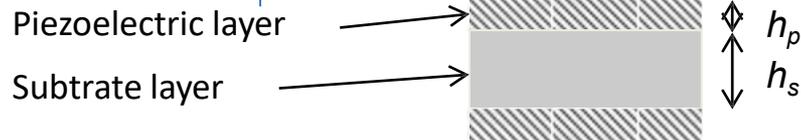
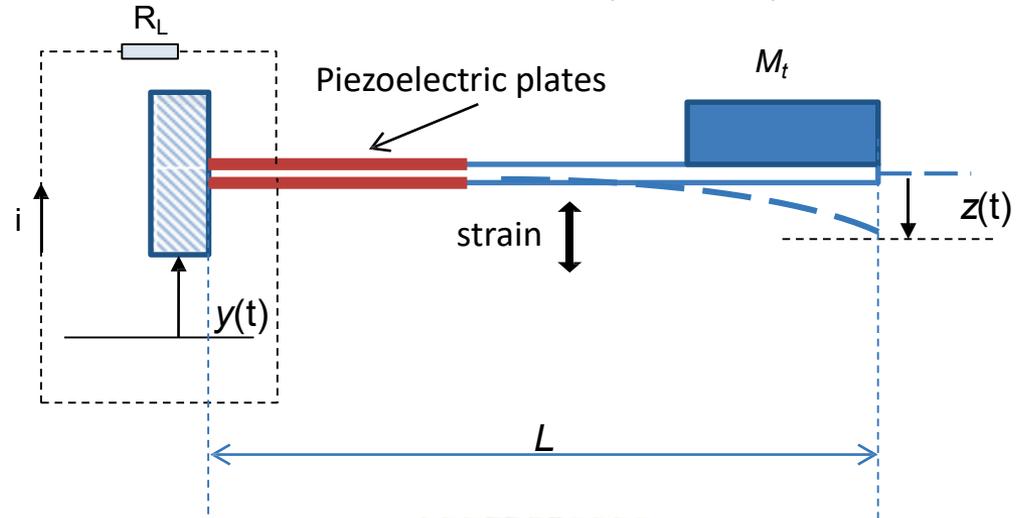


# Vibrations – Piezoelectric Conversion

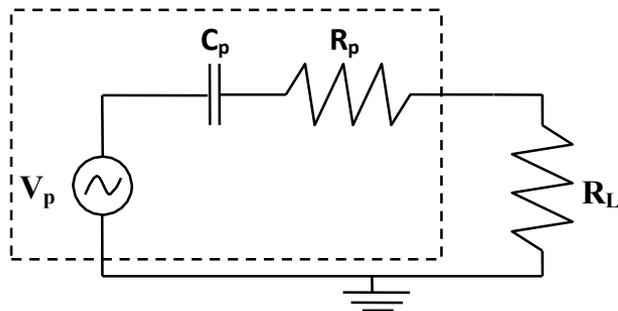
Piezoelectric bulk (33 mode)



Cantilever beam (31 mode)



Piezoelectric generator



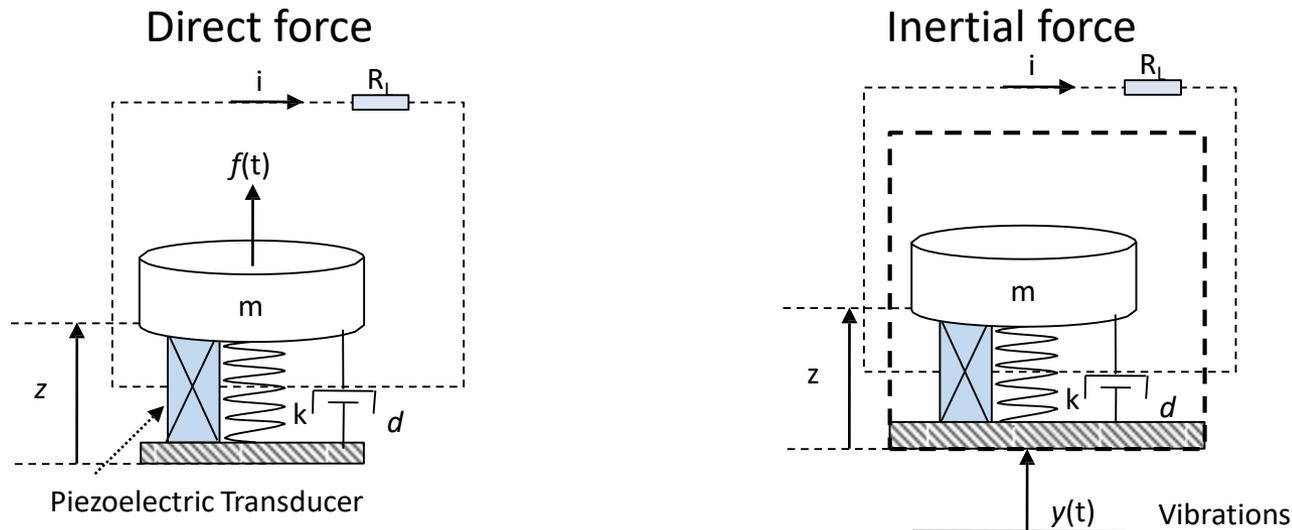
At open circuit

$$V_{oc} = - \frac{d_{31}h}{\epsilon S} T_1$$

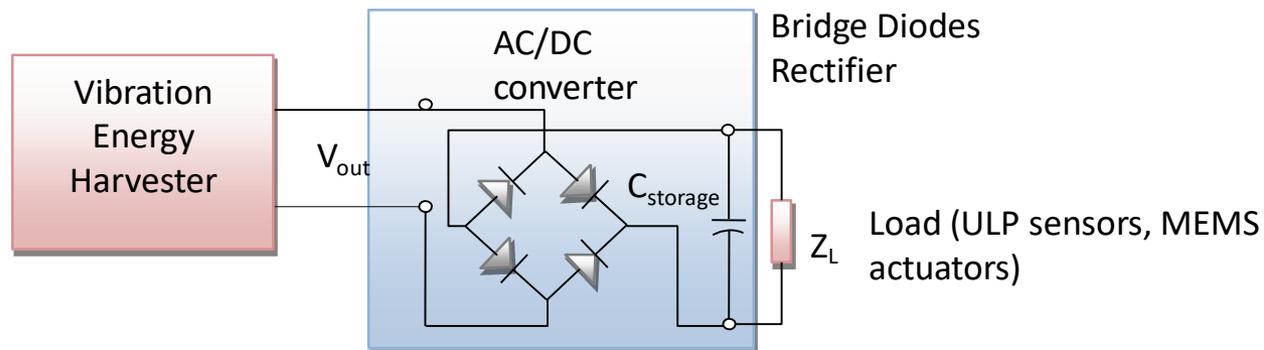
The power delivered to the load is simply

$$P = \frac{V_L^2}{R_L}$$

# Vibration – Basic Operating Principles



- Inertial generators are more flexible than direct-force devices because they require only one point of attachment to a moving structure, allowing a greater degree of miniaturization.



# Energy Harvesting Methods - Overview

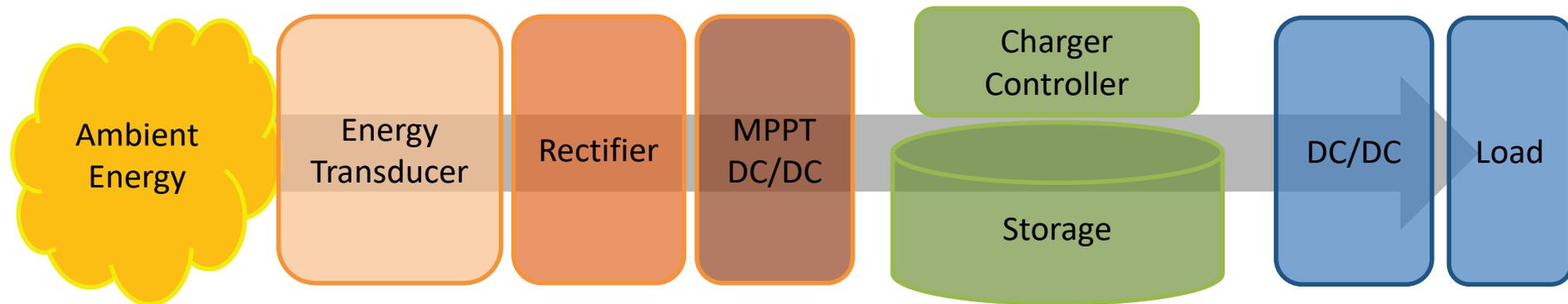
Power Source	P/cm <sup>3</sup> ( $\mu$ W/cm <sup>3</sup> )	E/cm <sup>3</sup> (J/cm <sup>3</sup> )	P/cm <sup>3</sup> /a ( $\mu$ W/cm <sup>3</sup> /a)	Secondary Storage Needed	Voltage Regulation	Comm. Available
Primary Battery	-	2880	90	No	No	Yes
Secondary Battery	-	1080	34	-	No	Yes
Micro-Fuel Cell	-	3500	110	Maybe	Maybe	No
Ultra-capacitor	-	50-100	1.6-3.2	No	Yes	Yes
Heat engine	-	3346	106	Yes	Yes	No
Radioactive( <sup>63</sup> Ni)	0.52	1640	0.52	Yes	Yes	No
Solar (outside)	15000	-	-	Usually	Maybe	Yes
Solar (inside)	10	-	-	Usually	Maybe	Yes
Temperature	40	-	-	Usually	Maybe	Upcoming
Human Power	330	-	-	Yes	Yes	No
Air flow	380	-	-	Yes	Yes	No
Pressure Variation	17	-	-	Yes	Yes	No
Vibrations	200	-	-	Yes	Yes	No

Low-Power System Design

# **ENERGY HARVESTING – SYSTEMS INTEGRATION**

# Generic Energy Harvesting Design

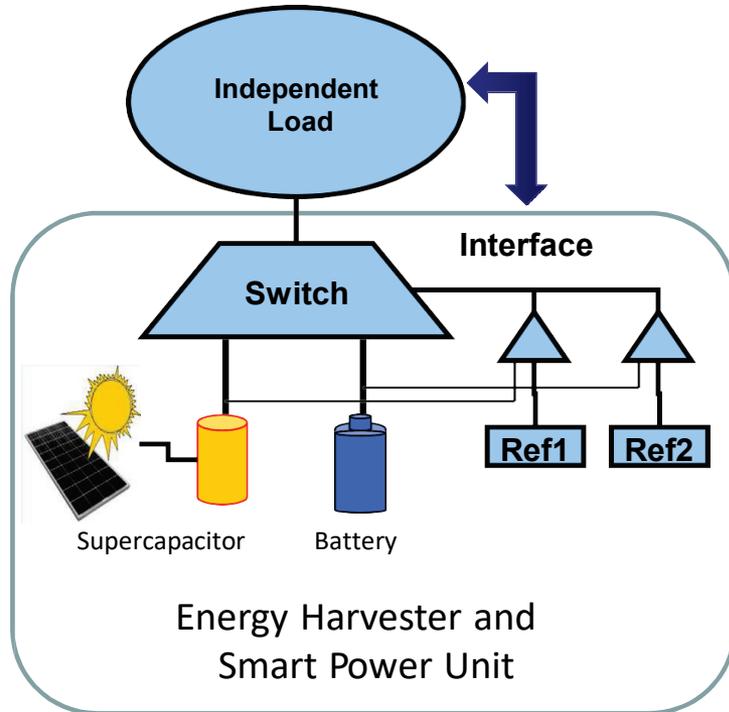
- **Dedicated blocks**, depending on energy source, ambient conditions and application
- **Not always all are required** in a given application/source
- Design process of rectifier, DC-DC converter and MPPT is **challenging**
- Charger/limiter/protection consumes additional power and are often to some extent redundant



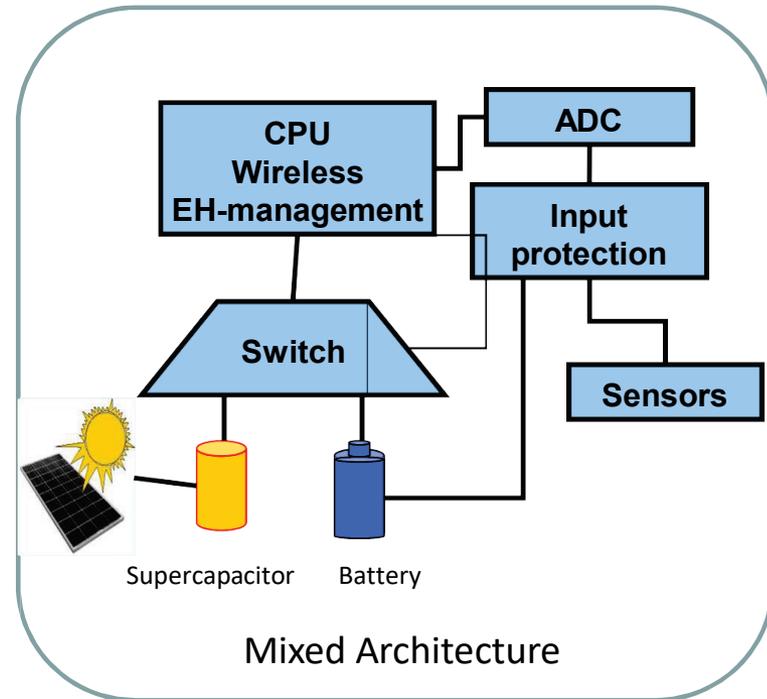
**Opens up significant control-space issues w.r.t. energy usage**

**This needs algorithmic/software support!**

# Integration Into Mixed Architectures



- General purpose
- Optimized from Ambient Source and storage, but not for a specific application
- Plug-&-play
- Analog or with digital Interface for external power management



- Usually more efficient
- Tailored on a specific application
- HW /SW dependent

# Electric Power – Source and Sink

- The instantaneous electric power delivered to a load is given by:

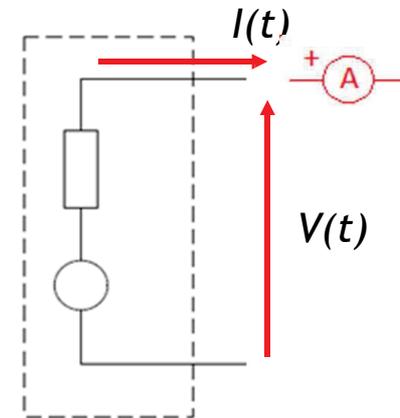
$$P(t) = I(t) V(t)$$

- In case of resistive loads, then

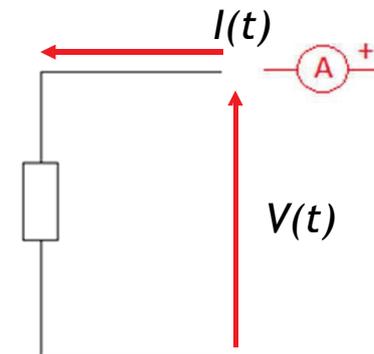
$$P(t) = R I(t)^2 = \frac{V(t)^2}{R}$$

- $P(t)$  is the **instantaneous power**, measured in Watts [W]
- $V(t)$  is the **voltage difference** across the load, measured in Volts [V]
- $I(t)$  is the **current** through it, measured in Amperes [A]
- $R$  is the **resistance**, measured in Ohms [ $\Omega$ ]

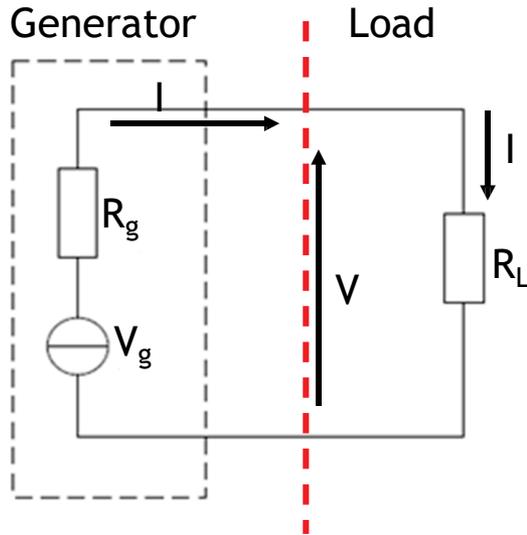
GENERATOR (delivered power  $>0$ )



USER (incoming power  $>0$ )



# Maximum Power Transfer



$$V_g - R_g I - R_L I = 0$$

$$I = \frac{V_g}{R_g + R_L}$$

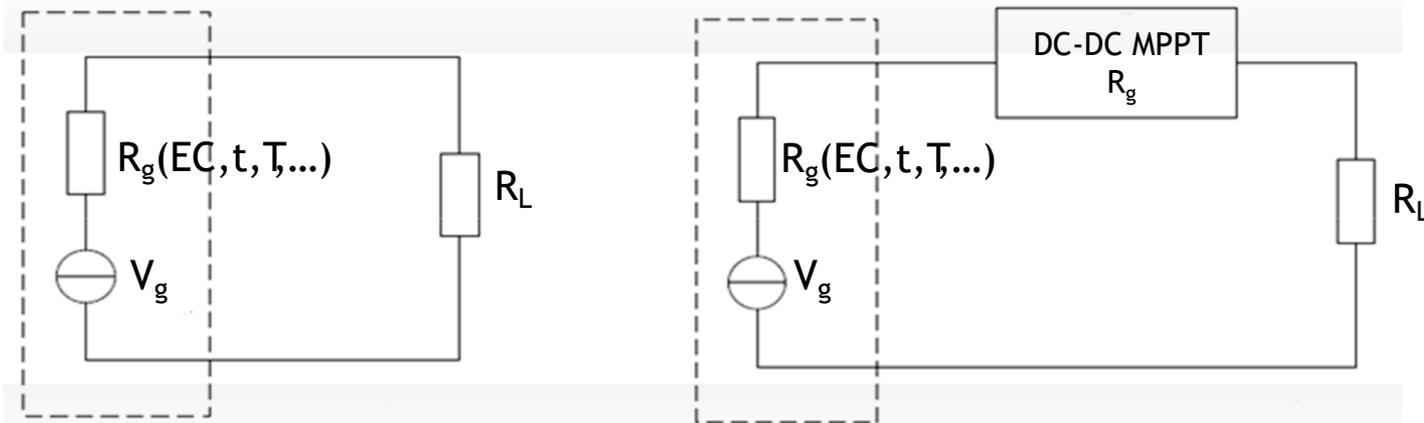
$$P = R_L I^2 = V_g^2 \frac{R_L}{(R_g + R_L)^2}$$

$$\max_{R_L}(P) \quad \rightarrow \quad \max_{R_L} \left( \frac{R_L}{R_g + R_L} \right) \quad \xrightarrow{\frac{dP}{dR_L} = 0} \quad \frac{(R_g + R_L)^2 - 2(R_g + R_L)^2 R_L}{(R_g + R_L)^4} = 0$$

$$R_L = R_g \quad \text{Resistance Matching}$$

# Maximum Power Point Tracking

- Maximum power from source to load when internal resistances are matched
- Input resistance of a DC-DC converter is influenced with its duty cycle
- $R_g$  depends on several factors  $\rightarrow R_g$  (Environmental condition, time, temperature, ...)



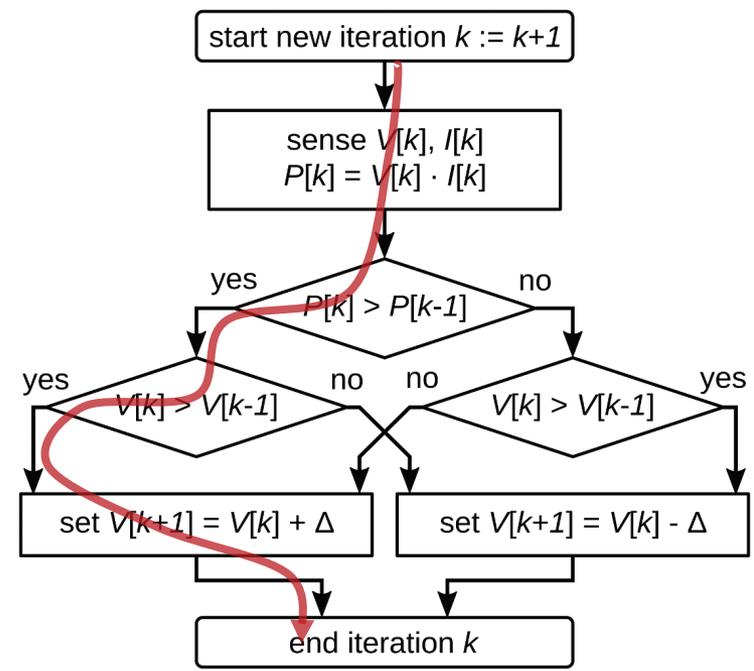
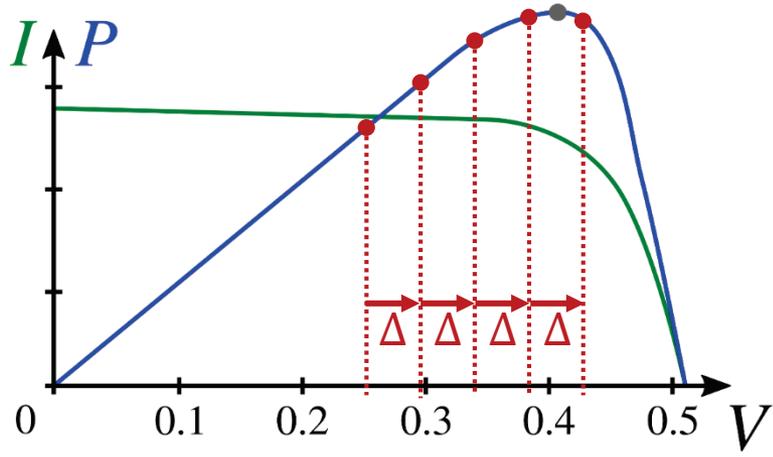
## ***Ideal situation:***

- Load  $R_L$  and internal resistance  $R_g$  are naturally matched
- $V_g$  in the correct range

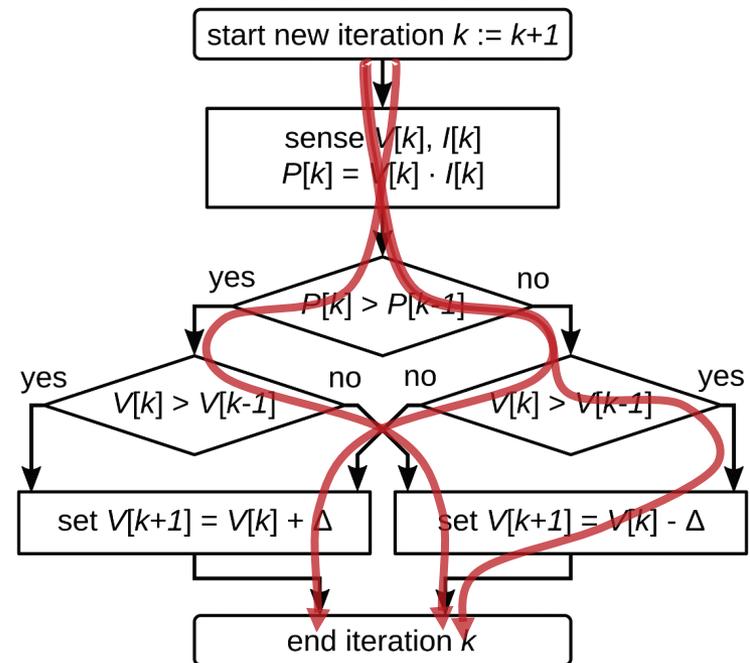
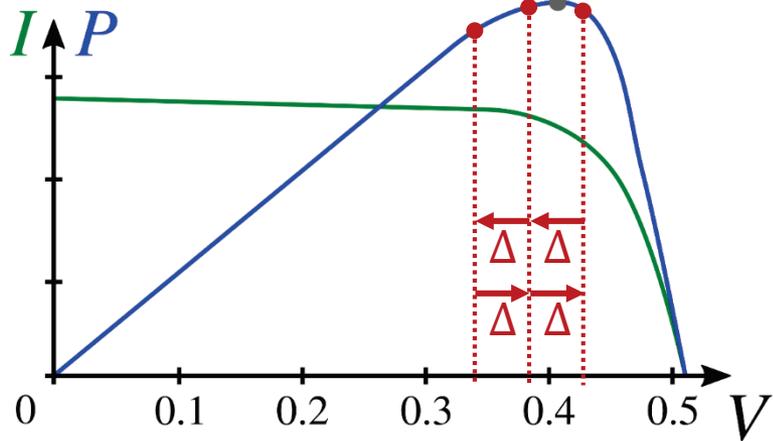
## ***Typical situation:***

- DC/DC with MPPT to match  $R_L$  and  $R_g$  and /or to adjust  $V_g$
- **MPPT adjusts resistance matching over time**

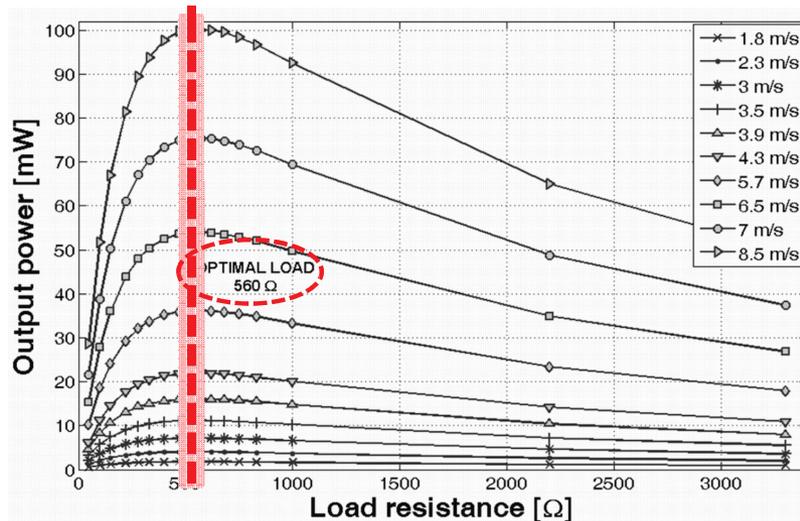
# Maximum Power Point Tracking



# Maximum Power Point Tracking

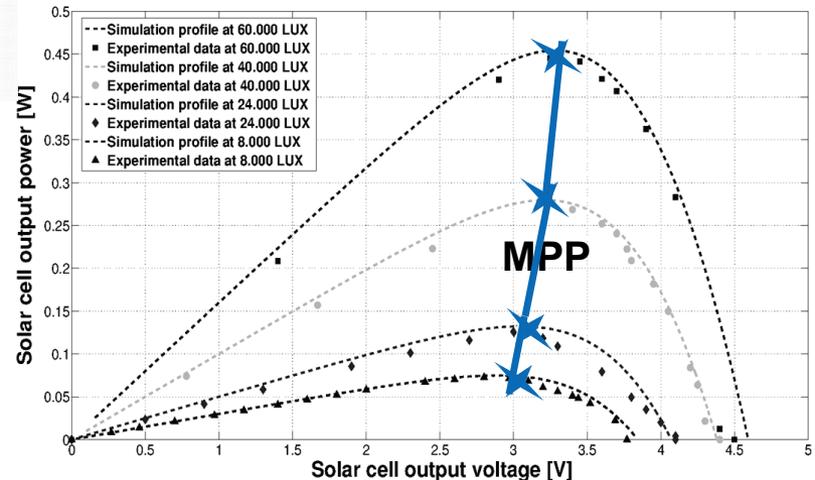


# Maximum Power Point Under Ambient Conditions



- Two main solutions:
  - Static impedance matching
  - Dynamic Maximum Power Point Tracking (MPPT)

- Two main cases:
  - MPP varies slightly with ambient conditions (e.g. wind generators)
  - Wide variations of the MPP (e.g. solar cells)

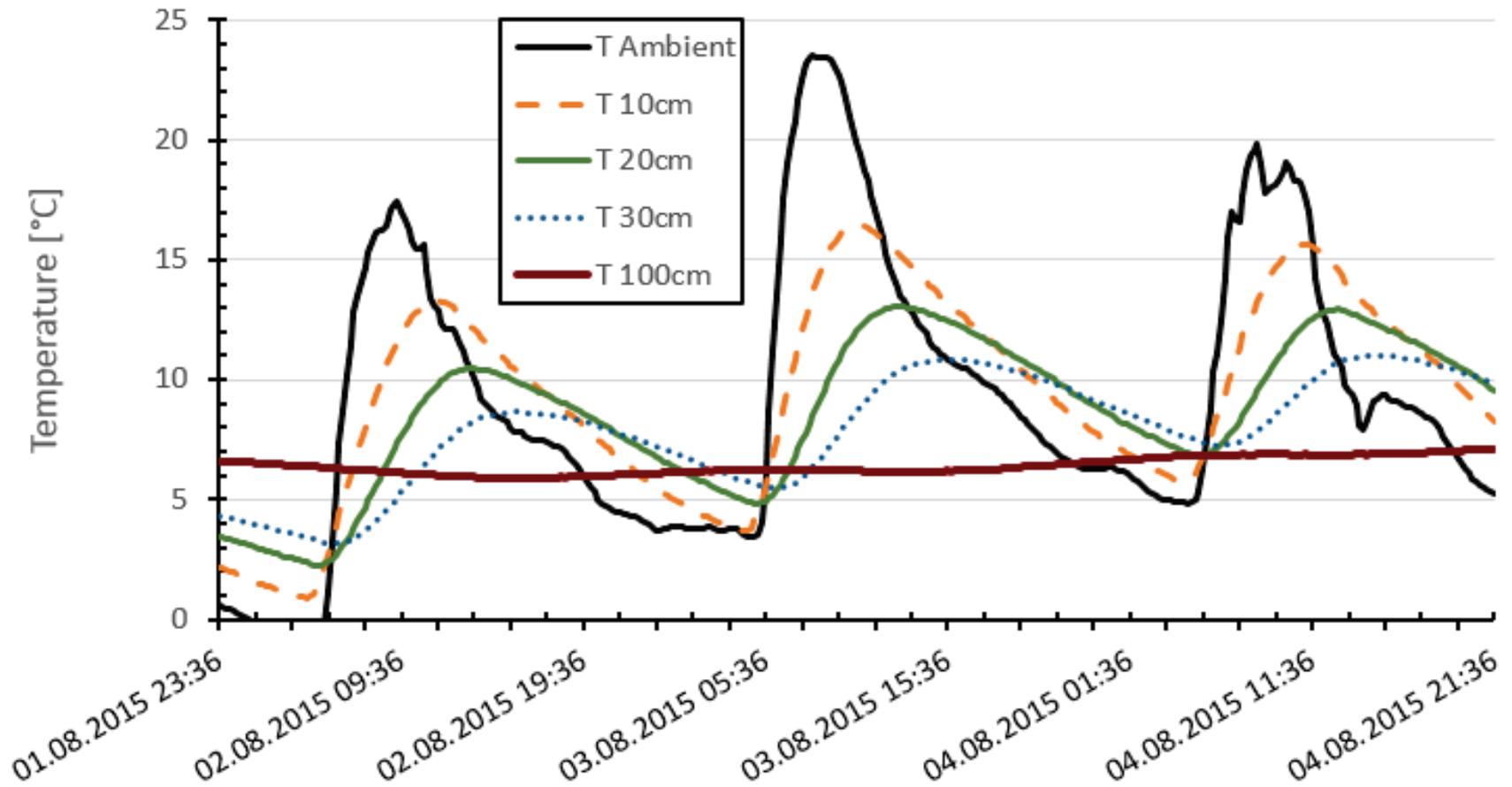


Low-Power System Design

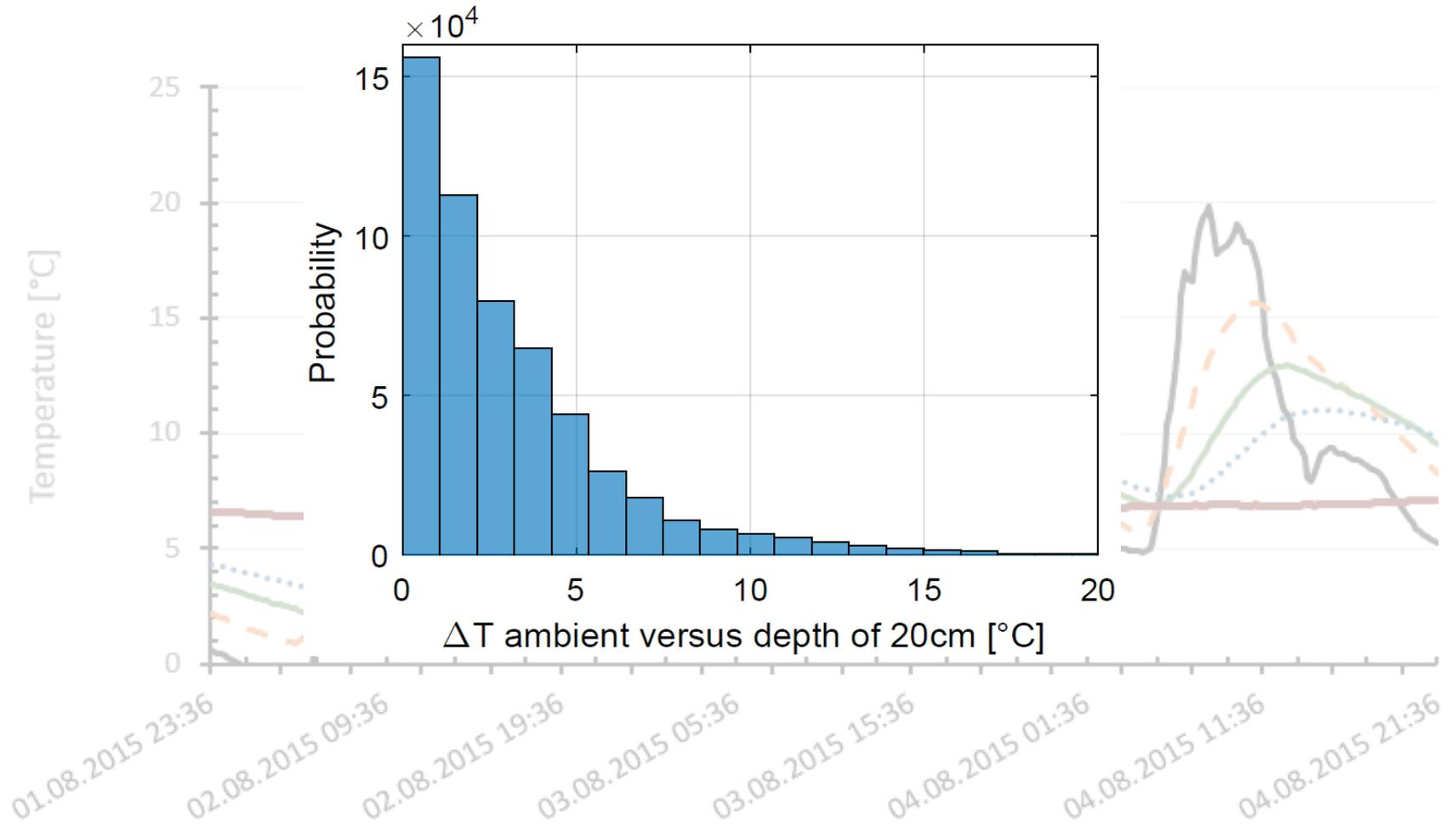
# **TEG-BASED ENERGY HARVESTING (FOR PERMASENSE SENSOR NODES)**

[Master Thesis by D. Bernath, 2016]

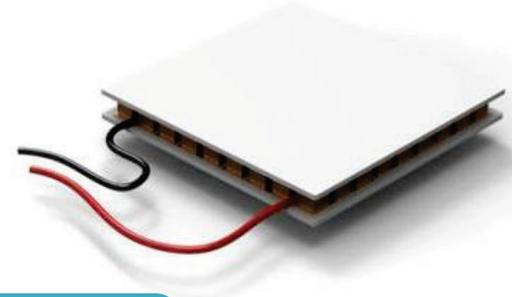
# Motivation – Diurnal Temperature Differences in Rock Walls



# Motivation – Diurnal Temperature Differences in Rock Walls



# Thermoelectric Generator (TEG)



$$V_{oc} = \alpha \cdot \Delta T_{TEG}$$

0-300 mV

$$P_{max} = \frac{\alpha^2}{4 \cdot R_{el\ TEG}} \cdot [\Delta T_{TEG}]^2 \ [W]$$

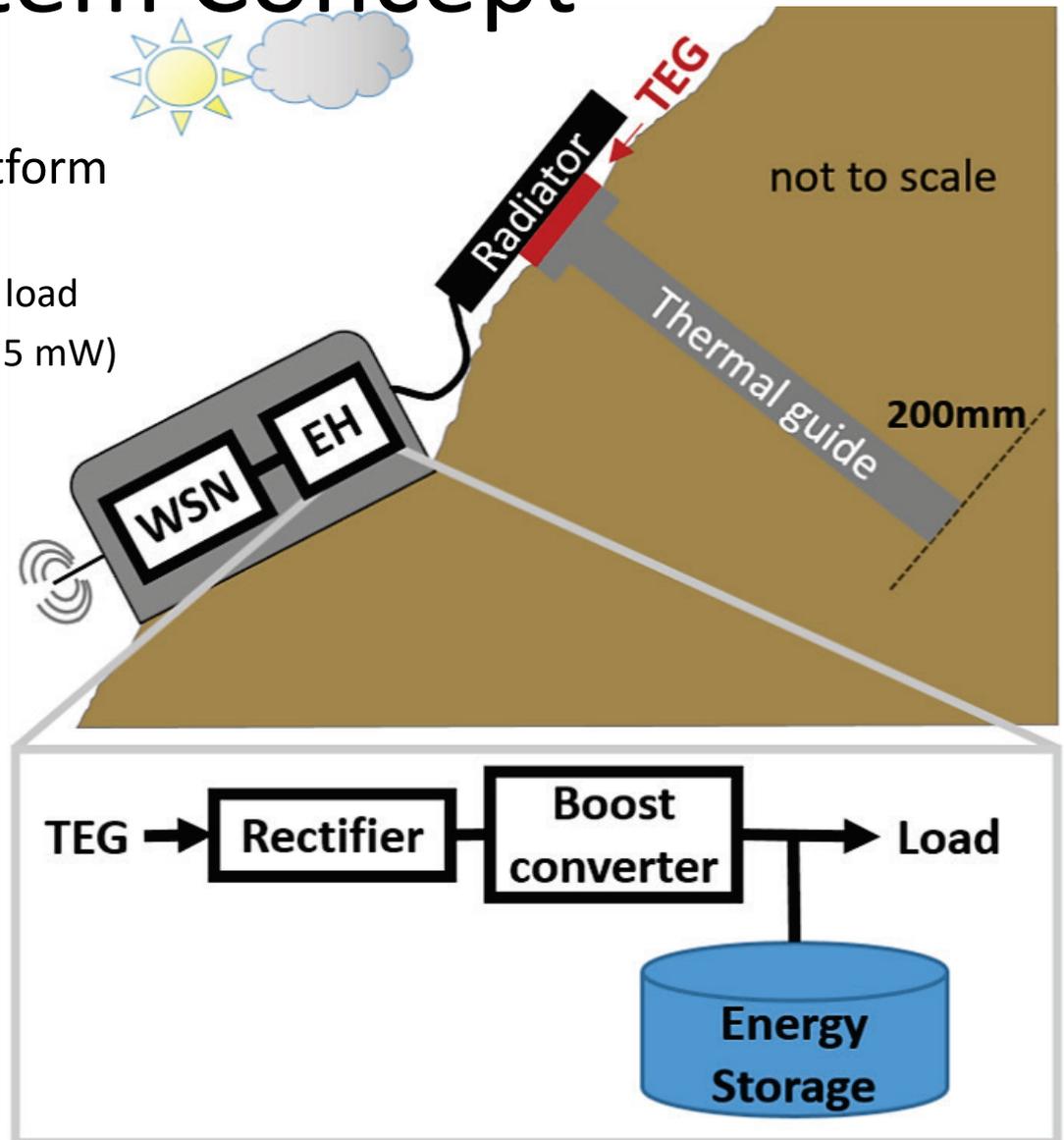
# System Concept

- Universal TEG Harvesting Platform

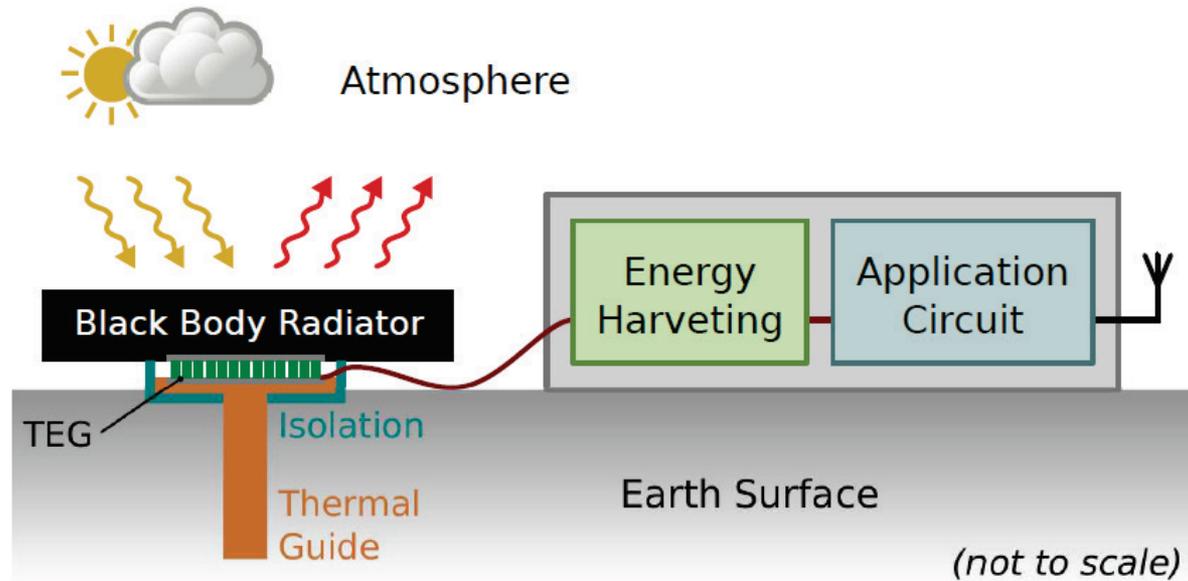
- Ground to atmosphere
- Supporting generic  $\sim 1\text{mW}$  class load
- Example: PermaSense WSN ( $\sim 0.5\text{ mW}$ )

- Optimization areas

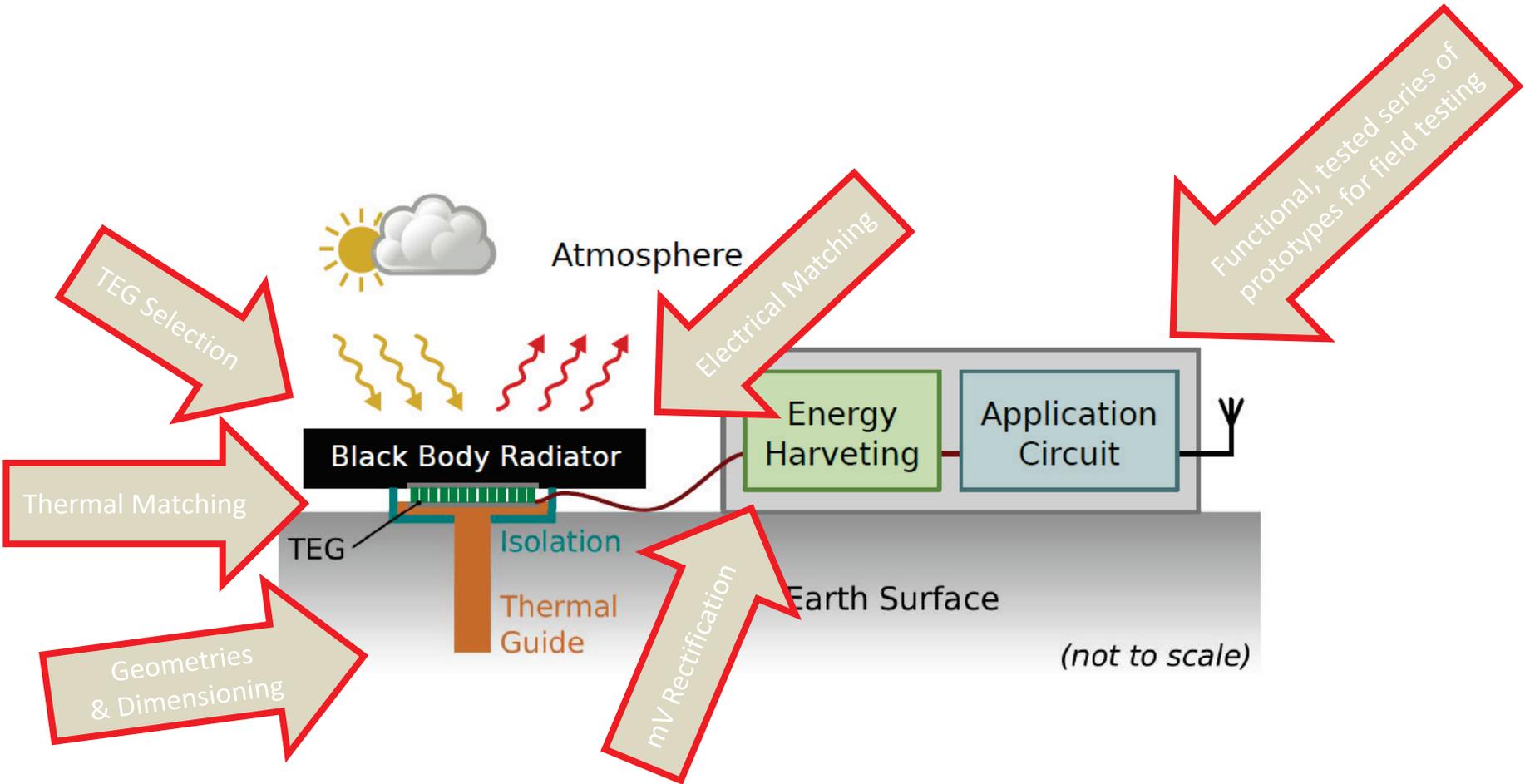
- Thermal guide
- Radiator
- TEG
- Rectifier
- Boost converter



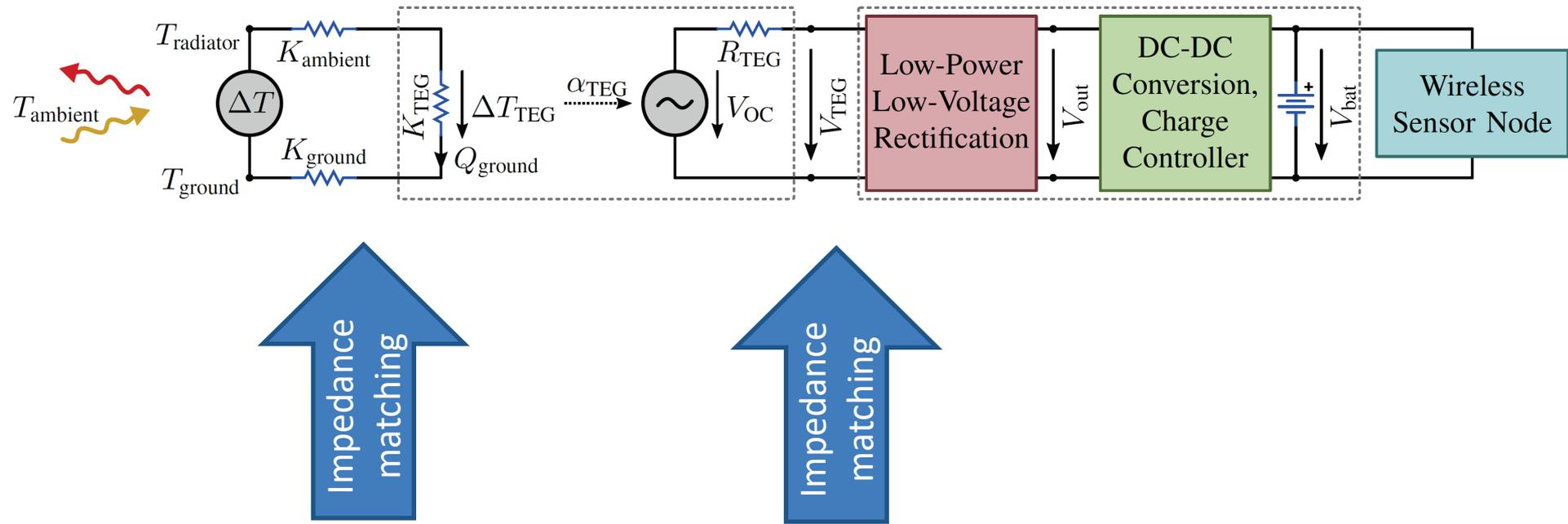
# System Design



# System Design Challenges



# System Overview



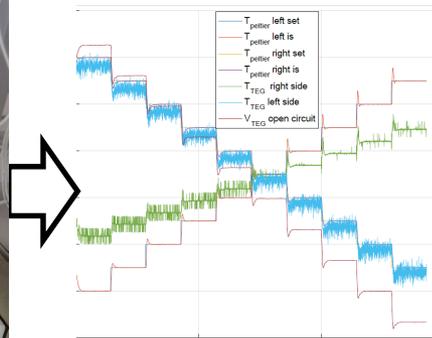
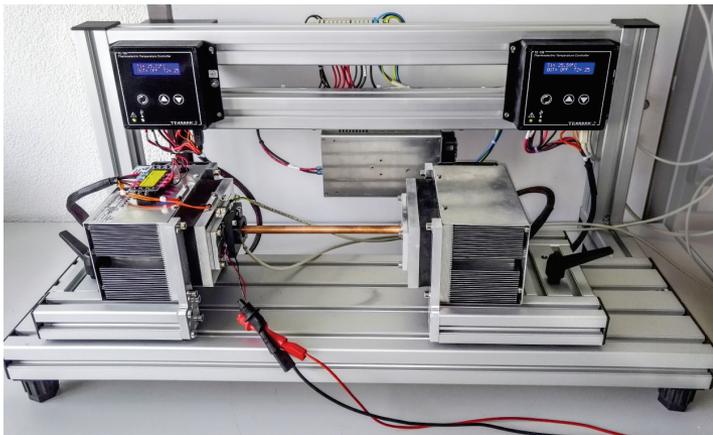
# Thermal Characterization: Testbed



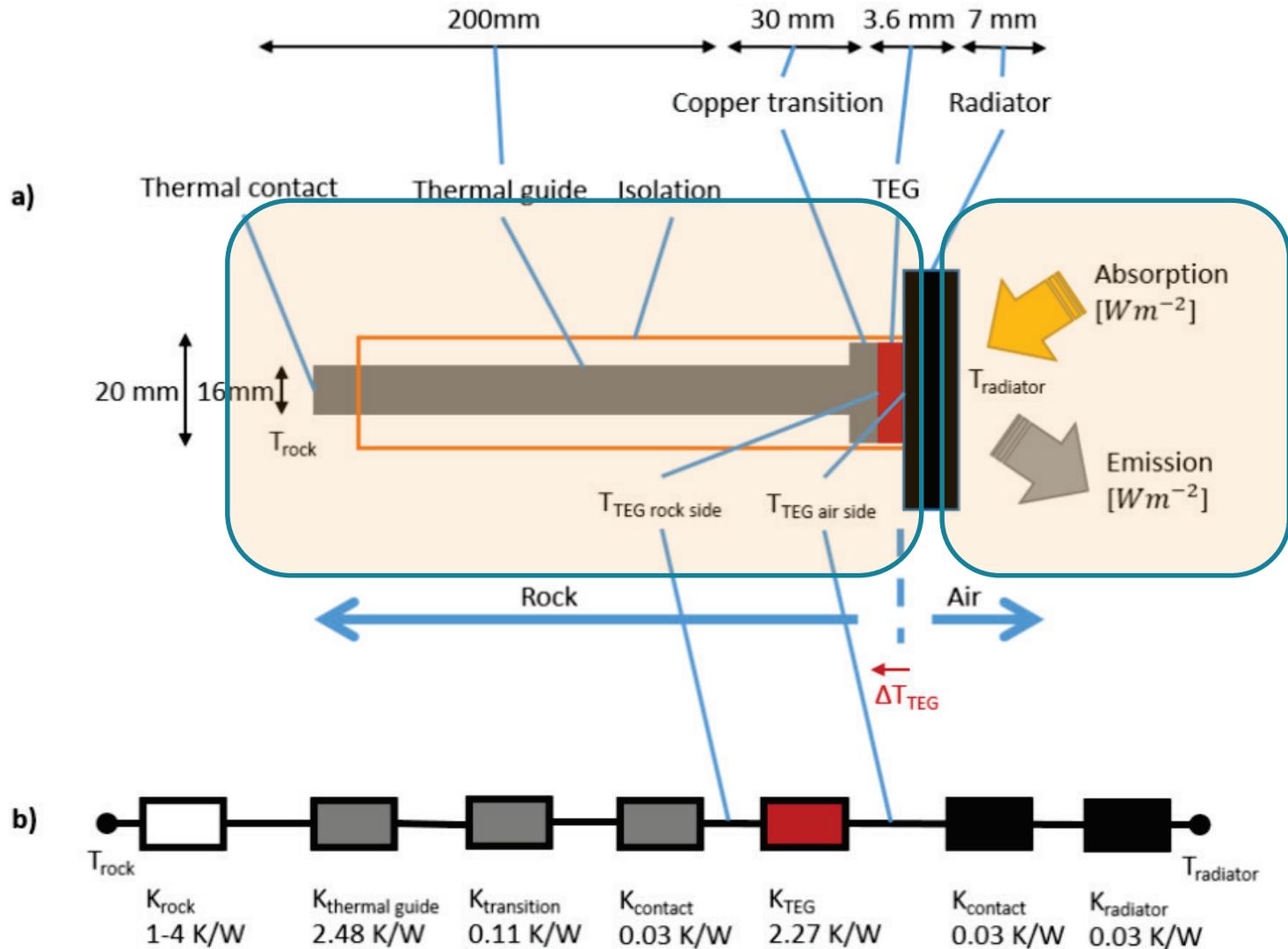
Two sided temperature control

- Temperature characteristics
- System response

Temperature vs radiation

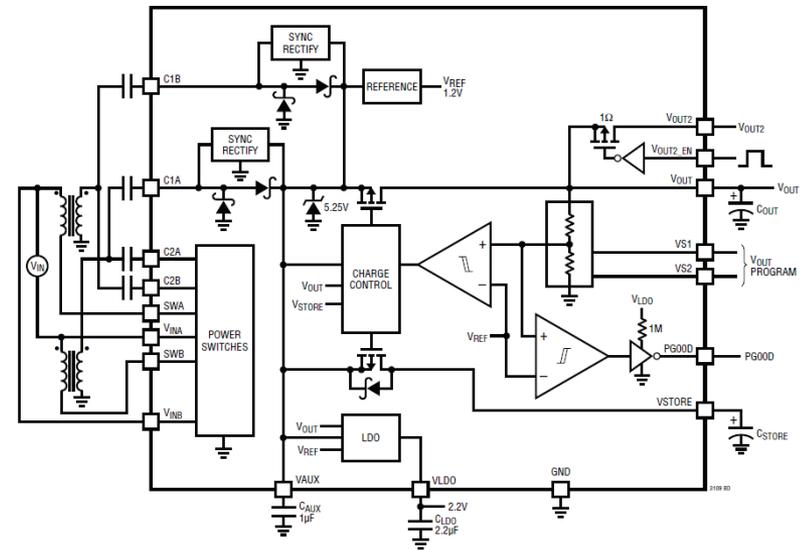


# Thermal Modelling



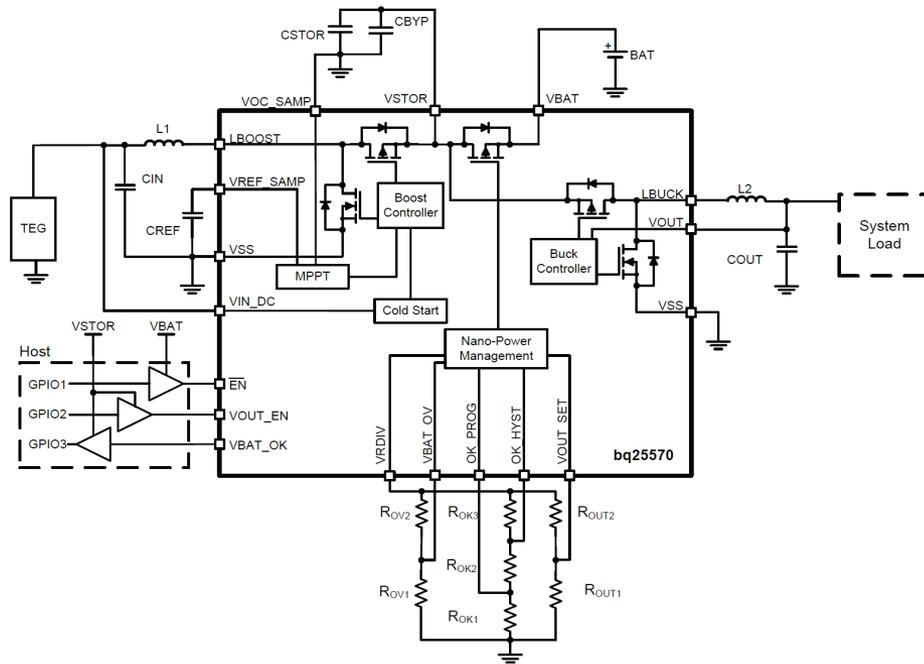
# Harvesting Charge Controller Options

	TI BQM255xx	Analog LTC3109
Regulator design	MPPT	Sync. Regulator
Input polarity	Unipolar	Bipolar
Min. harvesting voltage	100 mV	30 mV
Efficiency	0.6	0.3
Output	Unregulated	Regulated
Storage management	Yes	Partly
Power good output	Yes	Yes

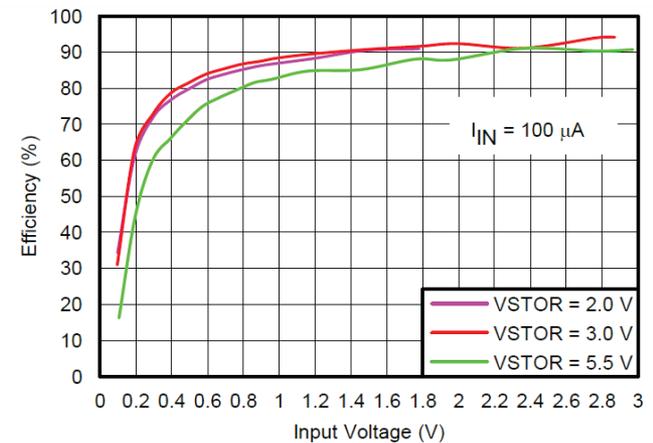


LTC 3109 Block Diagram

# BQ25570 MPPT Charge Controller



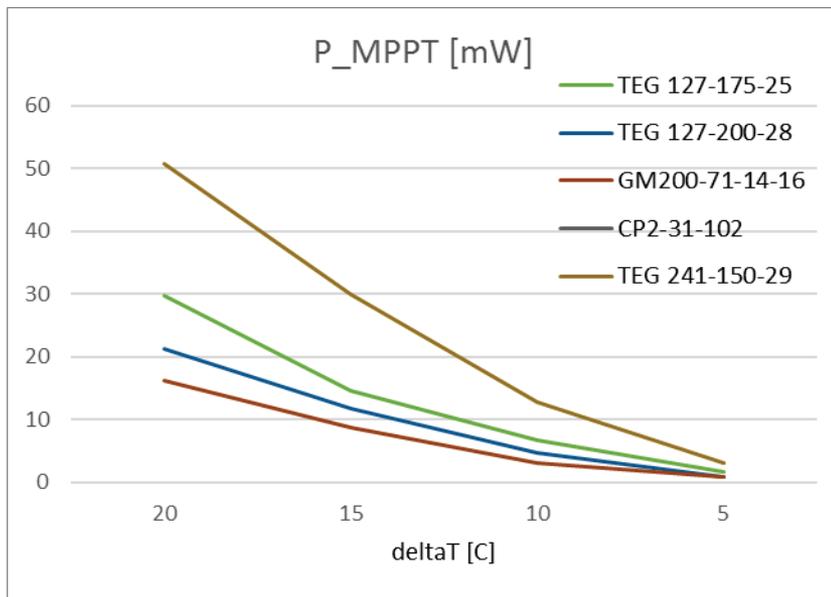
## Charger Efficiency vs Input Voltage



# Auxiliary Slides: BQ25570 vs LTC3109

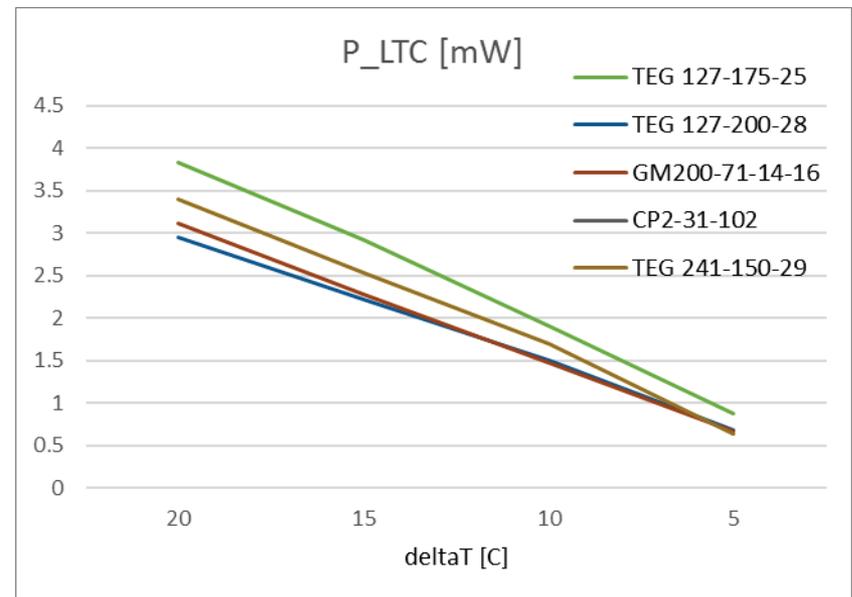
- BQ25570

- MPPT
- Buck converter



- LTC3109

- fixed input impedance
- low-dropout regulator

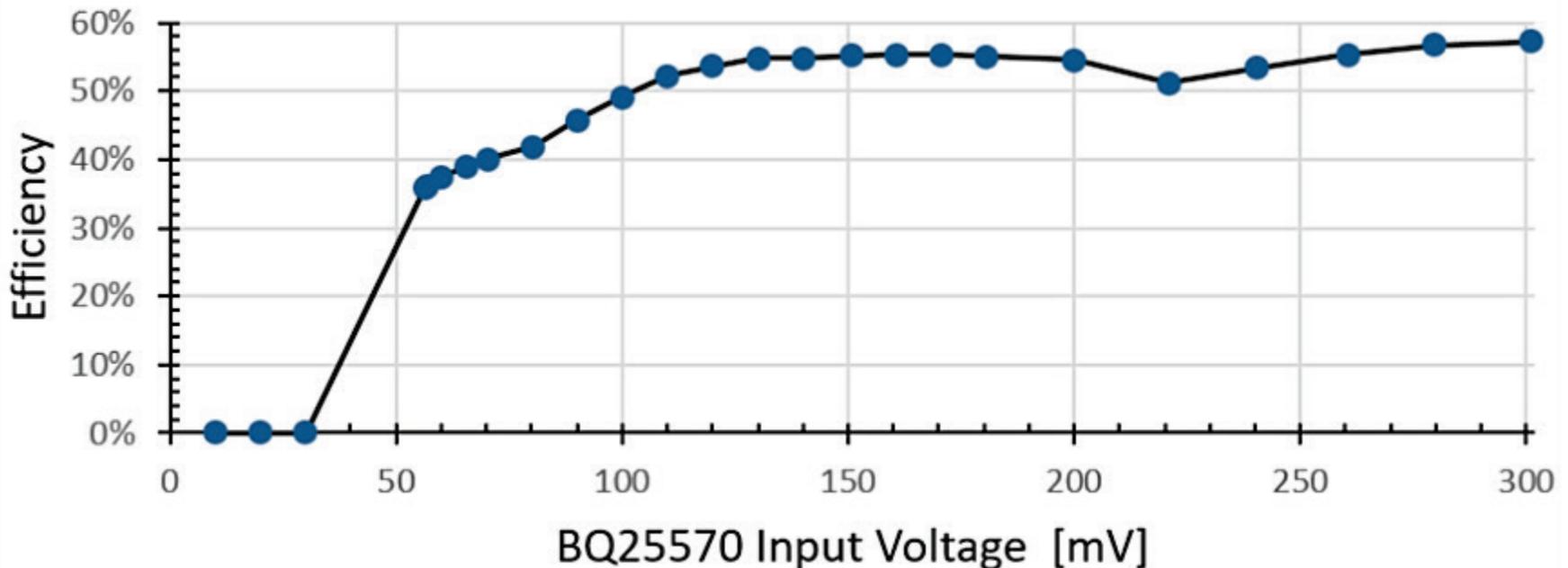


# Boosting Milivolts to Volts

- TEG: -300 - 300mV
- Storage: 3.6 - 4.2V
- Boost converter: BQ25570 + rectifier
  - Maximum Power Point Tracking (MPPT)



Measurement

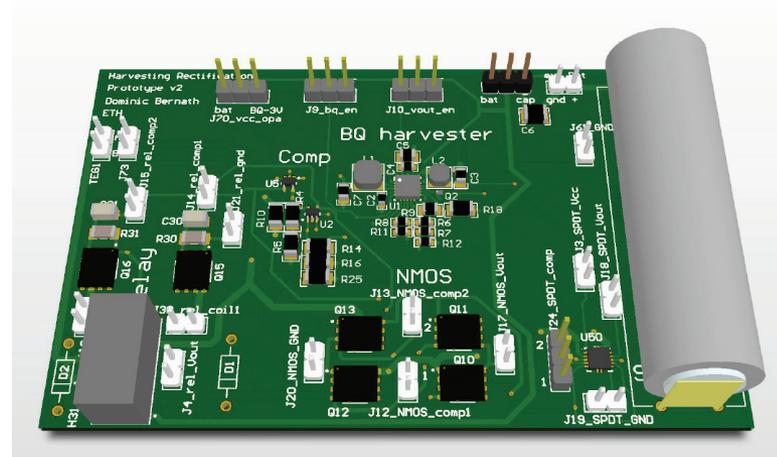


# Rectification of TEG Input

Type	Resistance	Quiescent power	Disadvantage
<i>Passive</i>			
Schottky diode		-	> 70mV forward voltage
<i>Active</i>			
Latching relay	0.2 $\Omega$	23 nW	mechanical sensitivity
SPDT	0.7 $\Omega$	10 nW	high resistance
Mosfet	0.2 $\Omega$	-	not break before make

## Gate driver

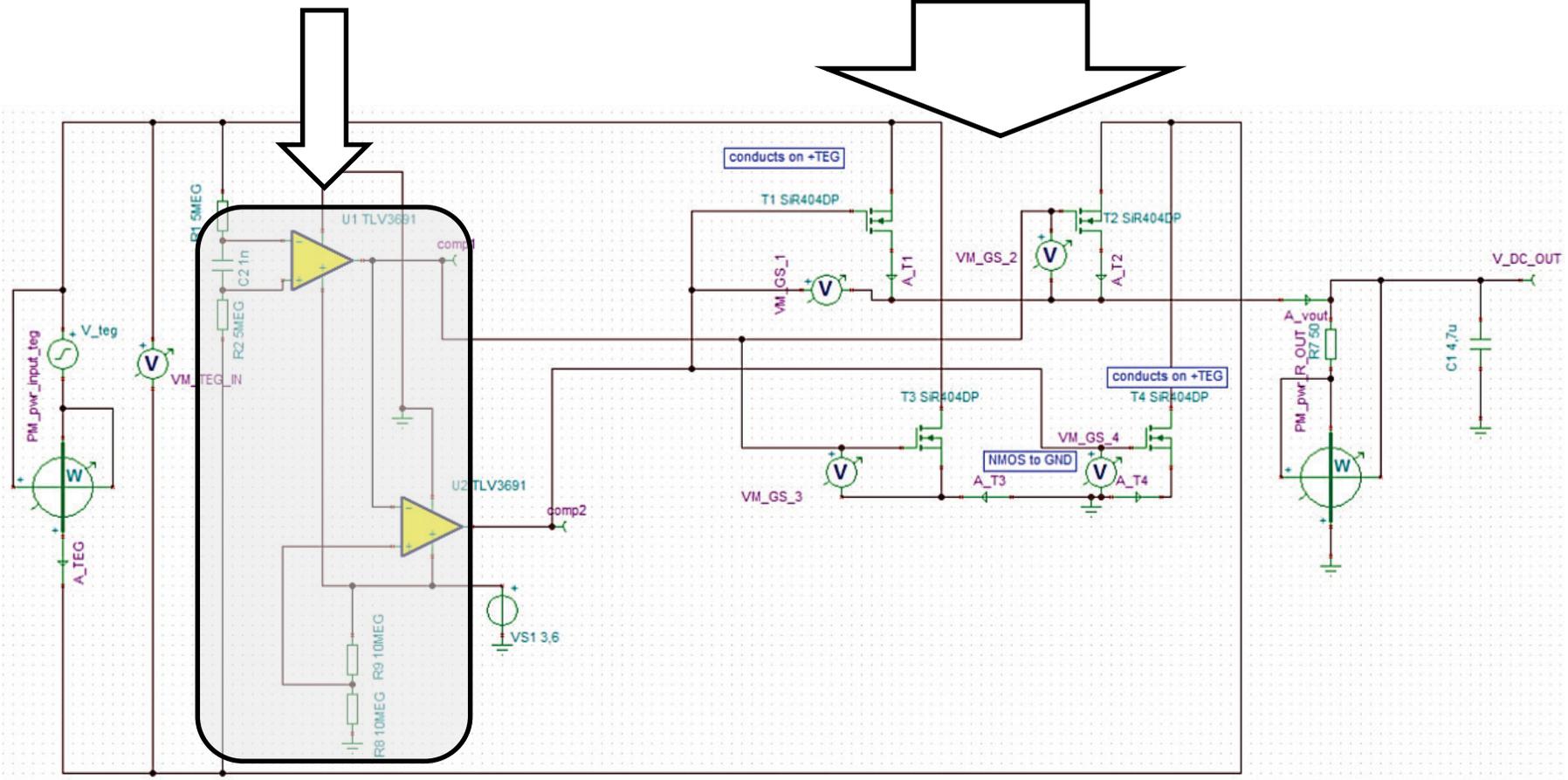
- Two comparators
- 0.5  $\mu$ W quiescent power



# SPICE Simulation of NMOS H-Bridge Rectifier

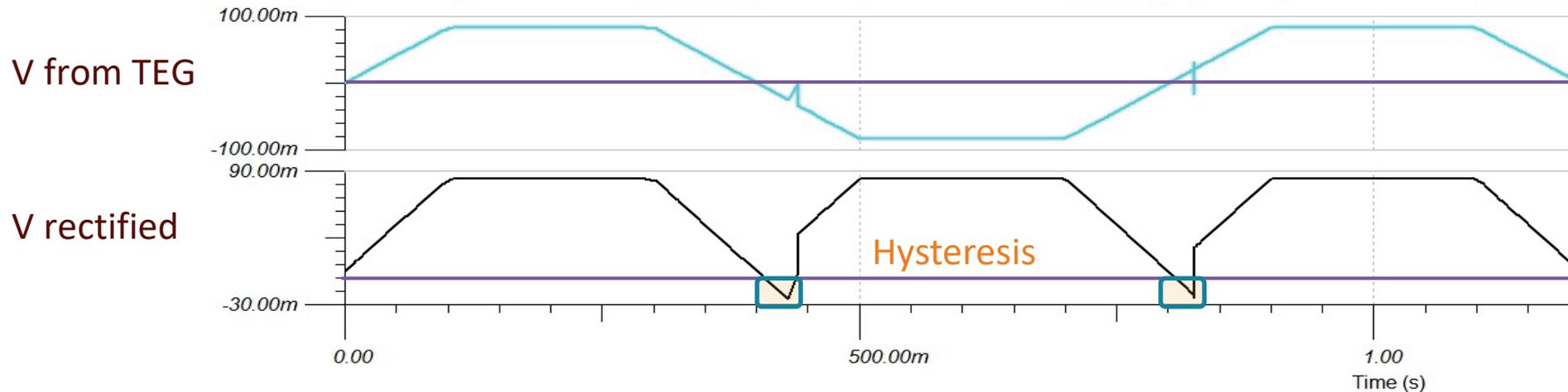
Comparator Gate Drivers

H-Bridge

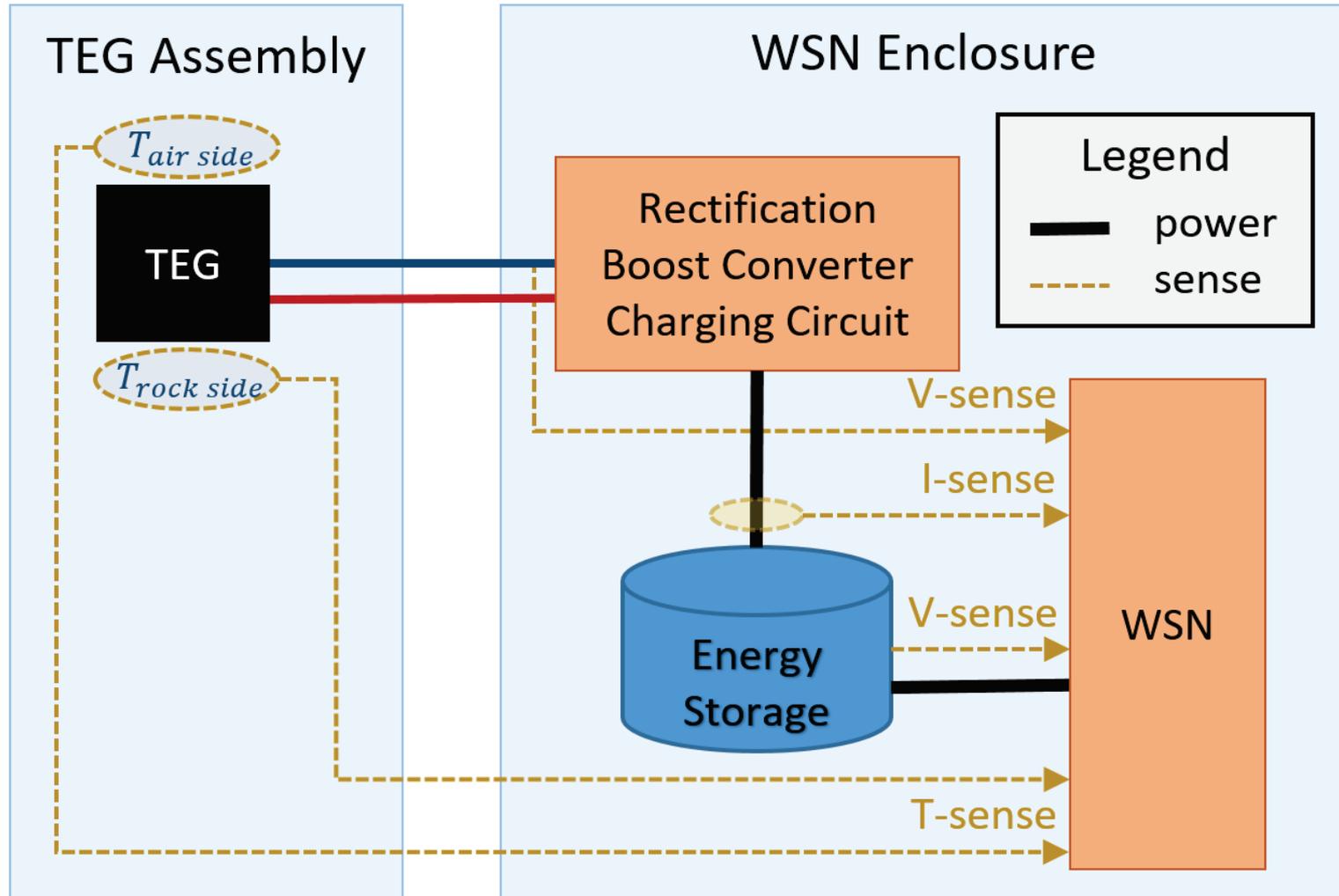


# SPICE Simulation of NMOS H-Bridge Rectifier

Break before make not guaranteed



# Electrical Overview





# Field Test – Different Thermal Guides

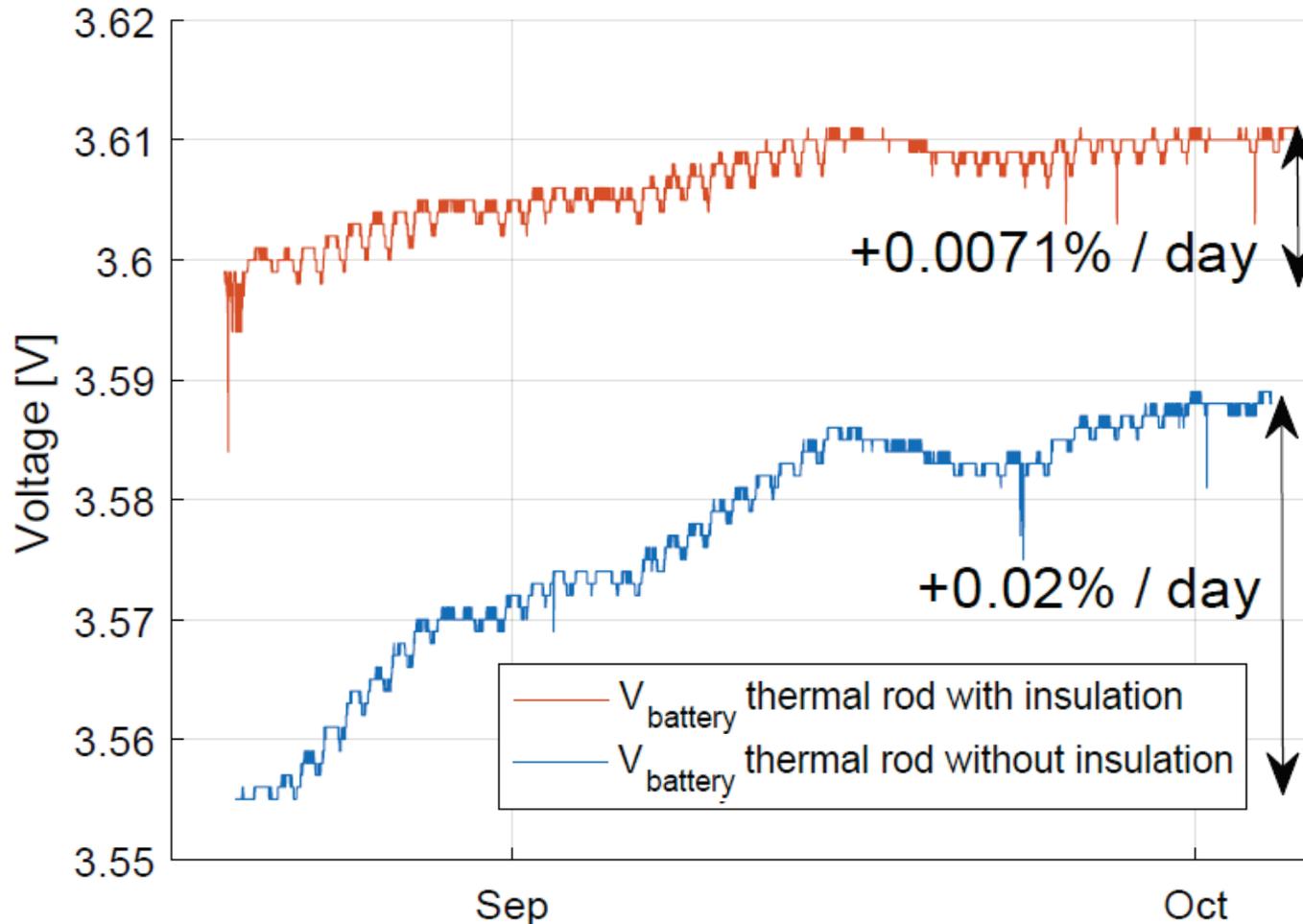


YES it works!

0.8mW average  
power margin: 61%

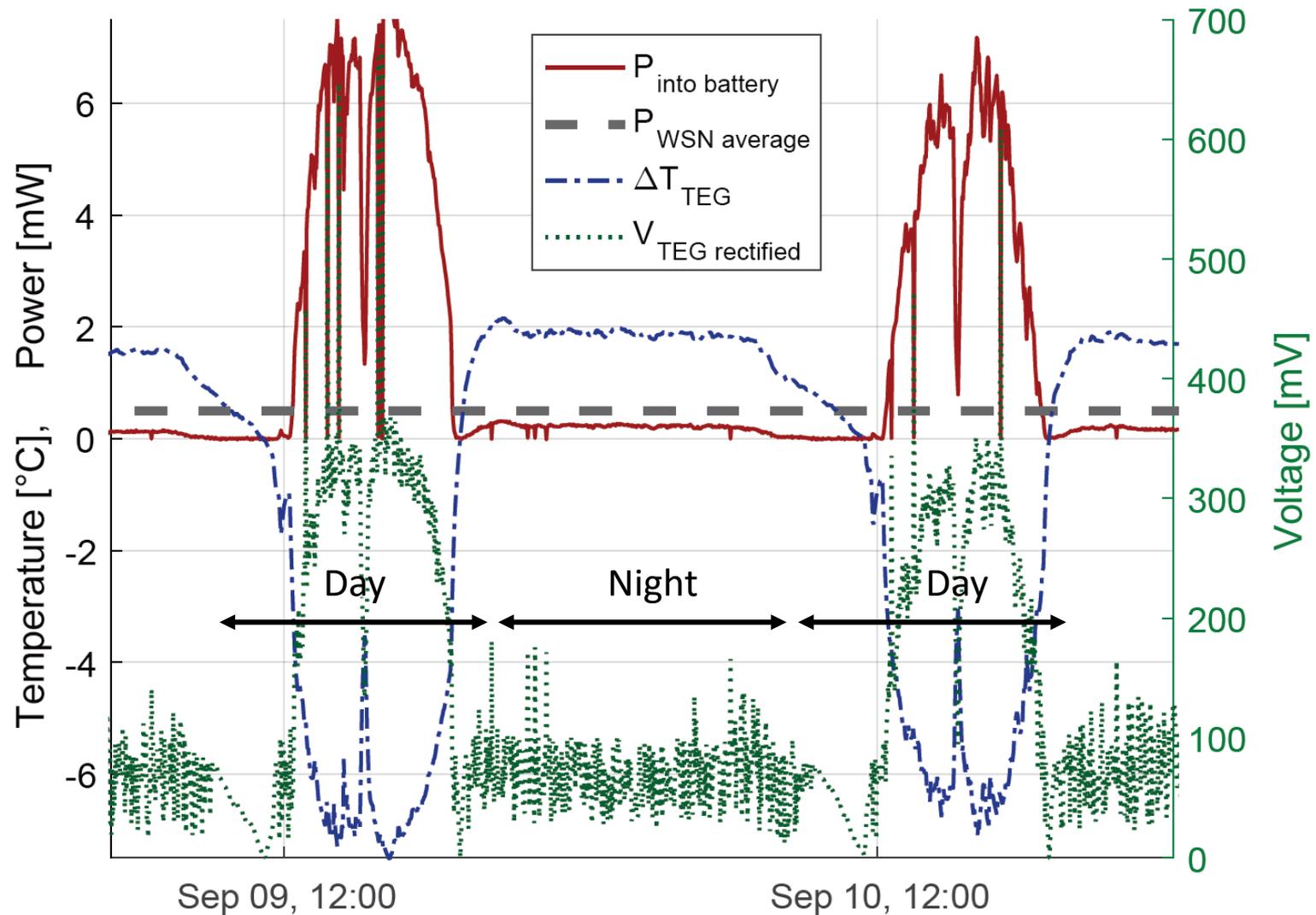
43 days of testing

# Long Term Energy Budget



2.8 times more surplus energy without insulation

# Diurnal Power Generation

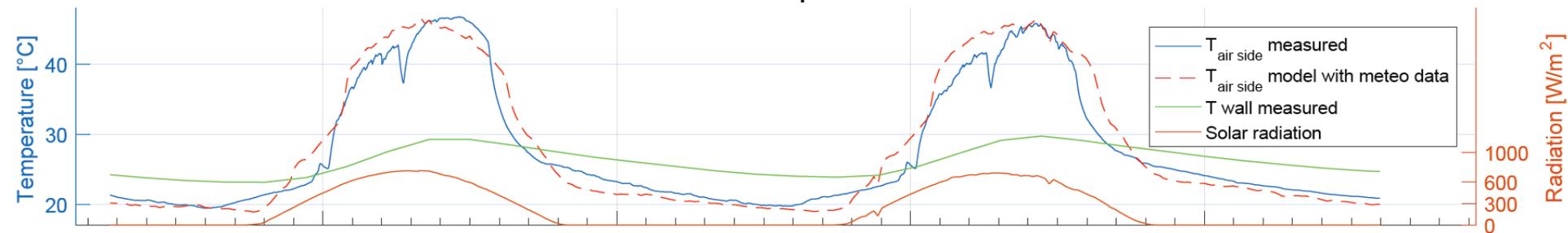


0.8mW mean power

# Model Validation

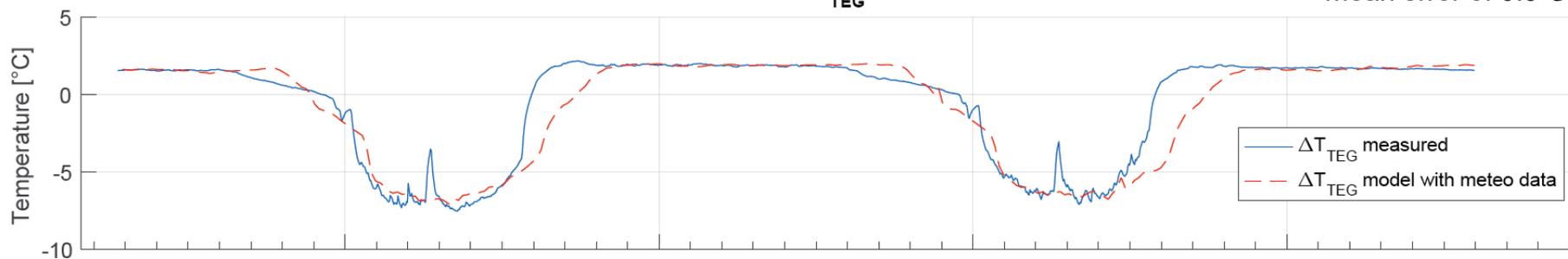
## Radiator Temperature

mean error of 5.7°C



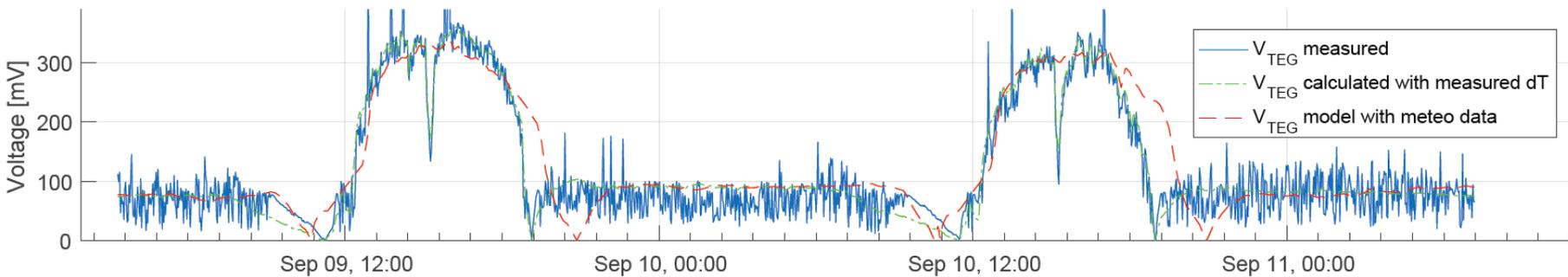
## $\Delta T_{\text{TEG}}$

mean error of 0.9°C



## $V_{\text{TEG}}$

mean error of 42 mV



# Jungfraujoch Field Test – South



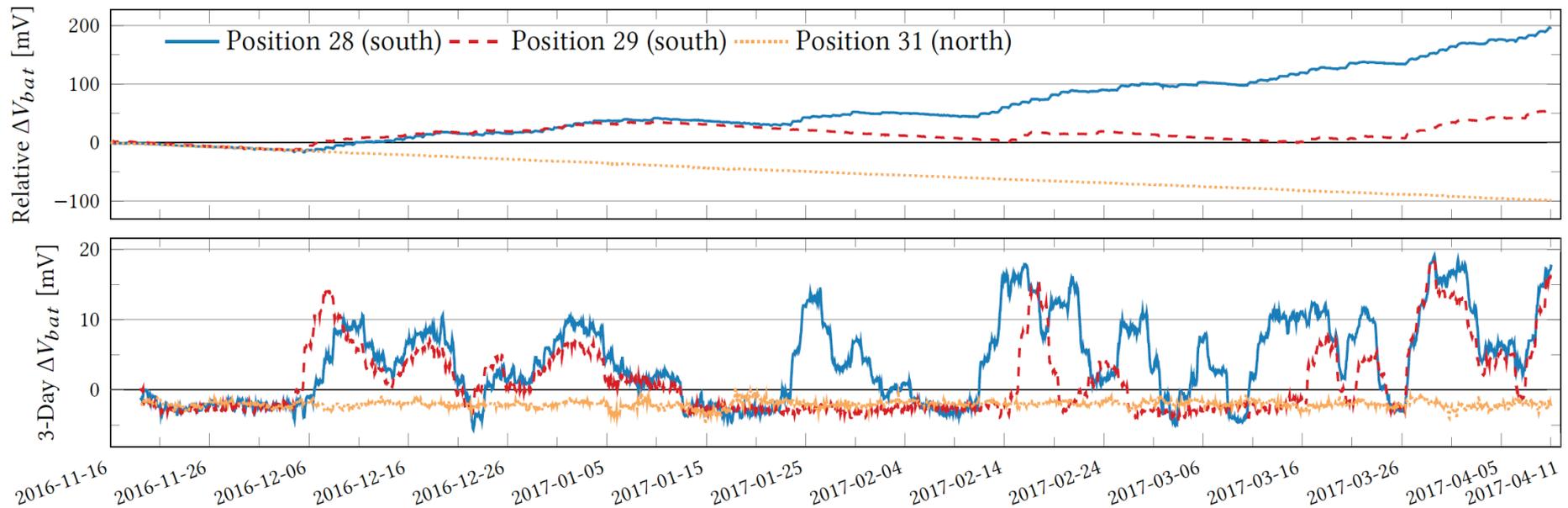
# Jungfrauoch Field Test – North



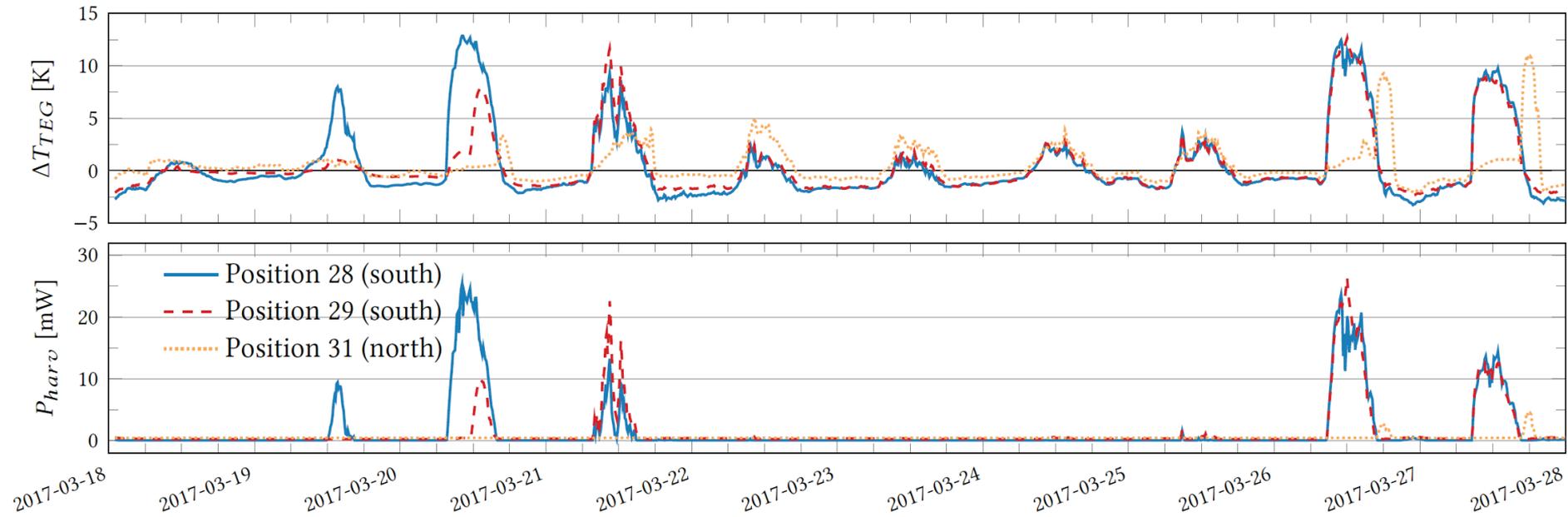
# Jungfrauoch Field Test – Partial Snow Cover



# Long-term Evolution: Steady Charging



# Short-term Differences on Meter-scale



# Performance of TEG Generator

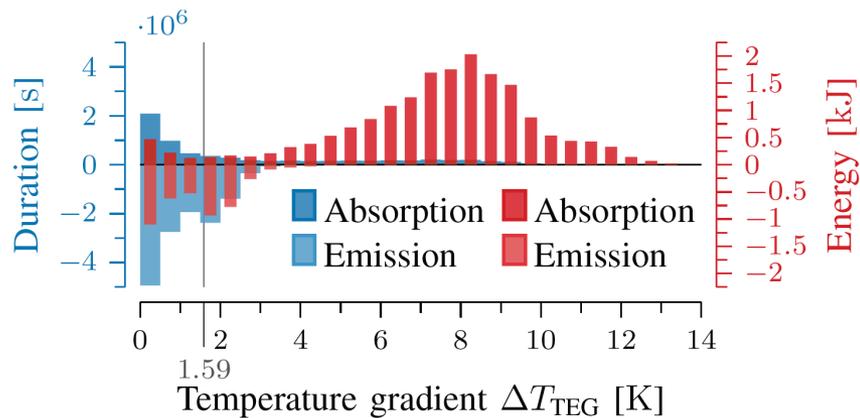


Figure 11. Histogram of temperature gradients and generated energy during 237 days, SE facing sensor node deployment.

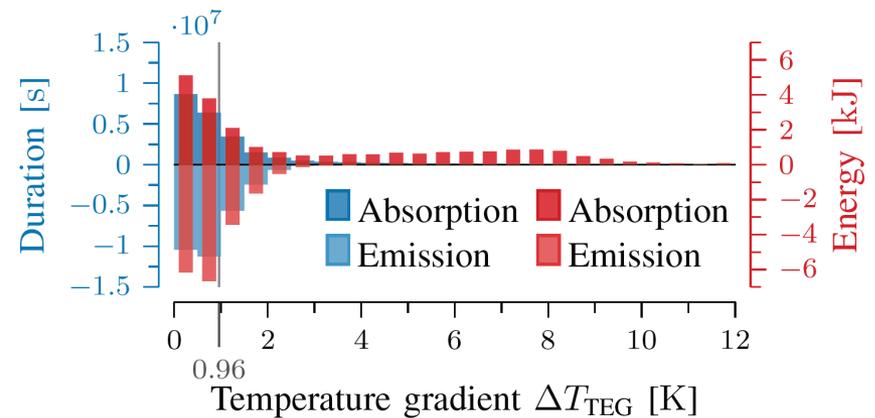


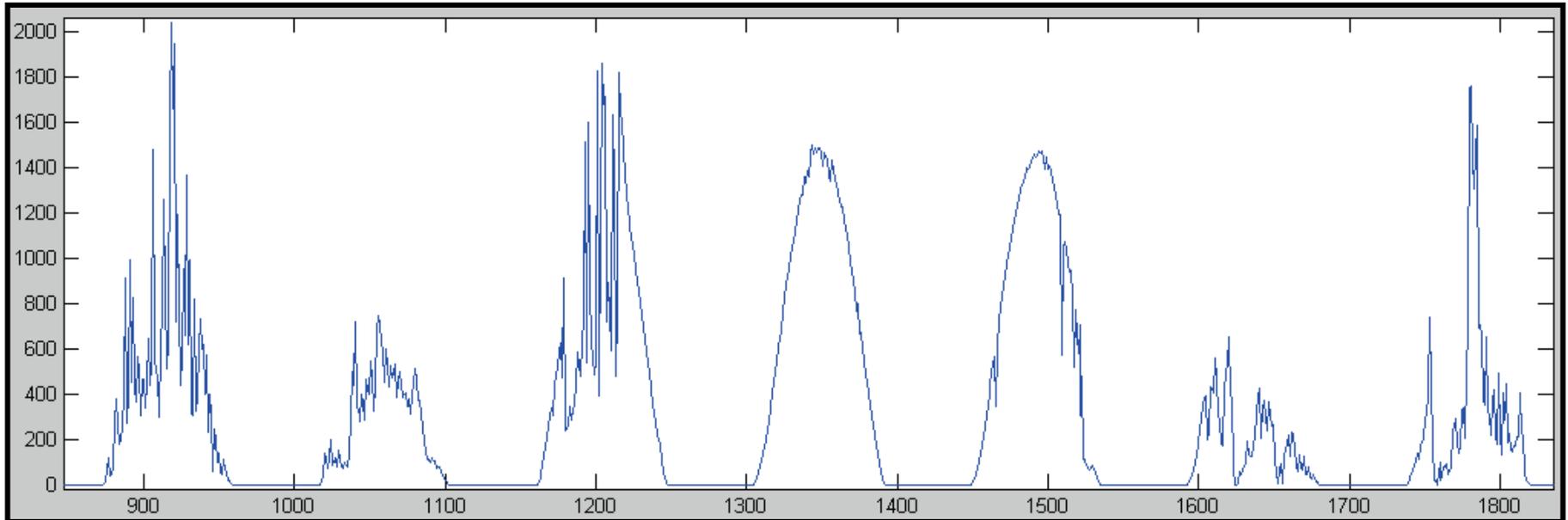
Figure 12. Histogram of temperature gradients and generated energy during 625 days, NW facing sensor node deployment.

Low-Power System Design

# **MODELING ENERGY USAGE – HARVESTING CONTROL**

# Harvesting Control: What is Different?

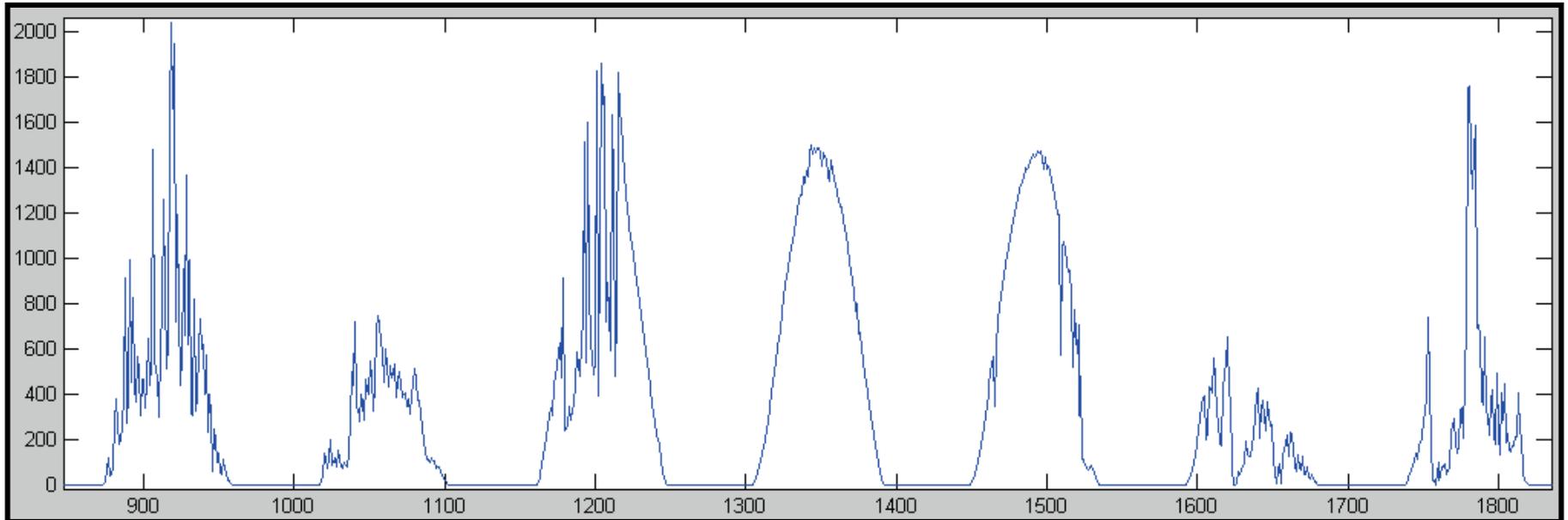
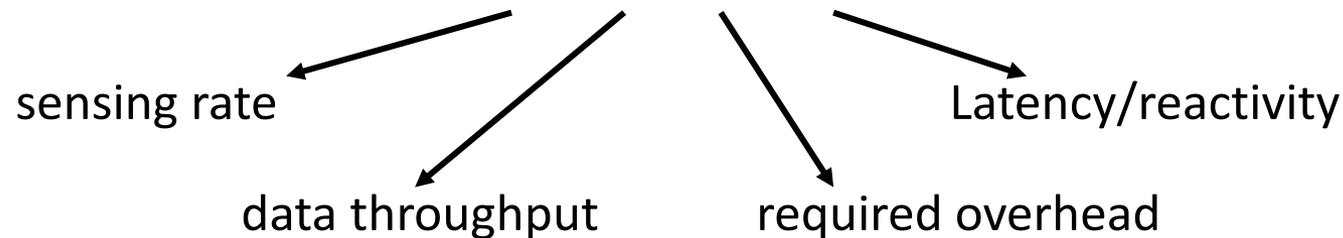
- Conventional energy management:
  - How do we **save** energy ?
- Energy harvesting:
  - When do we **use** energy ?



[Sunergy: June 2006]

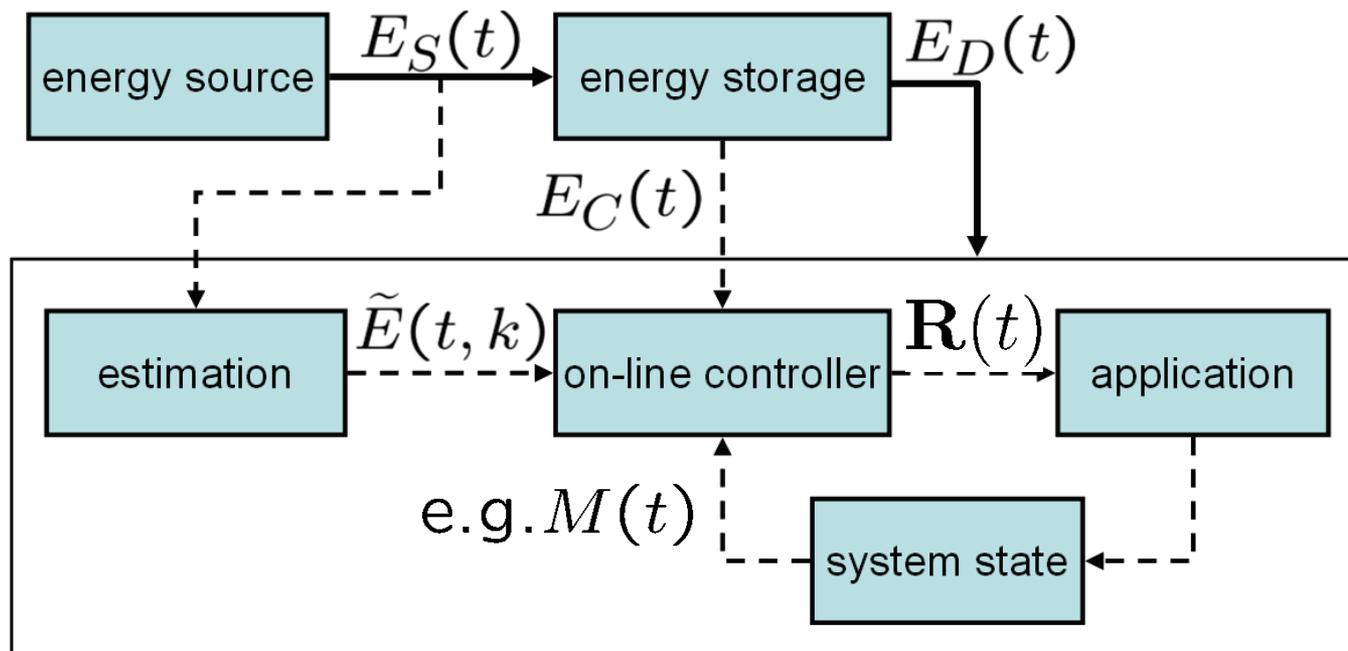
# Harvesting Control: Problem Definition

Determine **decisions on the application level** that optimize the long term system behavior



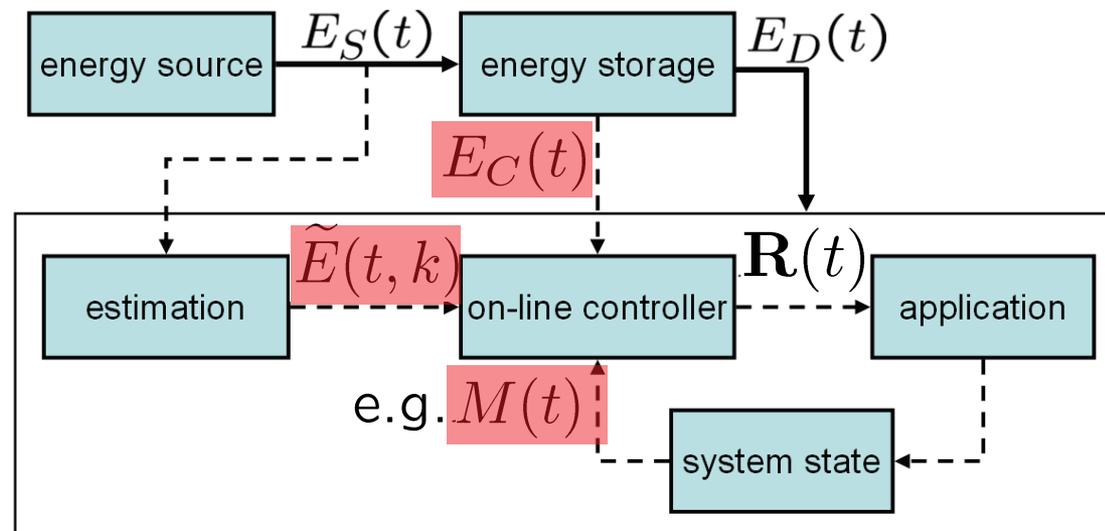
[Sunergy: June 2006]

# Harvesting Control: System Model



# Optimization: MP-Linear Programming

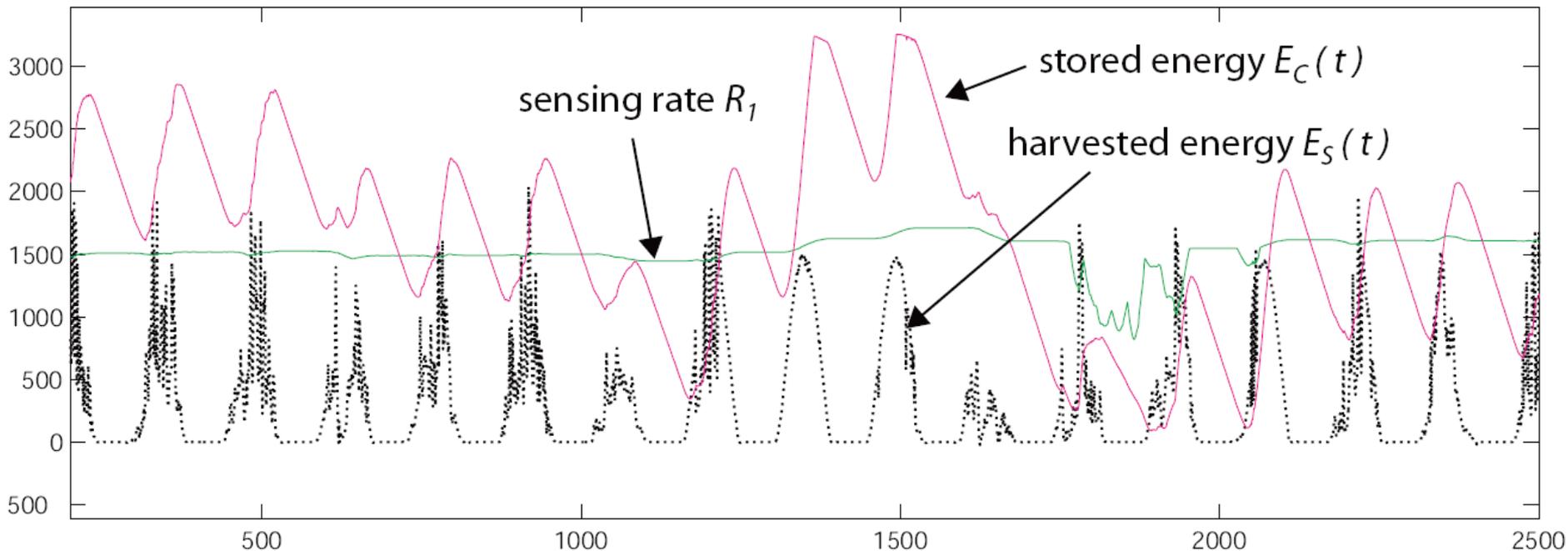
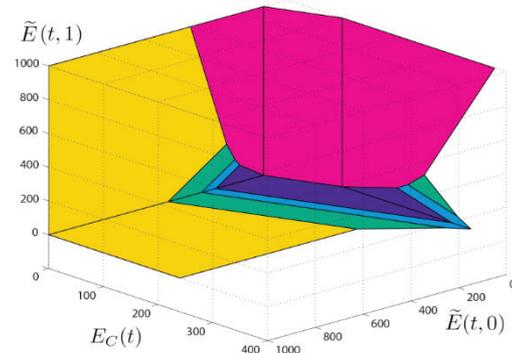
- Efficient run-time implementation by applying multiparametric linear programming
- Idea: Calculate optimal solution of the mp-LP as an explicit function of the state vector



# Simulation Results

- Adaptation of sensing rate depending on energy availability

$$\mathbf{H}_i \mathbf{X}(t) \leq \mathbf{K}_i, i = 1, \dots, N_{CR} = 7$$

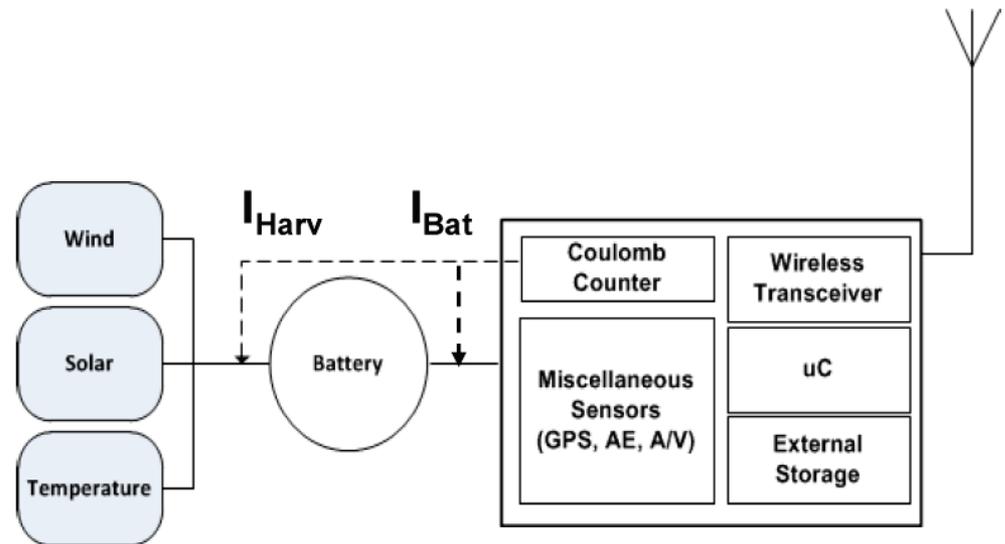


Low-Power System Design

# **MODELING BATTERY STATE OF CHARGE**

# Battery State-of Charge Approximation

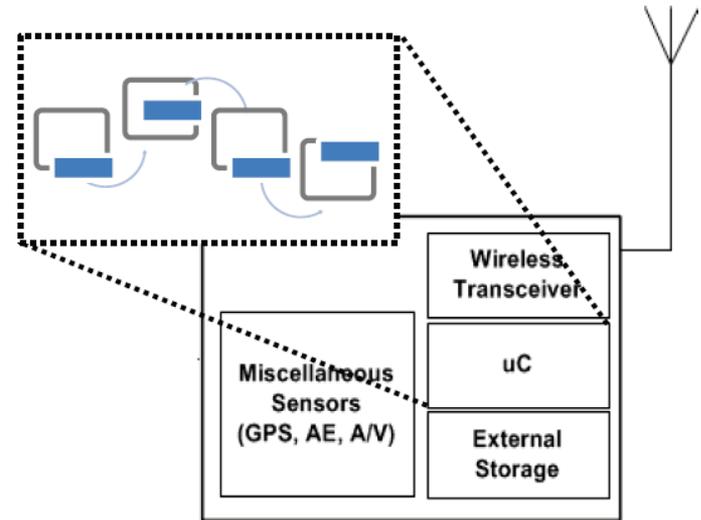
- Hardware
  - Coulomb counting



SOC Approach	Dedicated Hardware	Integration Effort	Account for Battery Inefficiencies
Pure HW	<b>Yes</b>	<b>High</b>	<b>No</b>
Pure SW			
Hybrid CC			
This work			

# Battery State-of Charge Approximation

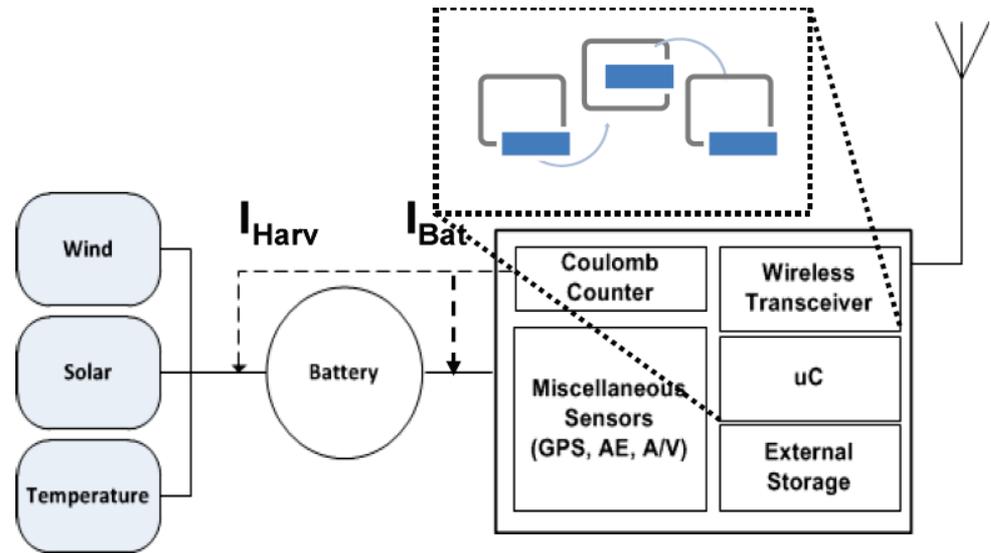
- Hardware
  - Coulomb counting
- Software
  - State monitoring, profiling



SOC Approach	Dedicated Hardware	Integration Effort	Account for Battery Inefficiencies
Pure HW	Yes	High	No
Pure SW	No	Low	No
Hybrid CC			
This work			

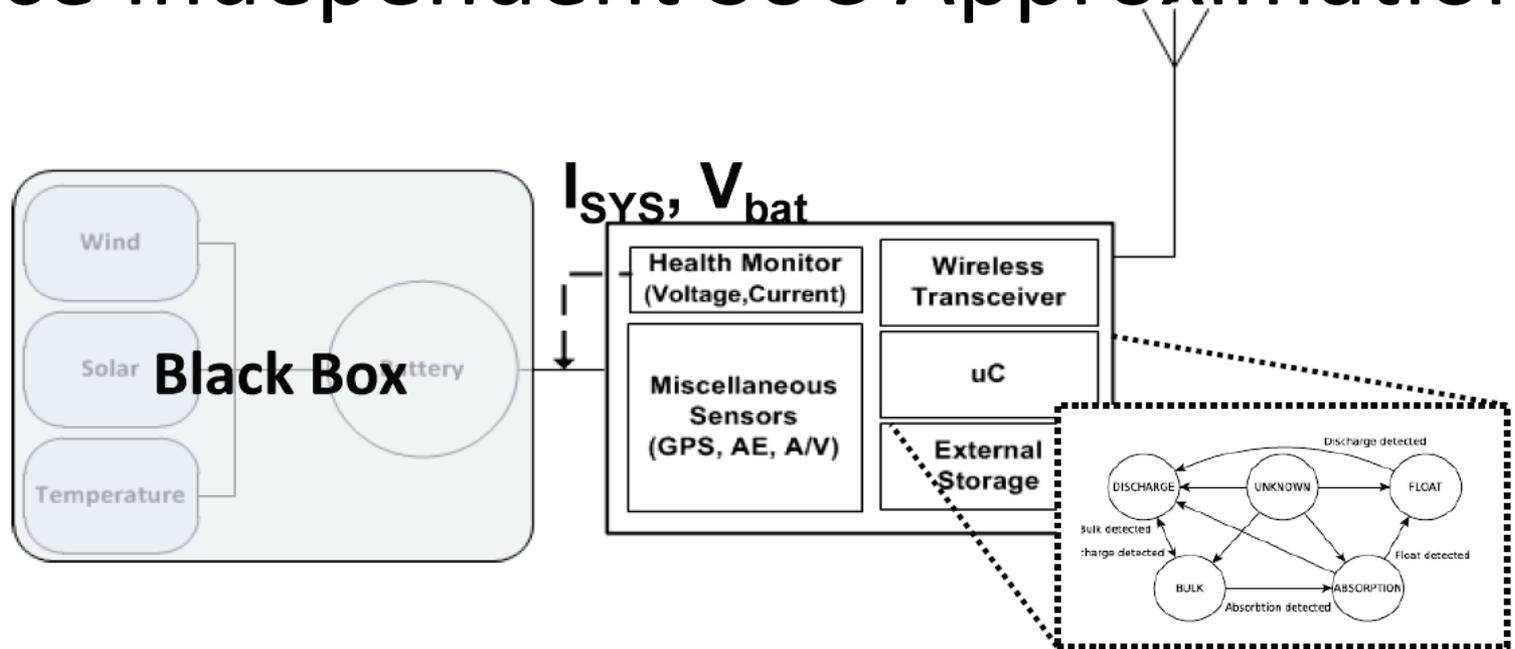
# Battery State-of Charge Approximation

- Pure HW
  - Coulomb counting
- Pure SW
  - State monitoring, profiling
- Hybrid HW/SW
  - Bookkeeping



SOC Approach	Dedicated Hardware	Integration Effort	Account for Battery Inefficiencies
Pure HW	Yes	High	No
Pure SW	No	Low	No
Hybrid CC	Yes	High	Yes
This work			

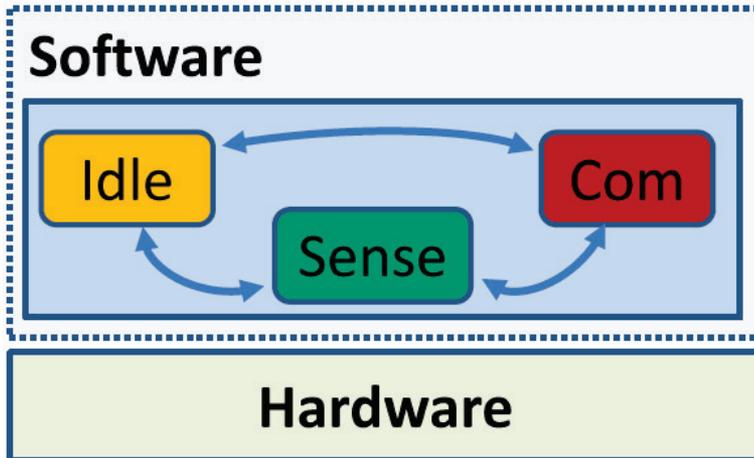
# Source Independent SoC Approximation



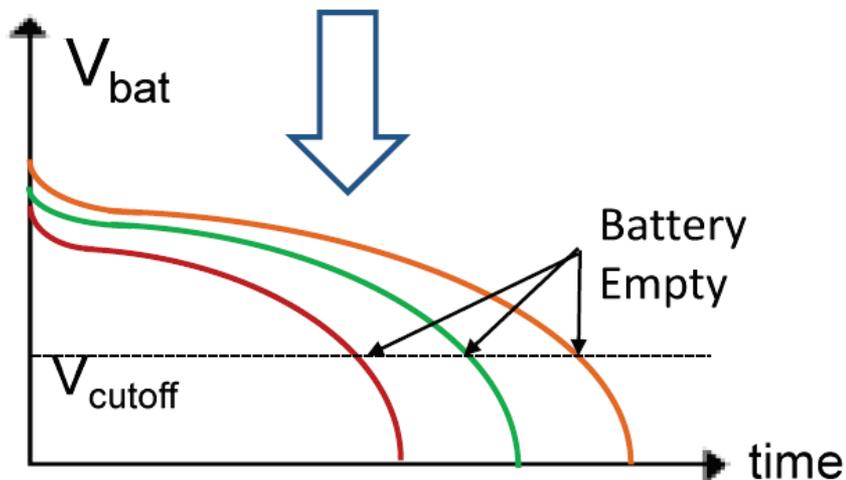
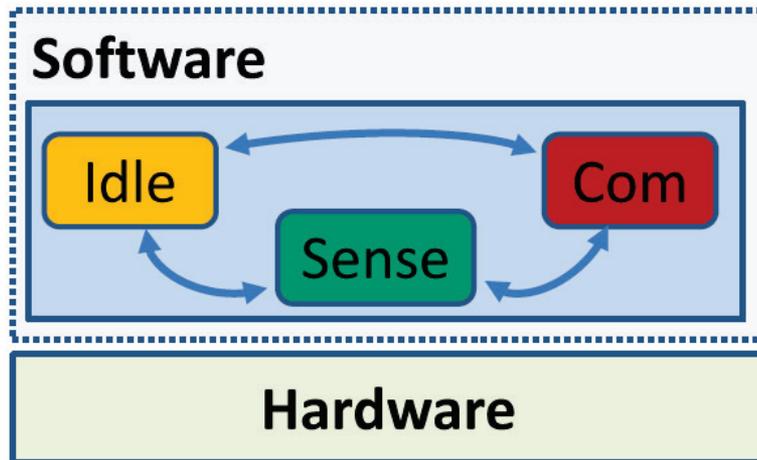
SOC Approach	Dedicated Hardware	Integration Effort	Account for Battery Inefficiencies
Pure HW	Yes	High	No
Pure SW	No	Low	No
Hybrid CC	Yes	High	Yes
This work	No	Low	Yes

[B. Buchli, D. Aschwanden and J. Beutel: Battery State-of-Charge Approximation for Energy Harvesting Embedded Systems. Lecture Notes on Computer Science. Proc. of 10th European Conference on Wireless Sensor Networks (EWSN 2013), p. 179-196, February 2013.]

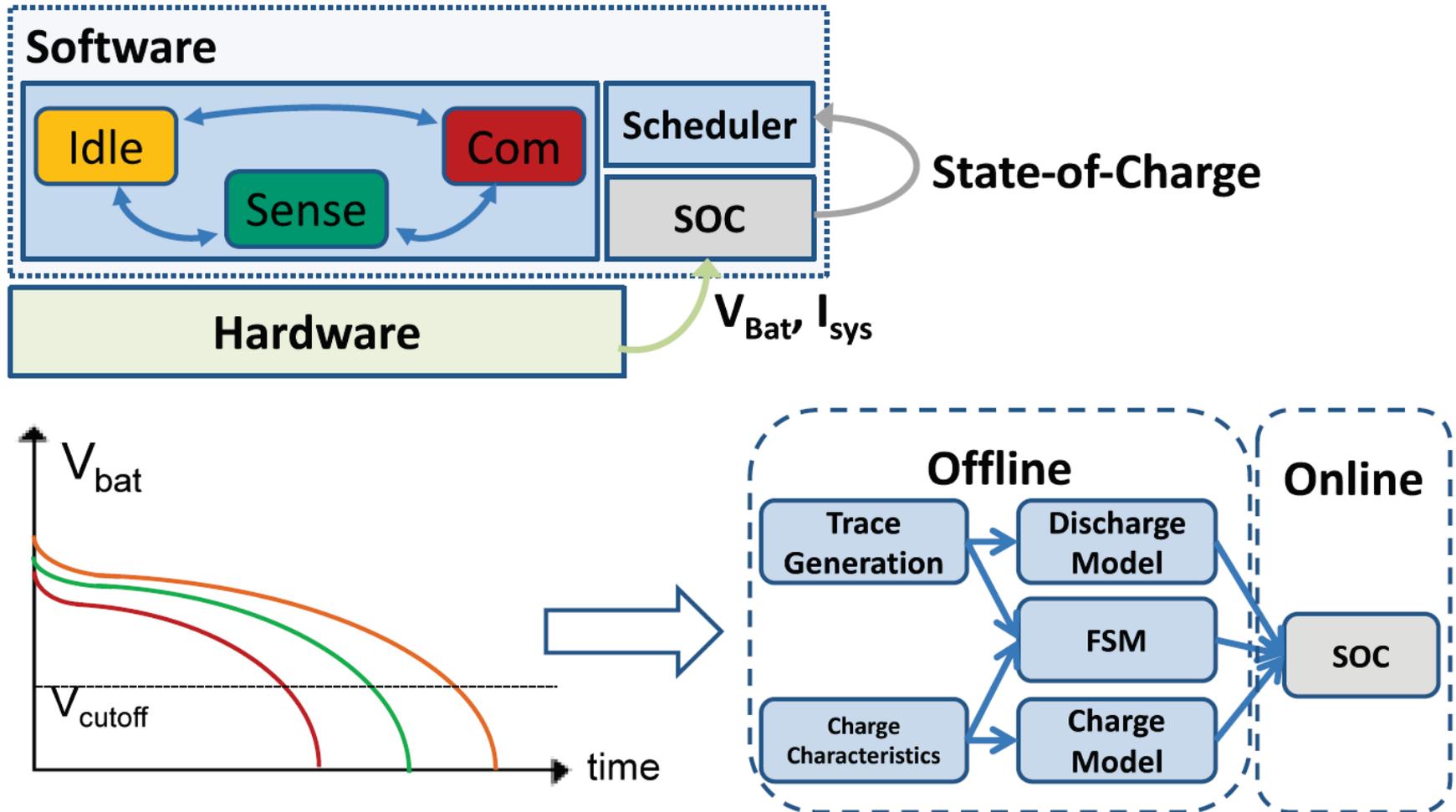
# Abstract System As State-Machine



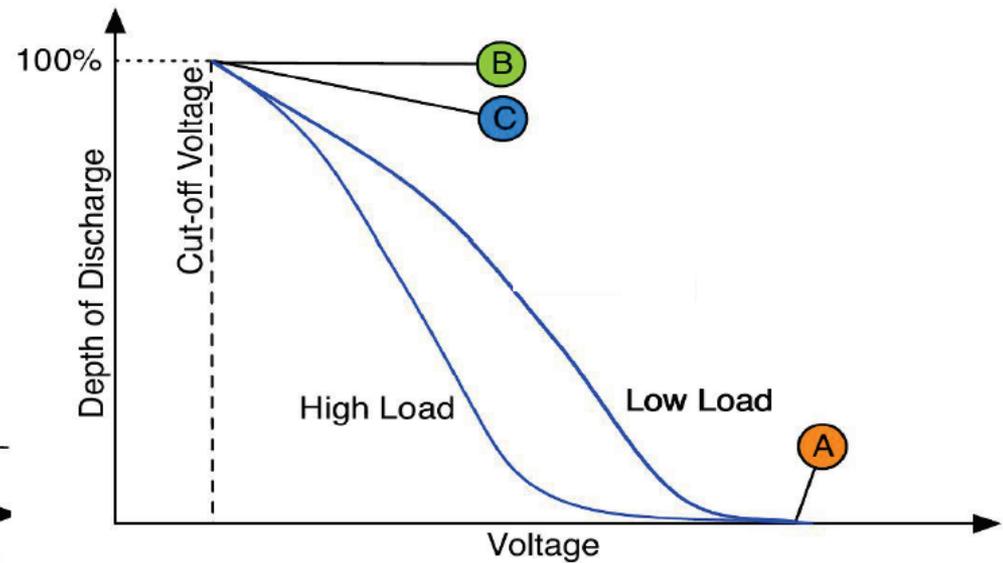
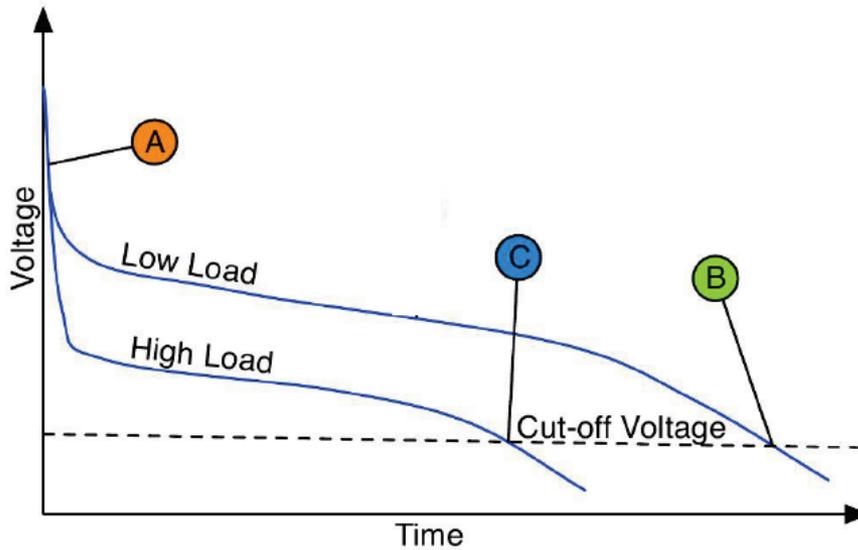
# States Exhibit Voltage Profile “Signature”



# Online State-of-Charge Information for Energy-Aware Scheduling

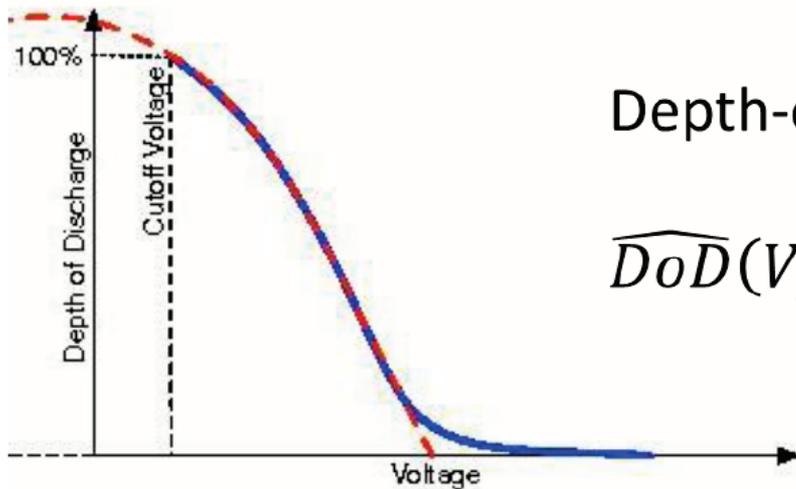


# Proposed Approach: Trace Generation and Transformation

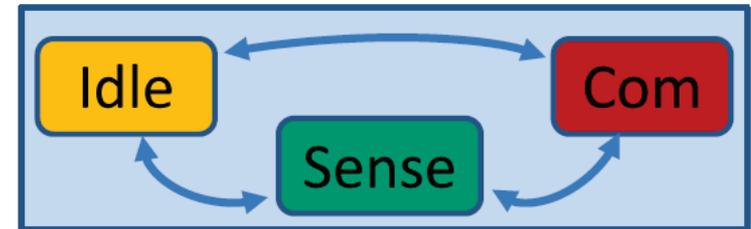
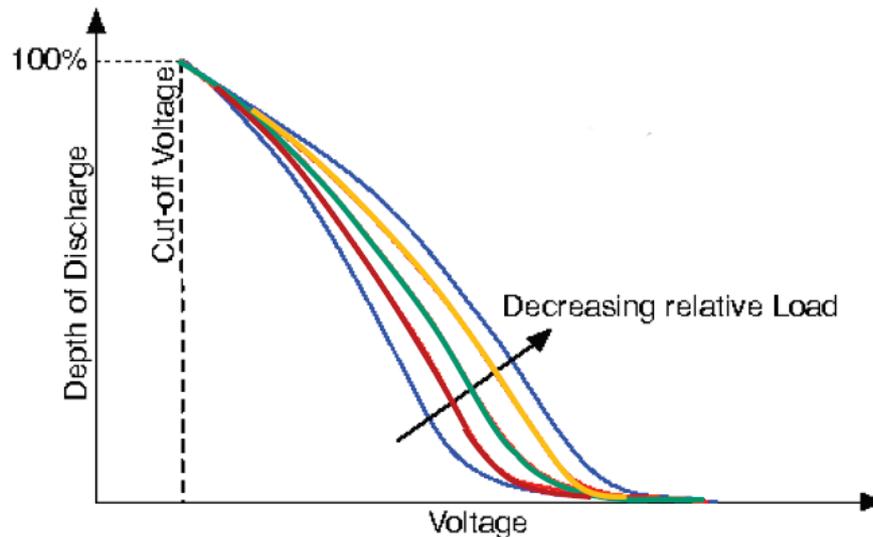


Depth-of-Discharge =  $DOD = 1 - SOC$

$$\widehat{DoD}(V_{bat}) = a_2 * V_{bat}^2 + a_1 * V_{bat} + a_0$$



# Proposed Approach: Discharge Model

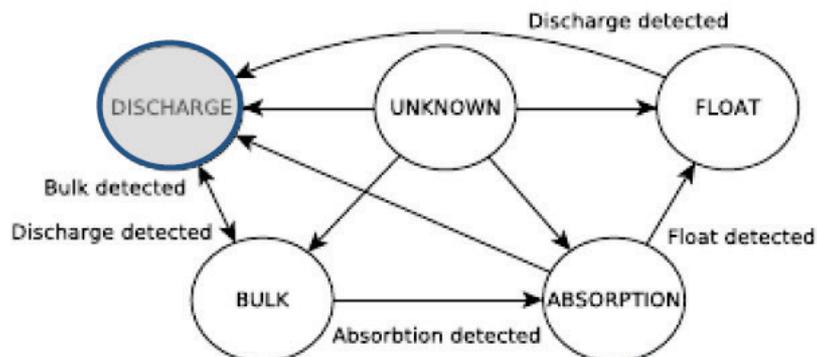
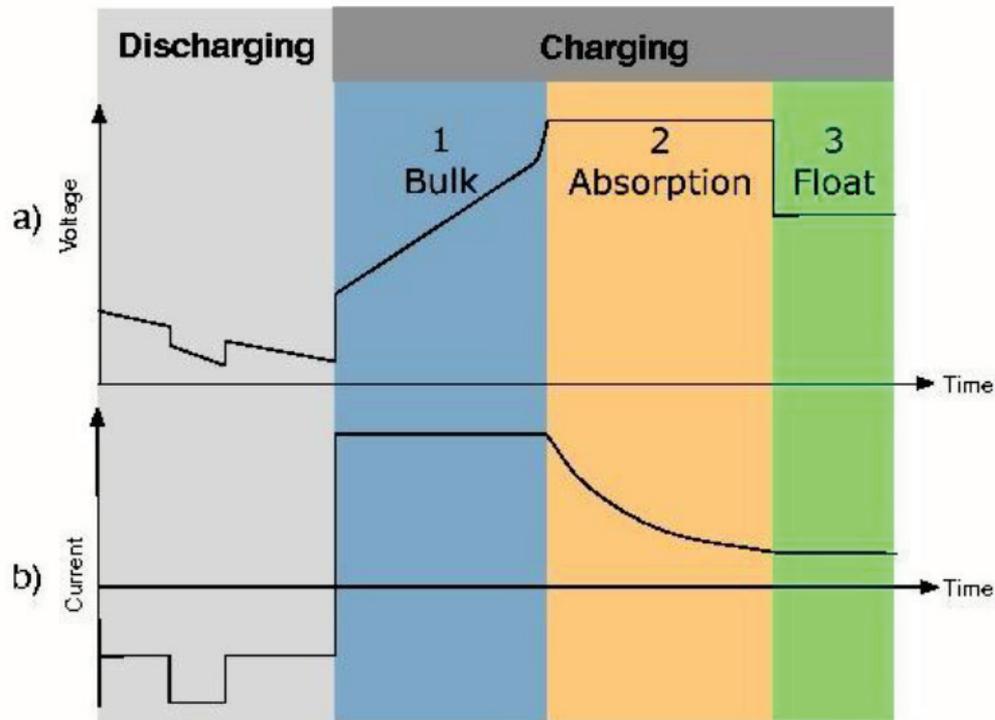


$$\text{Relative Load} = RL = \frac{\text{Drain Current}}{\text{Nom. Bat. Cap.}}$$

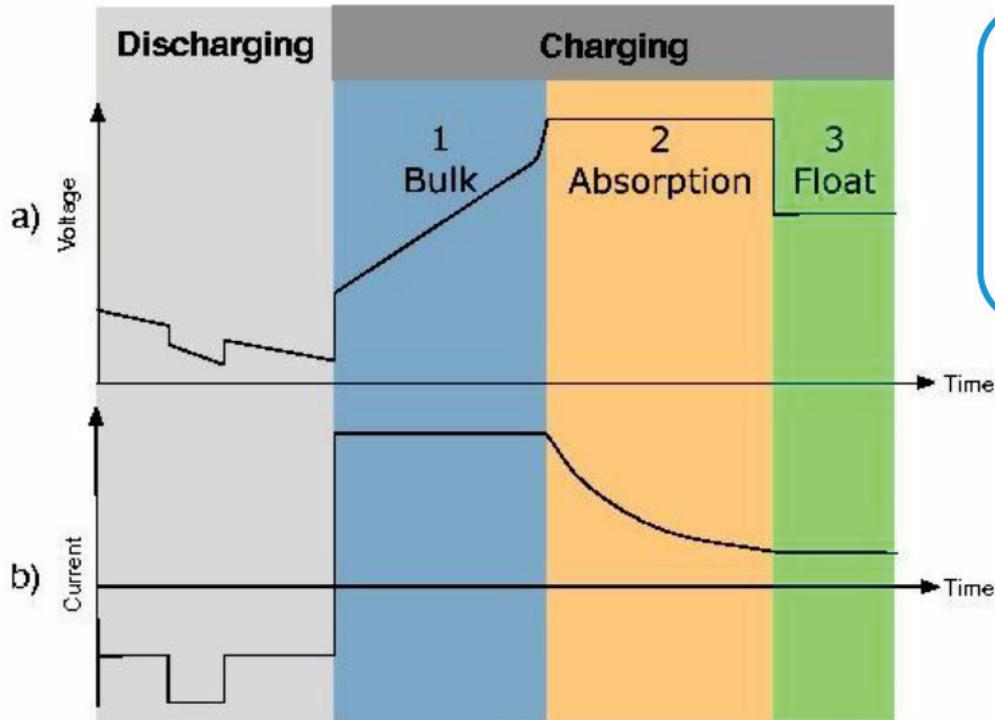
$$\widehat{\text{DoD}}(V_{bat}, RL) = a_2(RL) * V_{bat}^2 + a_1(RL) * V_{bat} + a_0(RL)$$

$$a_n(RL) = b_{n,2} * RL^2 + b_{n,1} * RL + b_{n,0}, \text{ for } n = 0, 1, 2$$

# Proposed Approach: Charge Model



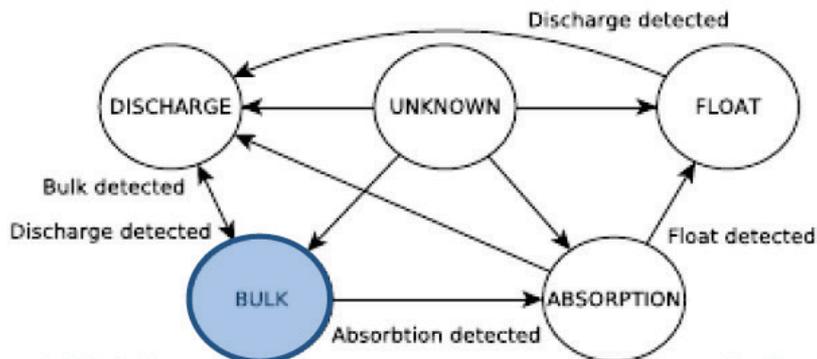
# Proposed Approach: Charge Model



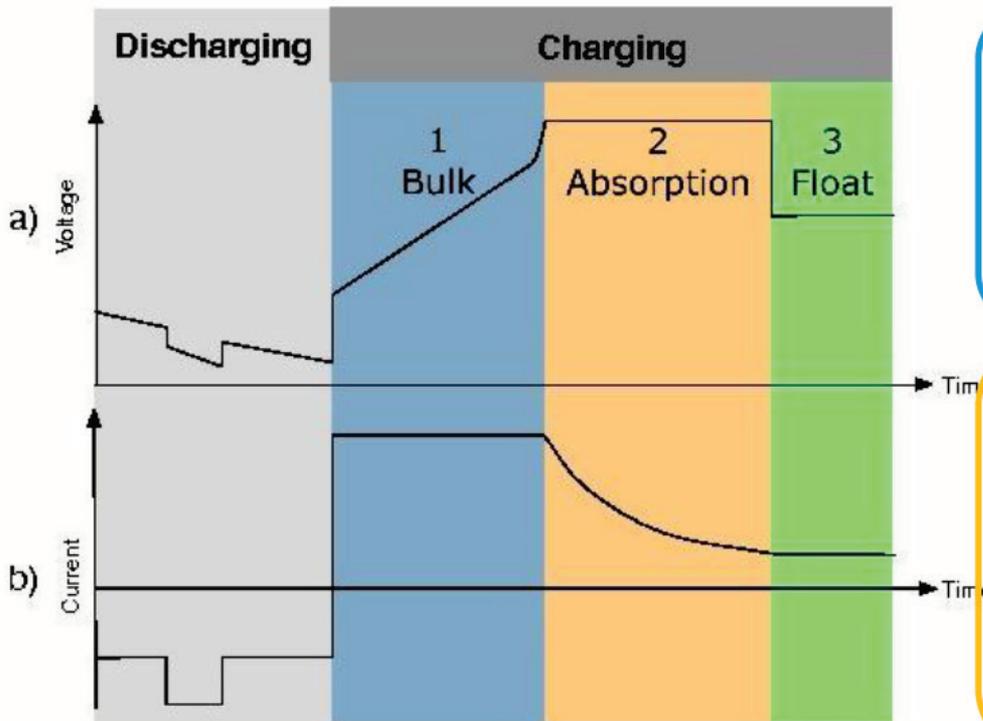
Bulk:

$$\widehat{RC}_{bulk} = c_1 * \frac{\delta V}{\delta t} + c_0$$

$$\widehat{SOC}(t) = \widehat{SOC}(t - t_{bulk}) + \widehat{RC}_{bulk} * t_{bulk}$$



# Proposed Approach: Charge Model



Bulk:

$$\widehat{RC}_{bulk} = c_1 * \frac{\delta V}{\delta t} + c_0$$

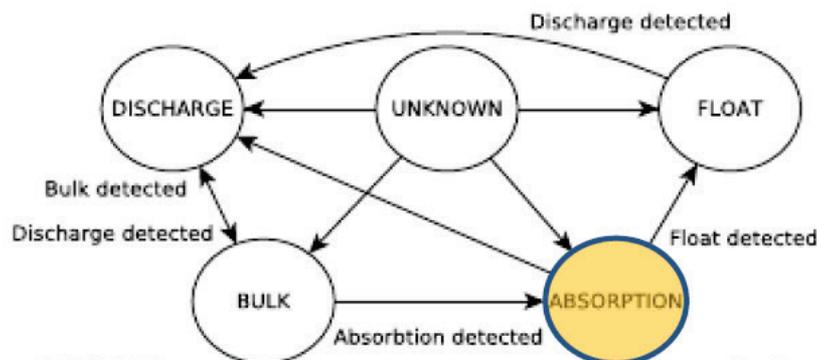
$$\widehat{SOC}(t) = \widehat{SOC}(t - t_{bulk}) + \widehat{RC}_{bulk} * t_{bulk}$$

Absorption:

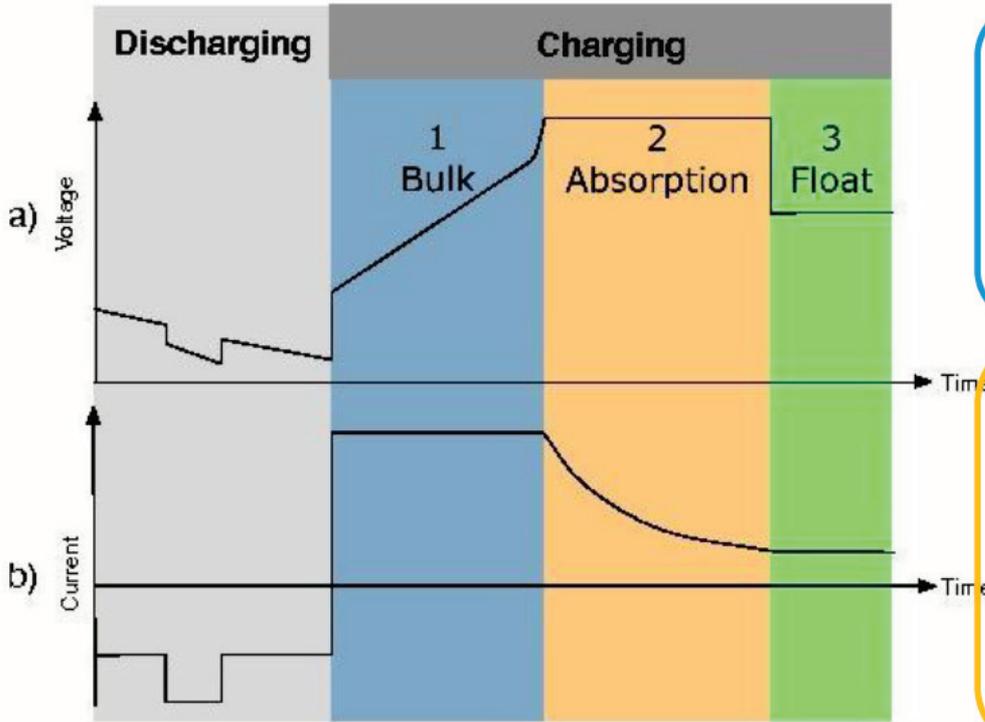
$$\widehat{RC}_{abs}(t) = \widehat{RC}_{bulk} * e^{(\lambda(\widehat{RC}_{bulk})*t_{abs})}$$

$$\lambda(\widehat{RC}_{bulk}) = d_1 * \widehat{RC}_{bulk} + d_0$$

$$\widehat{SOC}(t) = \widehat{SOC}(t - t_{abs}) + \widehat{RC}_{abs} * t_{abs}$$



# Proposed Approach: Charge Model



**Bulk:**

$$\widehat{RC}_{bulk} = c_1 * \frac{\delta V}{\delta t} + c_0$$

$$\widehat{SOC}(t) = \widehat{SOC}(t - t_{bulk}) + \widehat{RC}_{bulk} * t_{bulk}$$

**Absorption:**

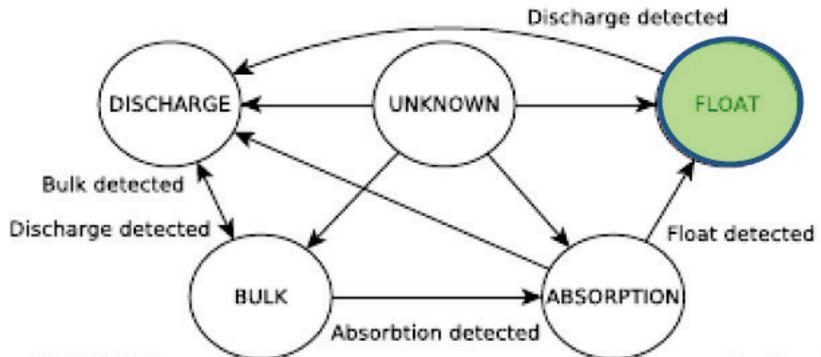
$$\widehat{RC}_{abs}(t) = \widehat{RC}_{bulk} * e^{(\lambda(\widehat{RC}_{bulk})*t_{abs})}$$

$$\lambda(\widehat{RC}_{bulk}) = d_1 * \widehat{RC}_{bulk} + d_0$$

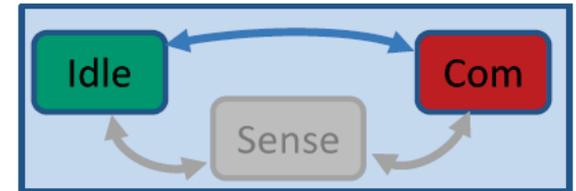
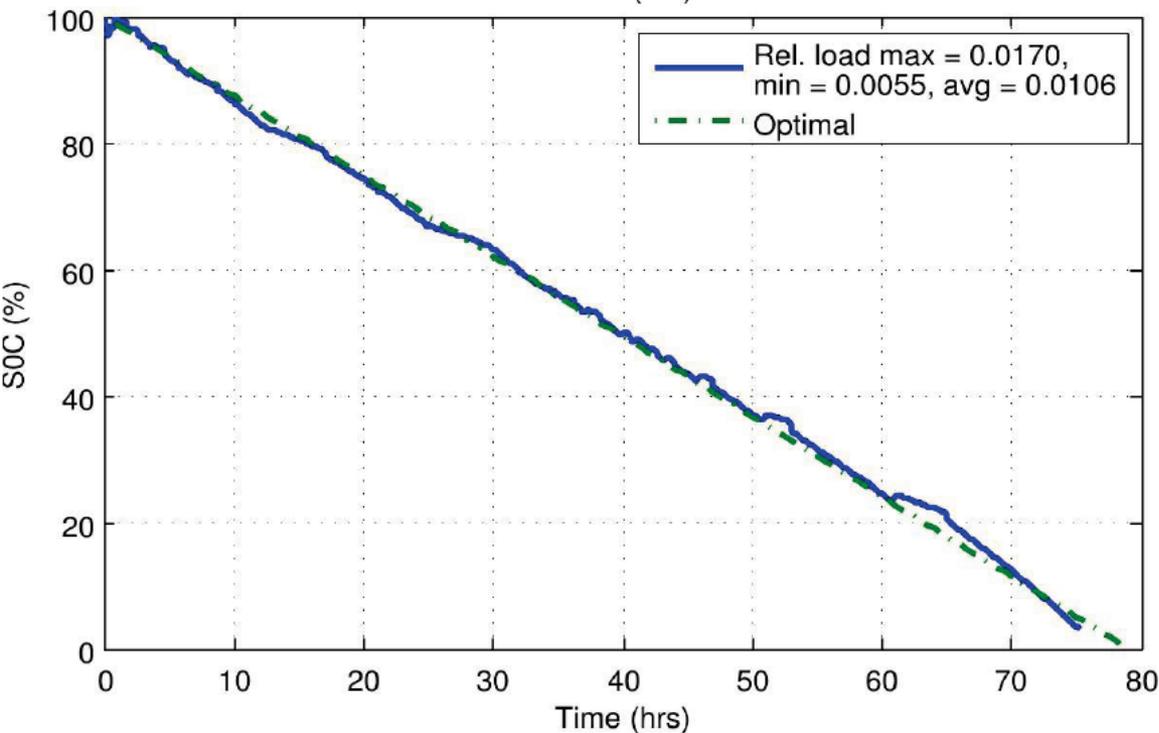
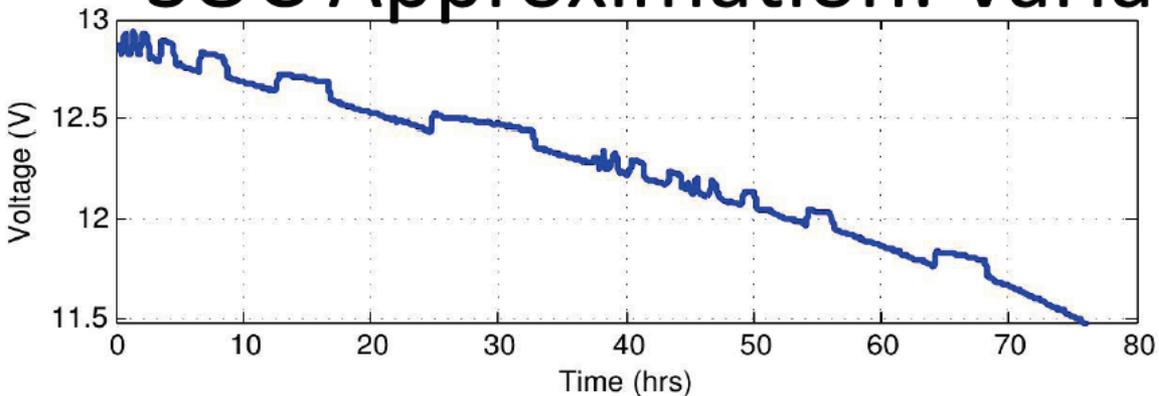
$$\widehat{SOC}(t) = \widehat{SOC}(t - t_{abs}) + \widehat{RC}_{abs} * t_{abs}$$

**Float:**

$$\widehat{SOC}(t) = 100\%$$



# SOC Approximation: Variable Load (BAT 3)



SOC estimation error (%):

Max	Min	Mean	Var.	Std.
4.98	-0.79	3.02	4.53	2.13

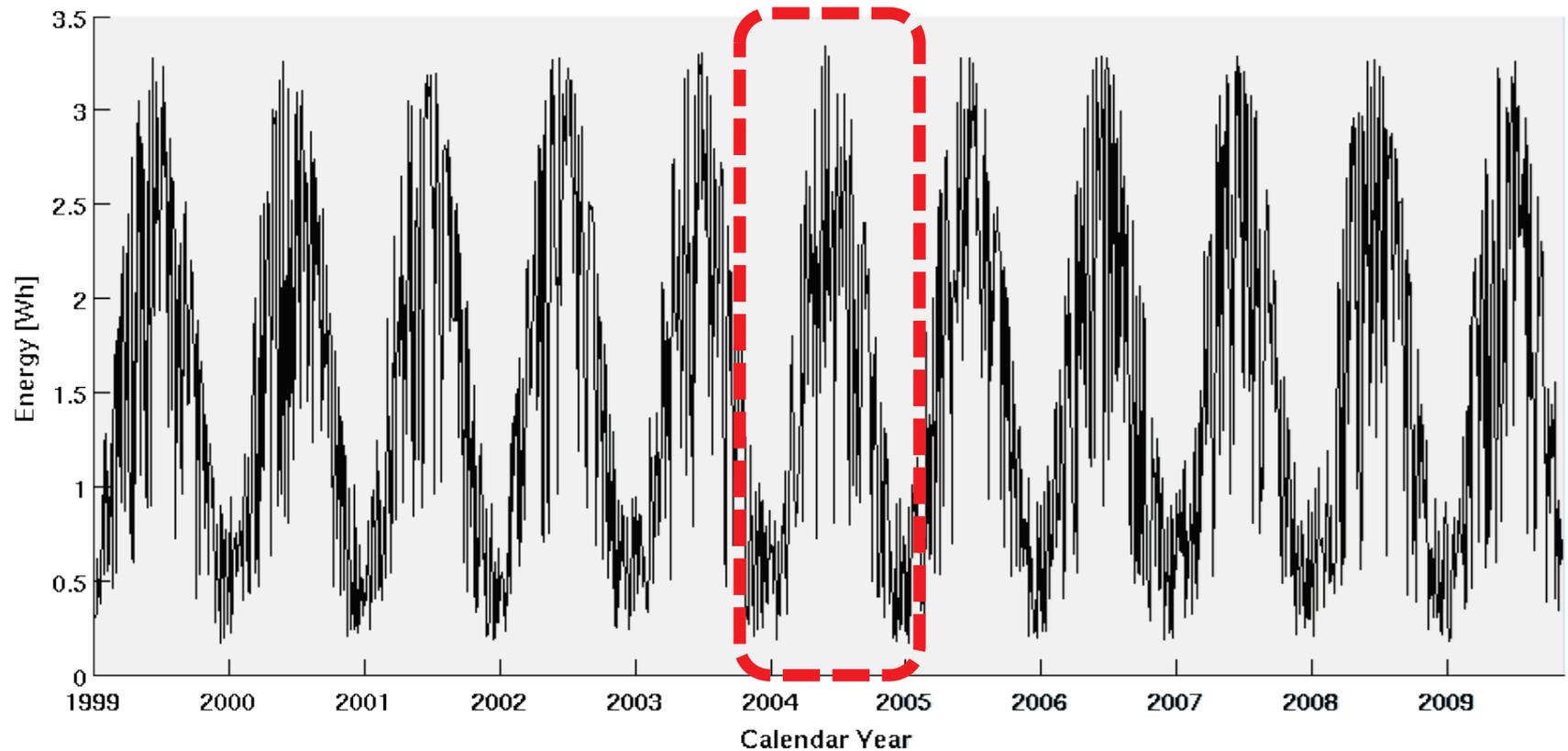
$$Error = SOC_{model} - SOC_{opt}$$

$$f_s = \frac{1}{60 \text{ sec}}$$

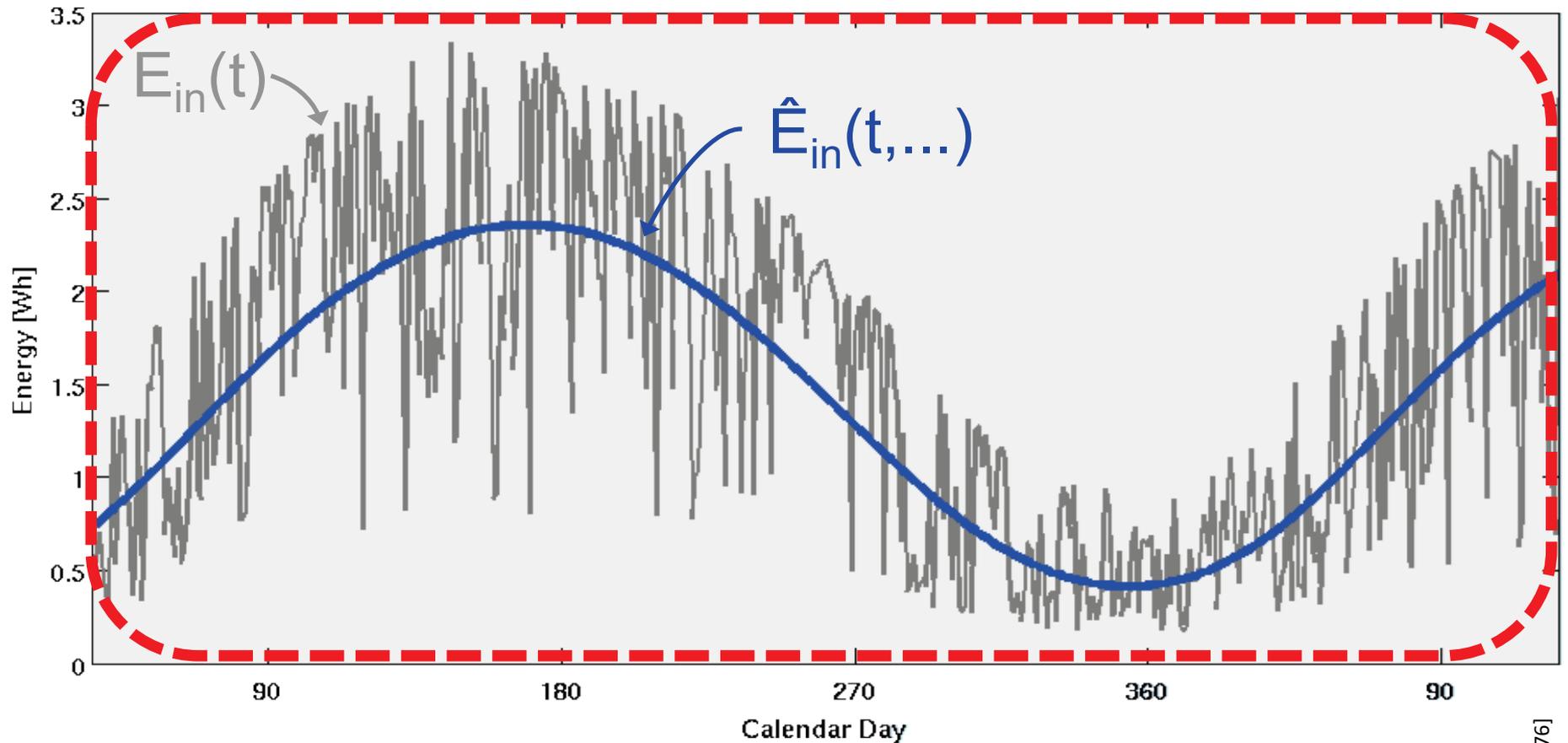
Low-Power System Design

# **LONG-TERM ENERGY NEUTRAL OPERATION – CAPACITY PLANNING**

# High Day-to-Day Relatively Low Year-to-Year Variability

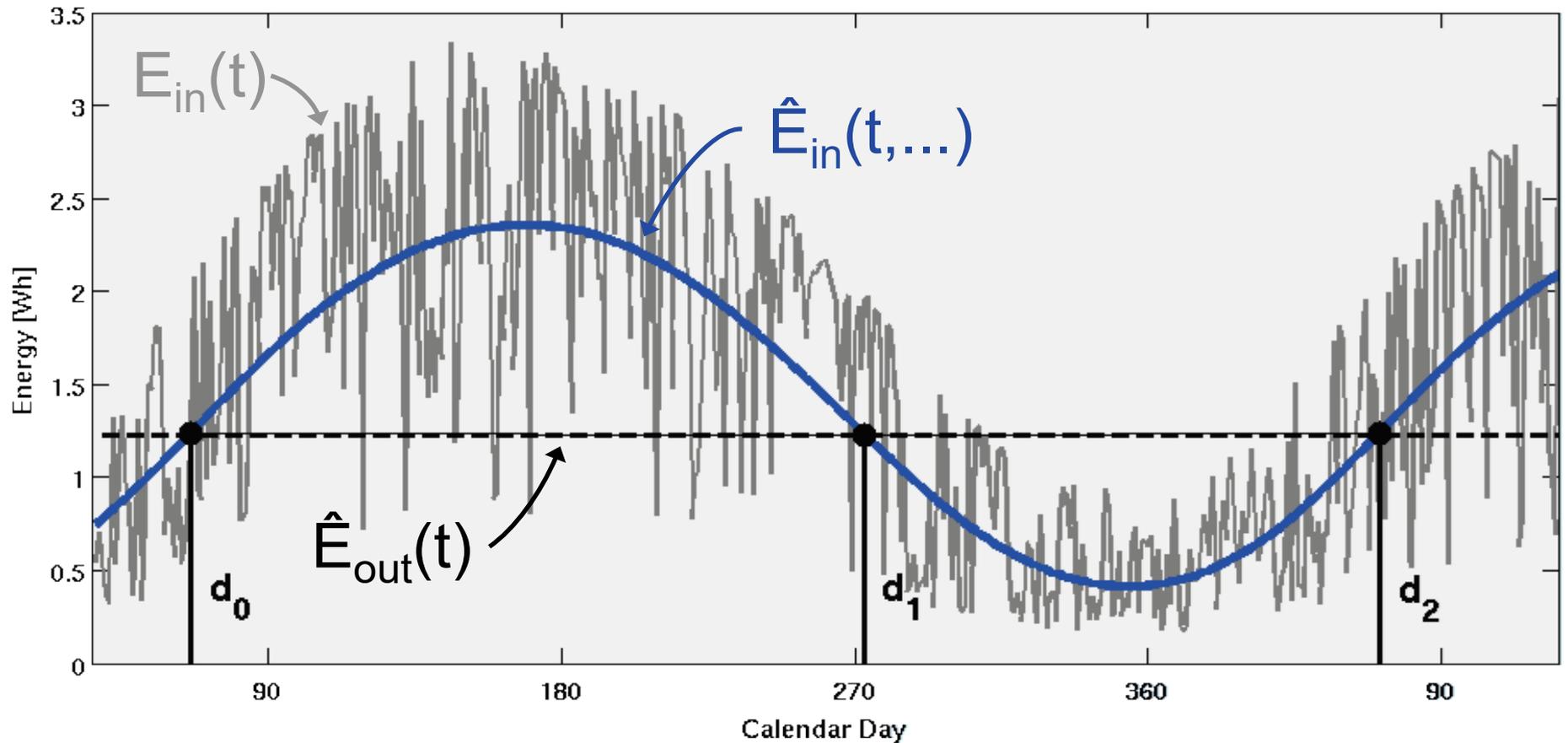


# Approximation by Astronomical Model

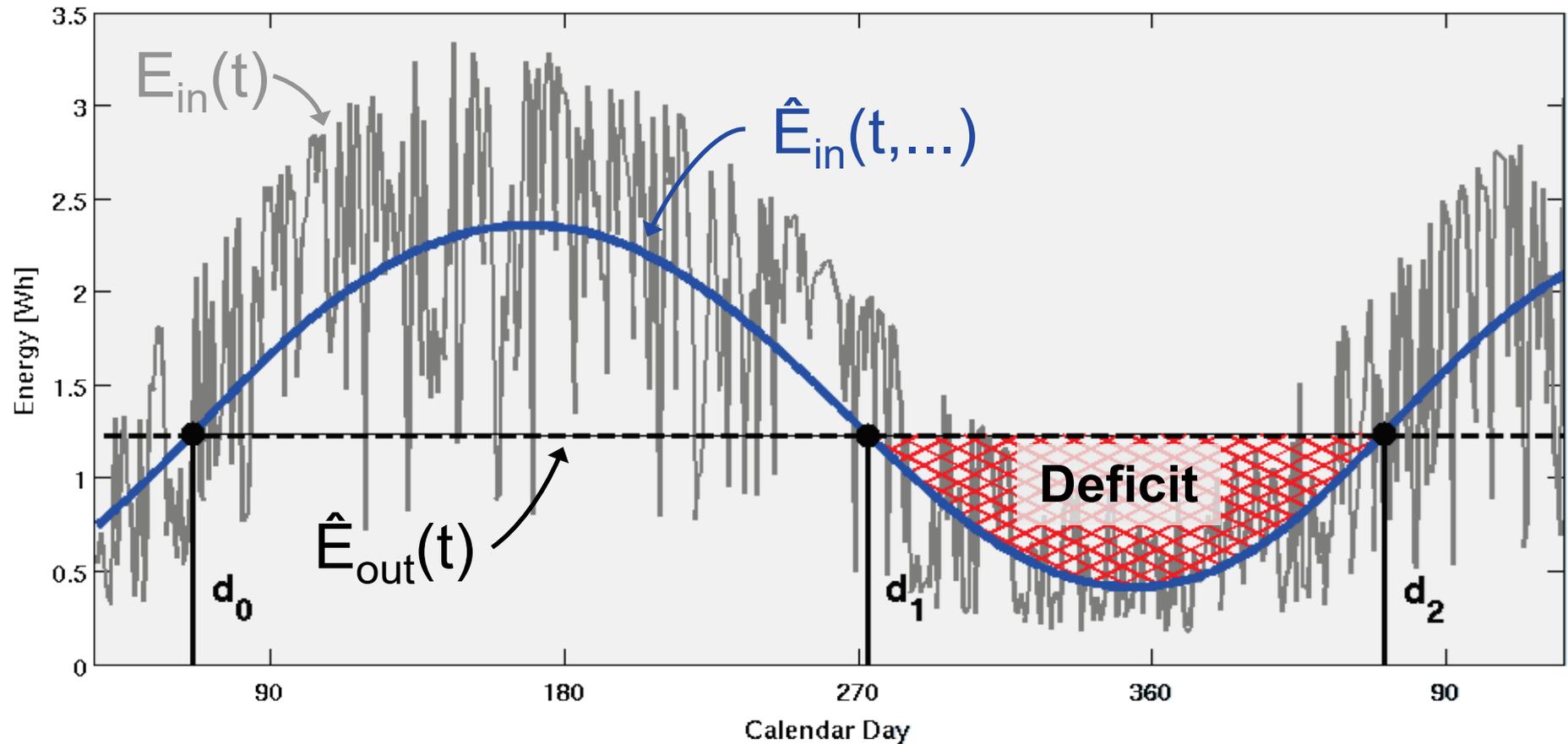


[Dave '76]

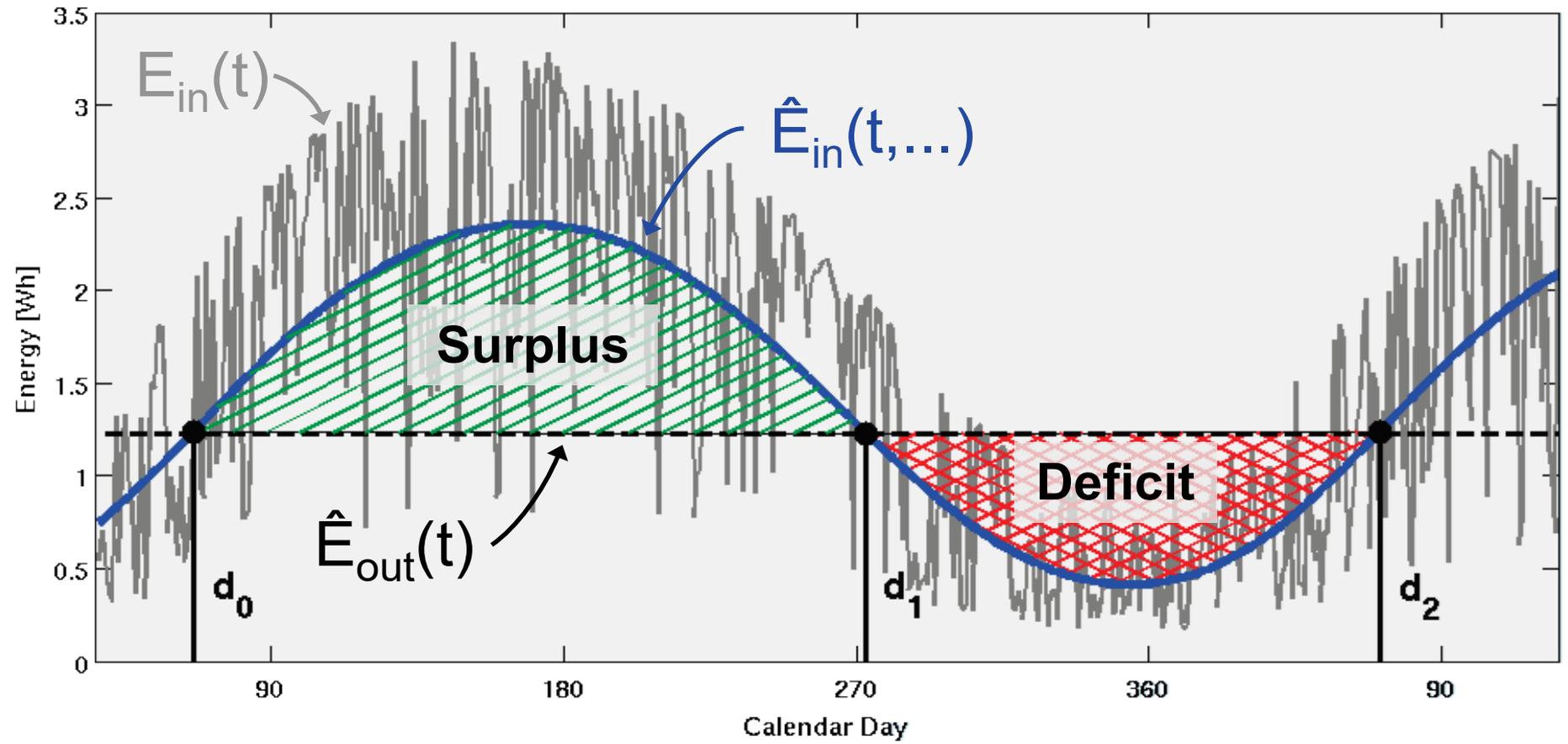
# Energy Profile Partitions into Surplus and Deficit



# Period of Continuous Deficit Defines Minimum Required Battery Capacity



# Period of Energy Surplus Defines Maximum Battery Capacity Supported by Solar Panel

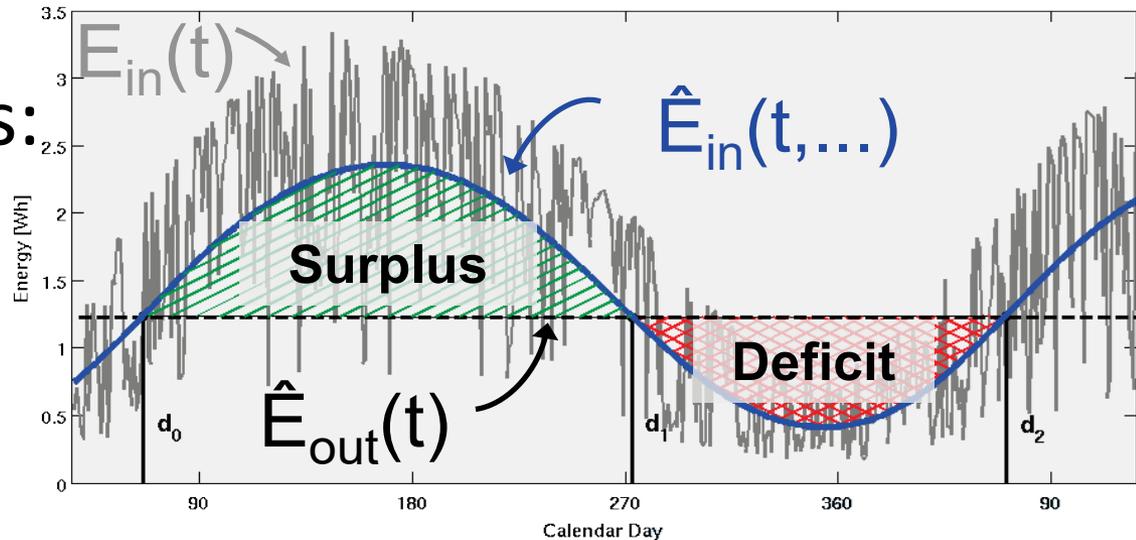


# Capacity planning for Uninterrupted Long-Term Operation

Periods of continuous:

-surplus:  $d_0$  to  $d_1$

-deficit:  $d_1$  to  $d_2$



Battery capacity:

$$B_{\text{nom}} \geq \sum_{t=d_1}^{d_2} (\hat{E}_{\text{out}}(t) - \hat{E}_{\text{in}}(\cdot))$$

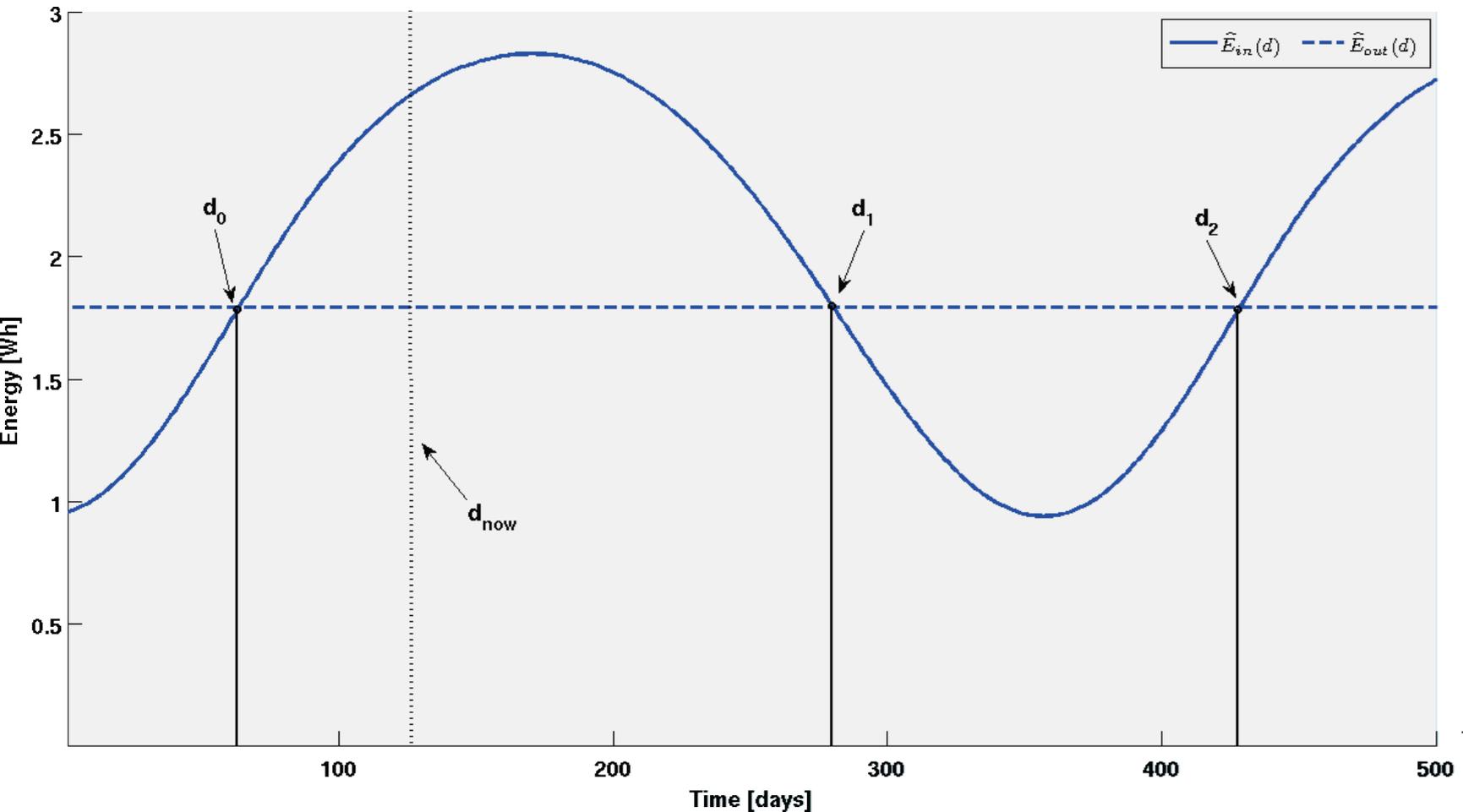
And panel size such that:

$$\sum_{t=d_0}^{d_1} \hat{E}_{\text{in}}(\cdot) \geq B_{\text{nom}} + \sum_{t=d_0}^{d_1} \hat{E}_{\text{out}}(t)$$

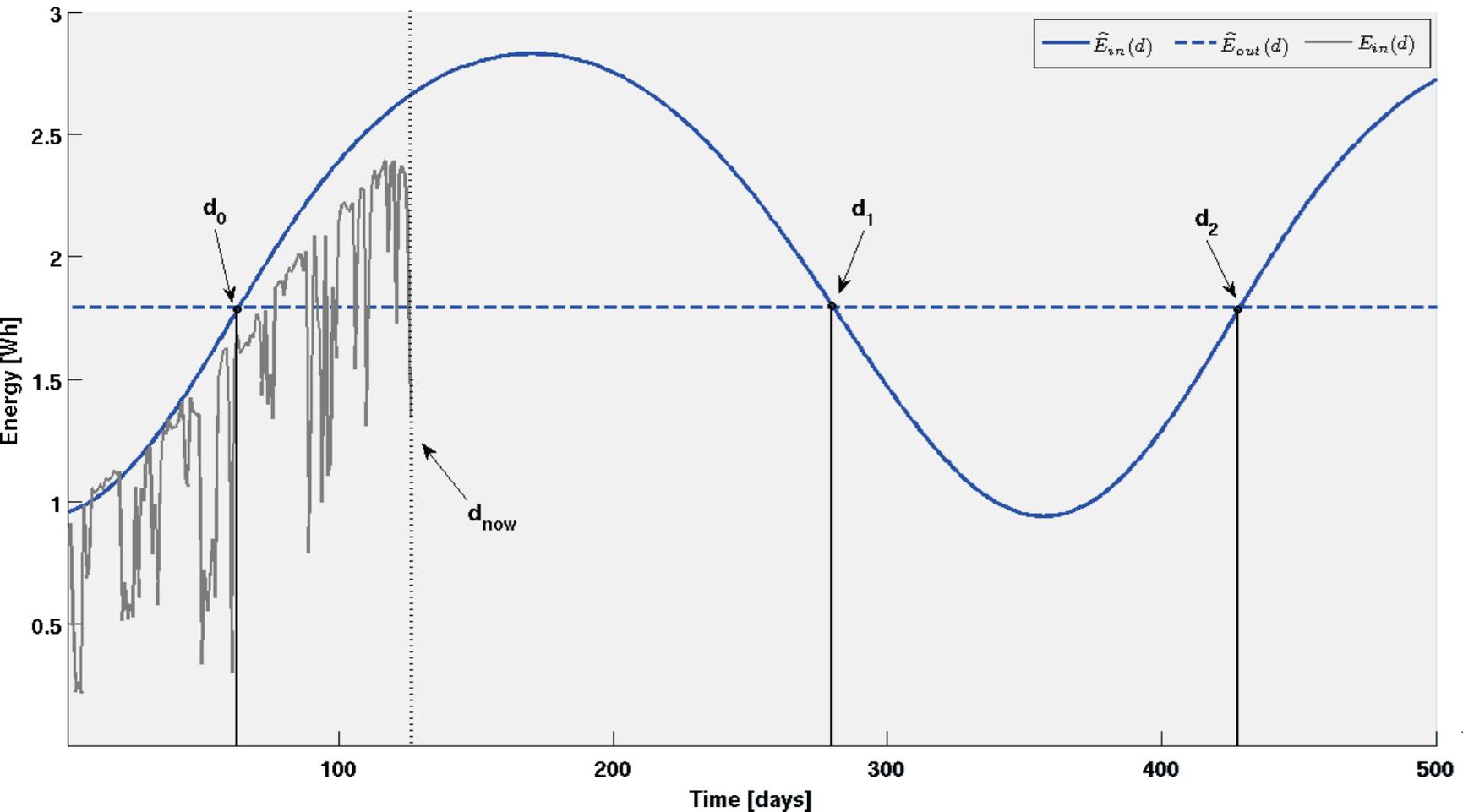
Low-Power System Design

# **LONG-TERM ENERGY NEUTRAL OPERATION – DYNAMIC POWER MANAGEMENT**

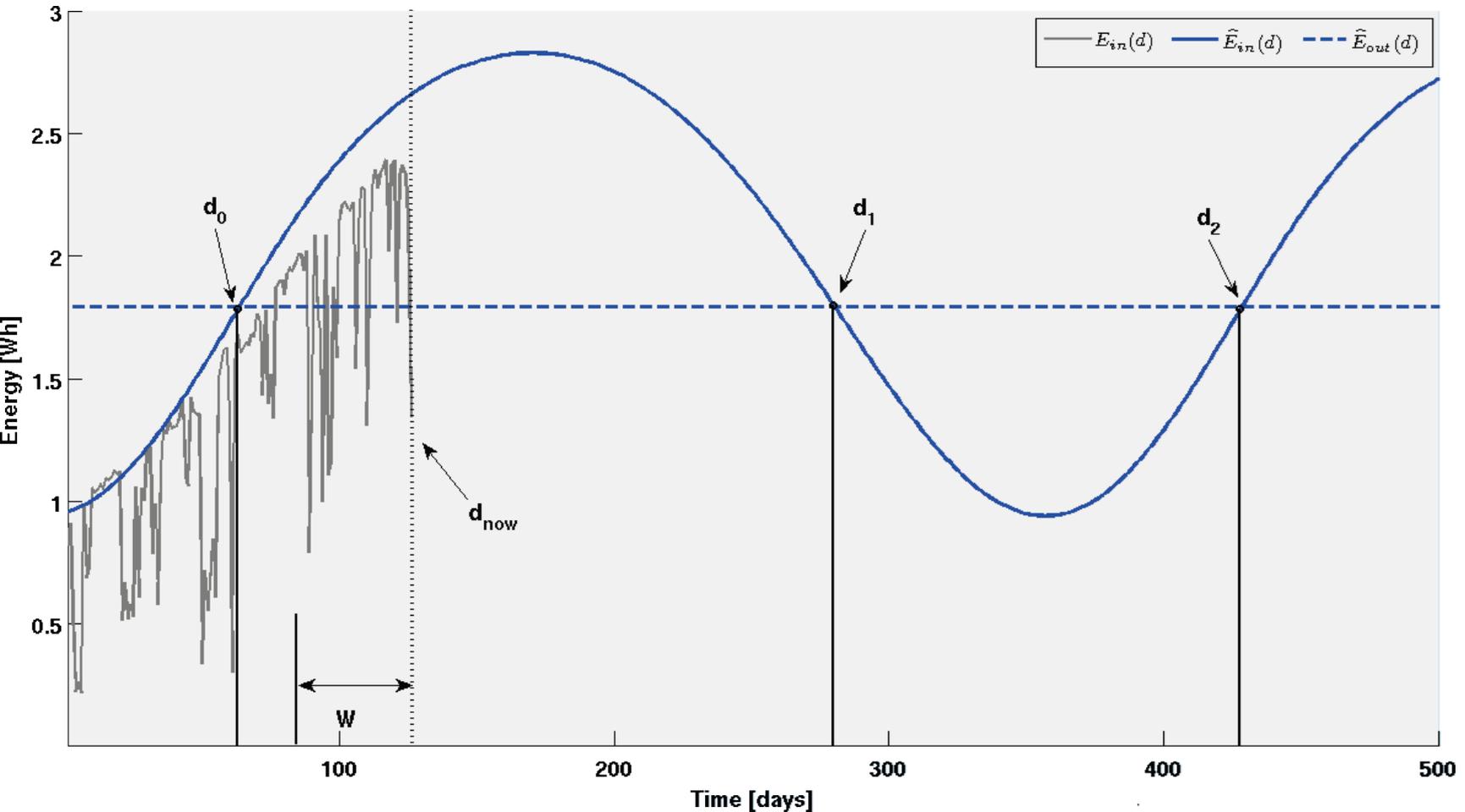
# DPM knows Energy Input Profile Used for Capacity Planning



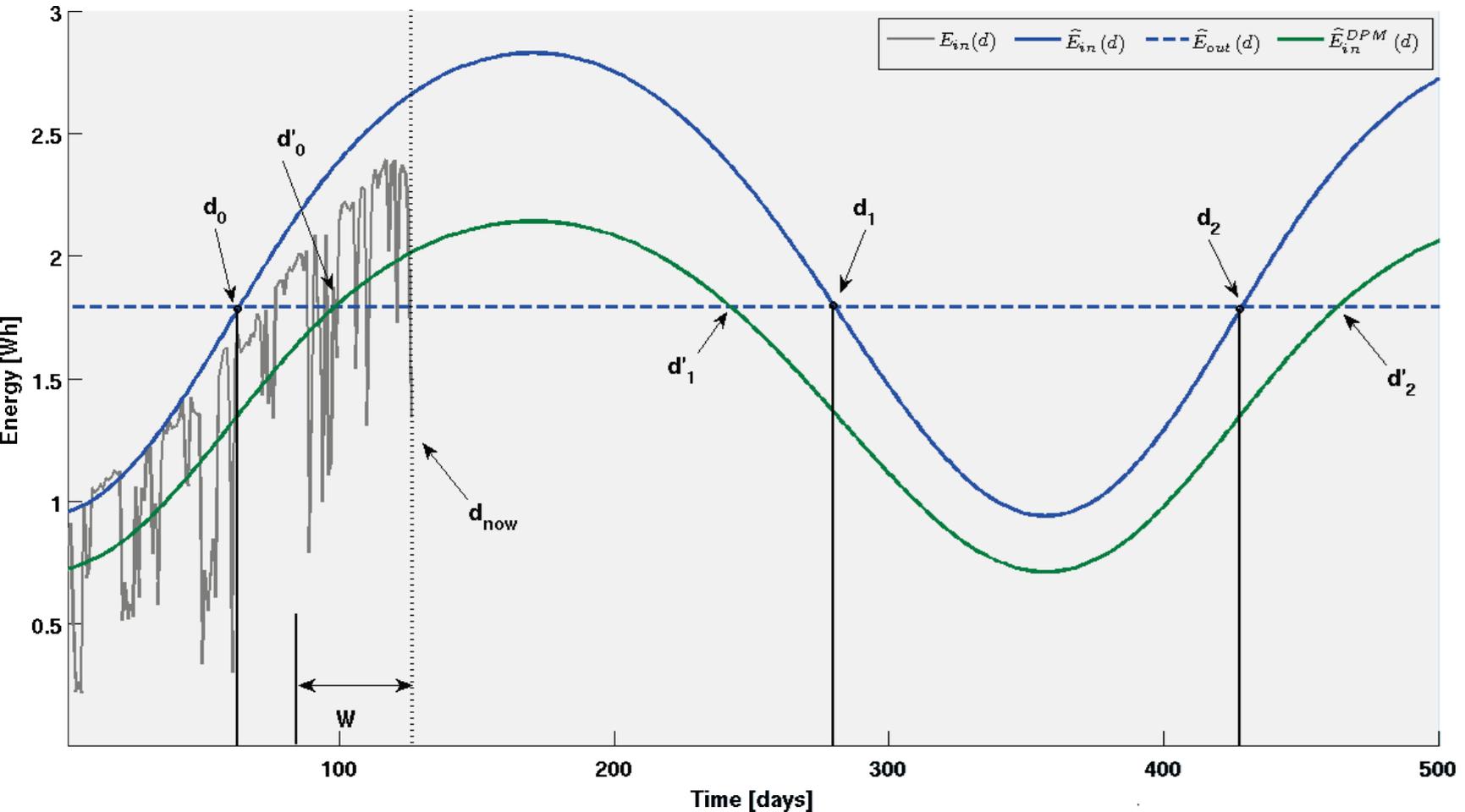
# Performance Level Adjustment According to Actual Conditions



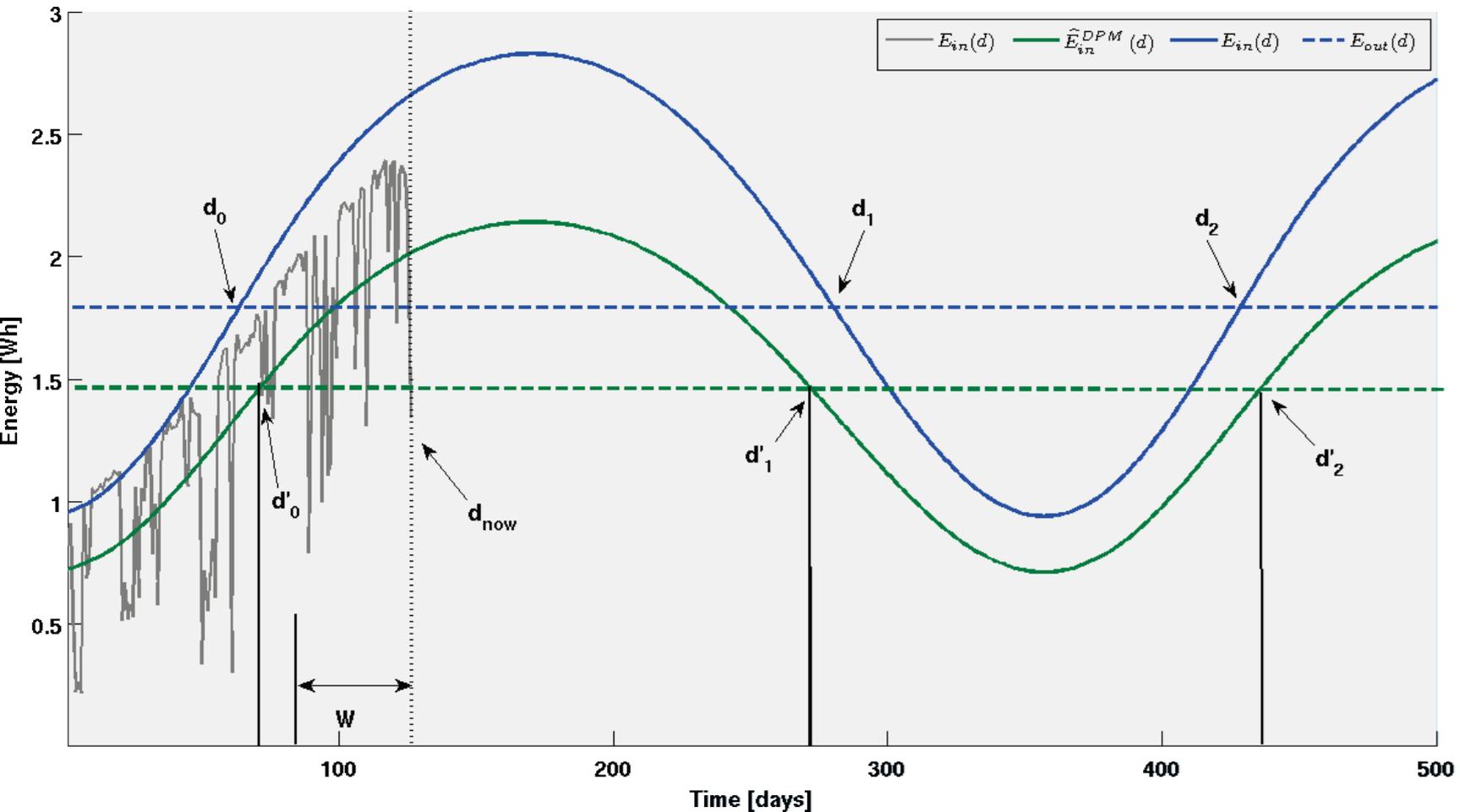
# Step 1: Approximate Energy Availability Using History Window and Offline Model



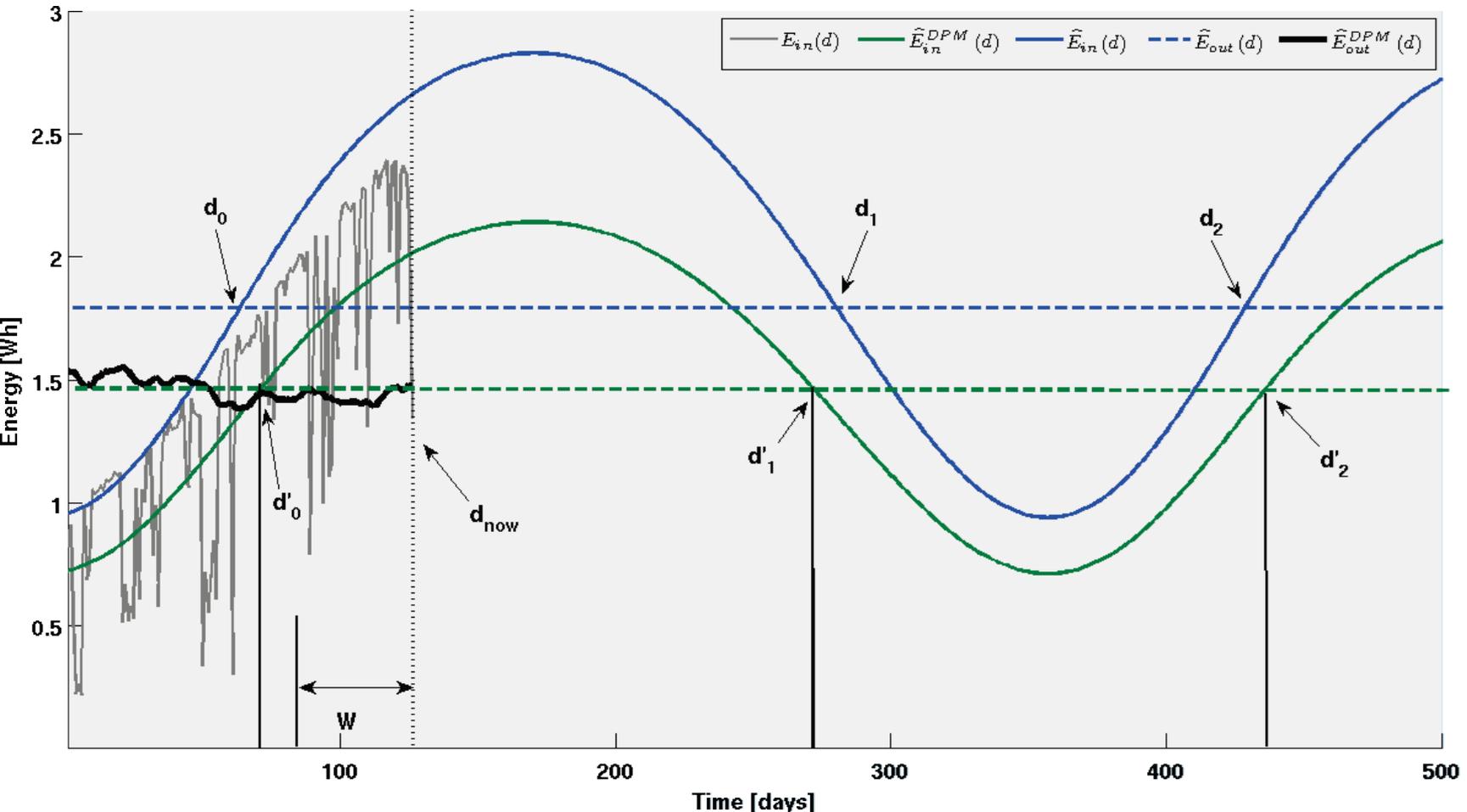
# Step 2: Find Long-Term Performance Level



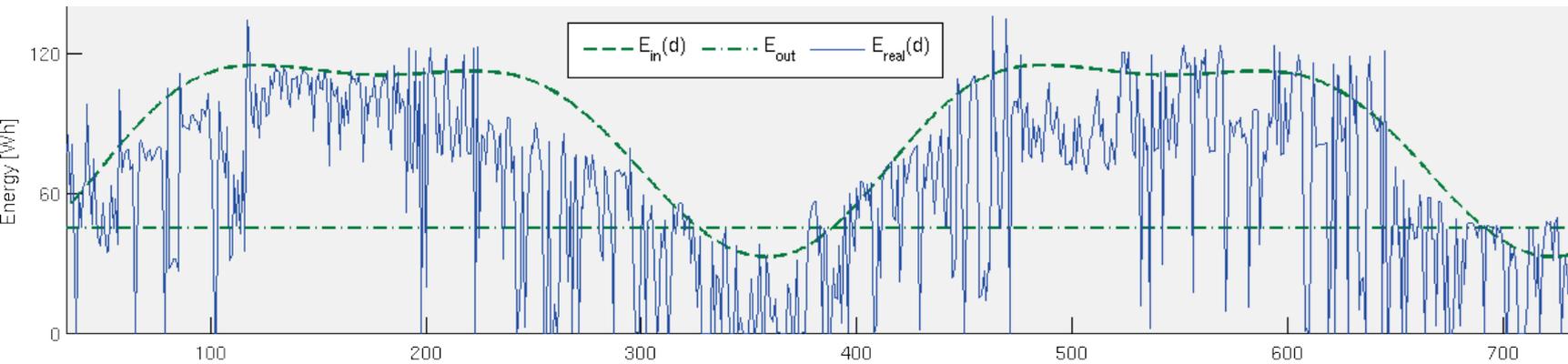
# Step 2: Find Long-Term Performance Level



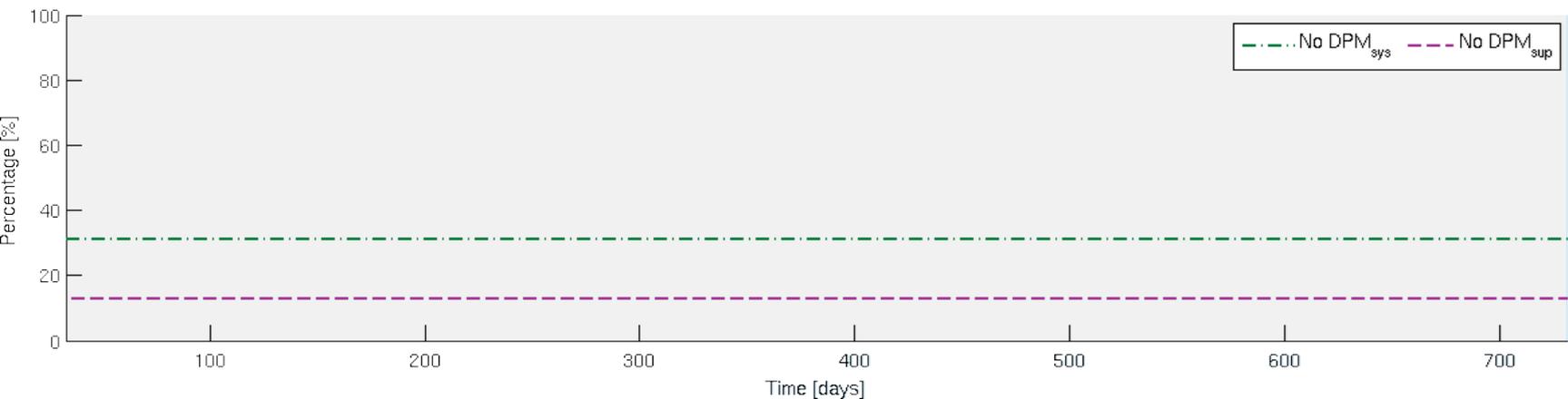
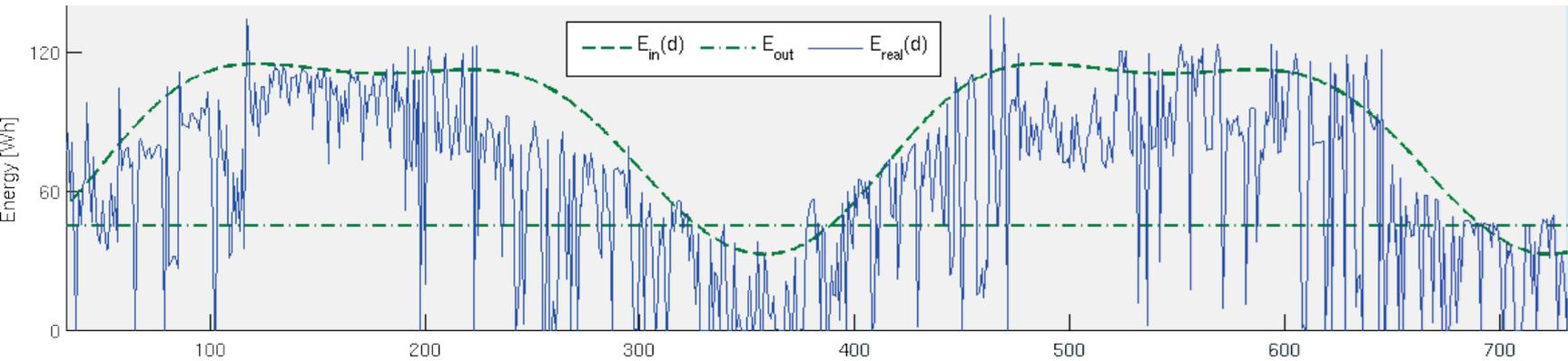
# DPM Ensures Long-Term Energy Neutrality



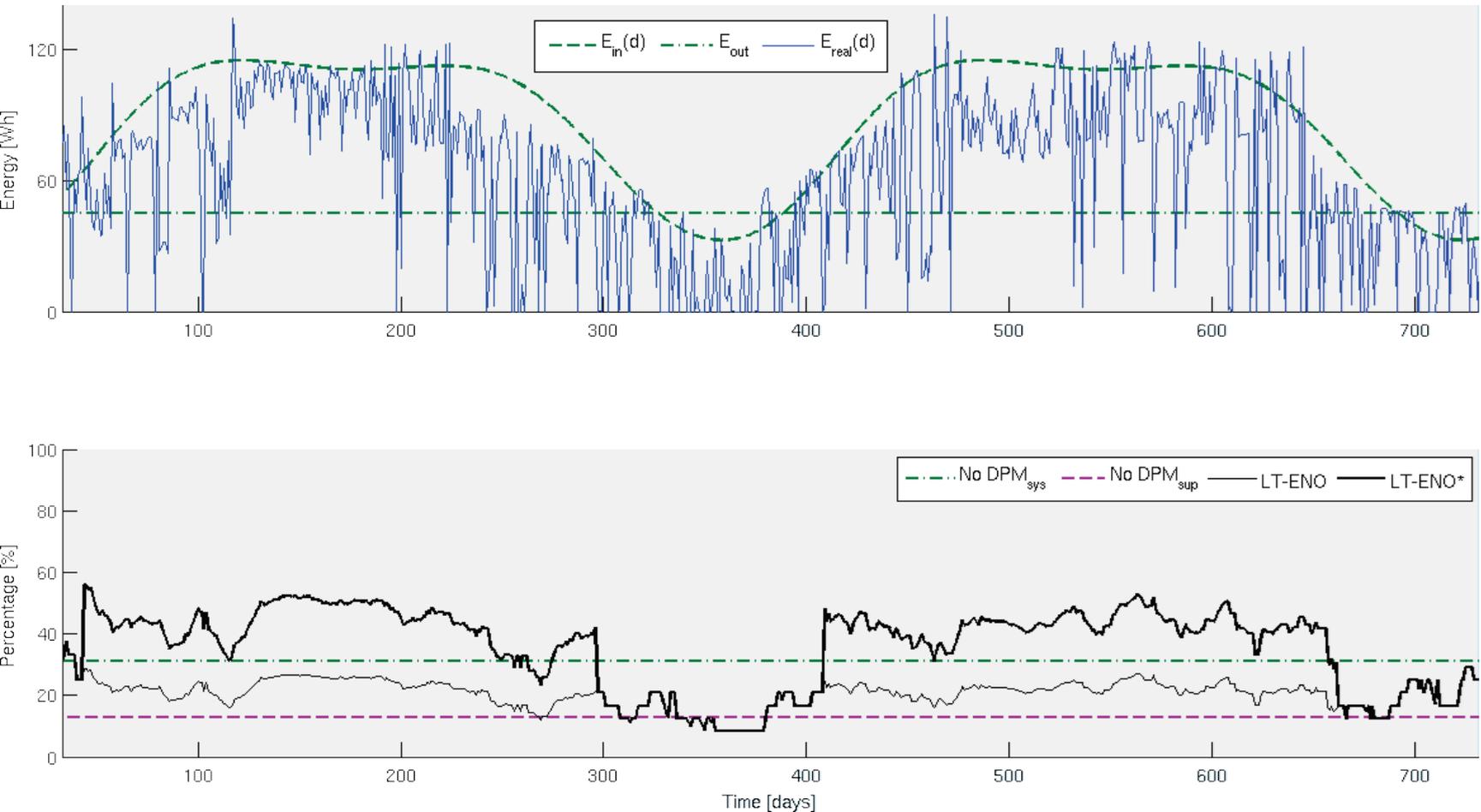
# Caveat: Energy Availability Model Overestimates True Conditions



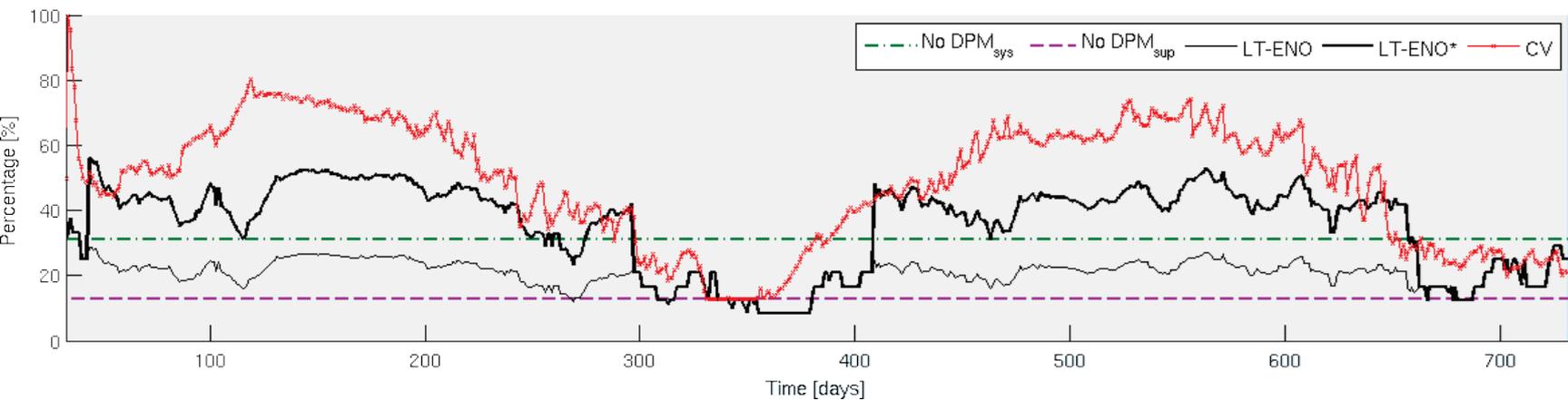
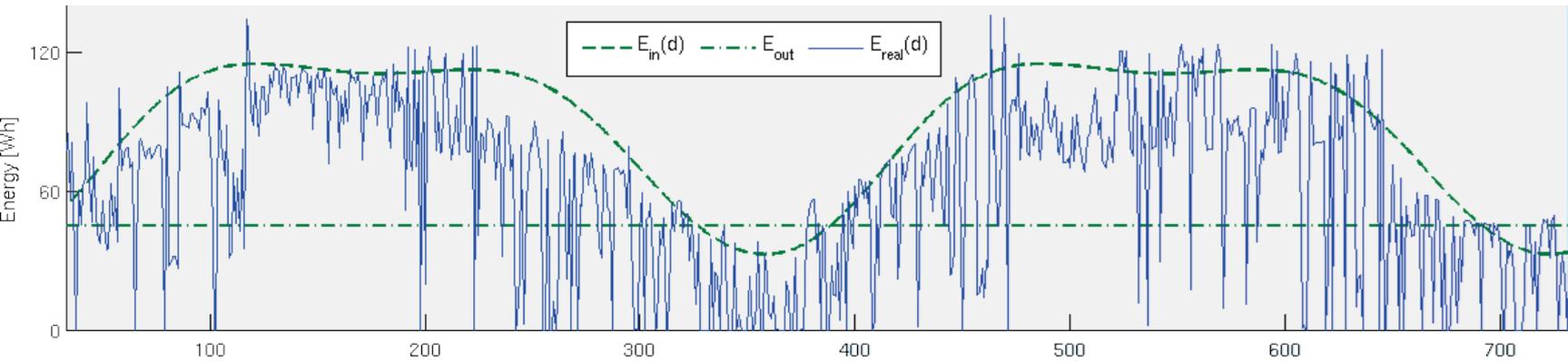
# Supported Performance Level According Model/True Conditions (no DPM)



# Long-Term Energy Neutral DPM



# Clairvoyant Energy Predictor



# Recap of Today

- All energy storage technologies have severe limitations
- Battery technology is slow in improvement vs. Moores Law
- Energy scavenging methods are widely researched
  - No real breakthrough yet
  - Most promising is solar and mechanical, TEGs play a side role
  - Increased complexity through control
- LP architectures are increasingly designed with power subsystem in mind

# Today's Hot Researcher & Paper

- Shad Roundy
  - Faculty Mechanical Engineering  
University of Utah  
(Integrated Self-Powered Sensing Lab)
  - PhD University of California, Berkeley
- Very early work on energy harvesting systems
  - Focus on vibration energy sources
- Roundy, S., Wright PK, Rabaey JM 2003. *Energy Scavenging for Wireless Sensor Networks*, Kluwer Academic Publishers, Boston MA.
- Briand, D., Yeatman, E., Roundy, S., (Eds.). (2015). *Micro Energy Harvesting (Advanced Micro and Nanosystems)* . John Wiley & Sons.

